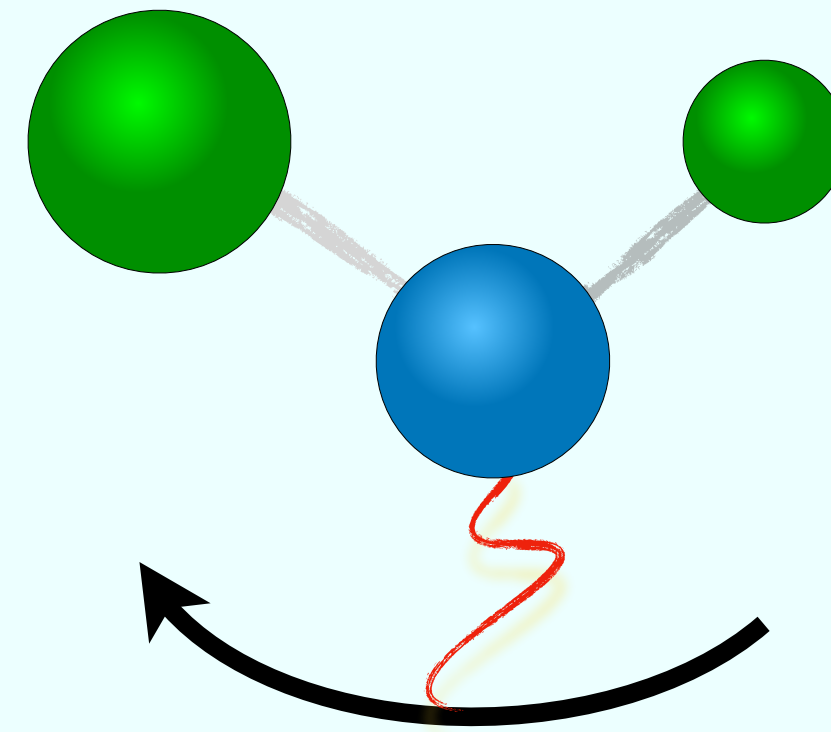




# SINGLE MESON ELECTROPRODUCTION



*Maxim Mai*

[Jülich-Bonn-Washington (JBW) collaboration]

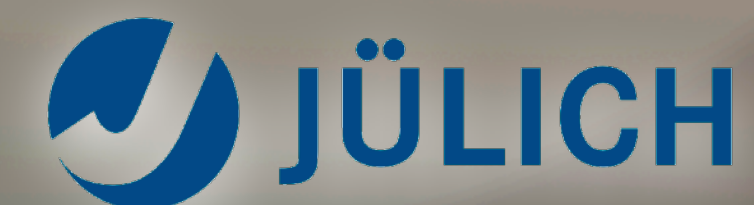
*M. Döring, J. Hergenrather, C. Granados, H. Haberzettl, Ulf-G. Meißner, D. Rönchen, I. Strakovsky, R. Workman*

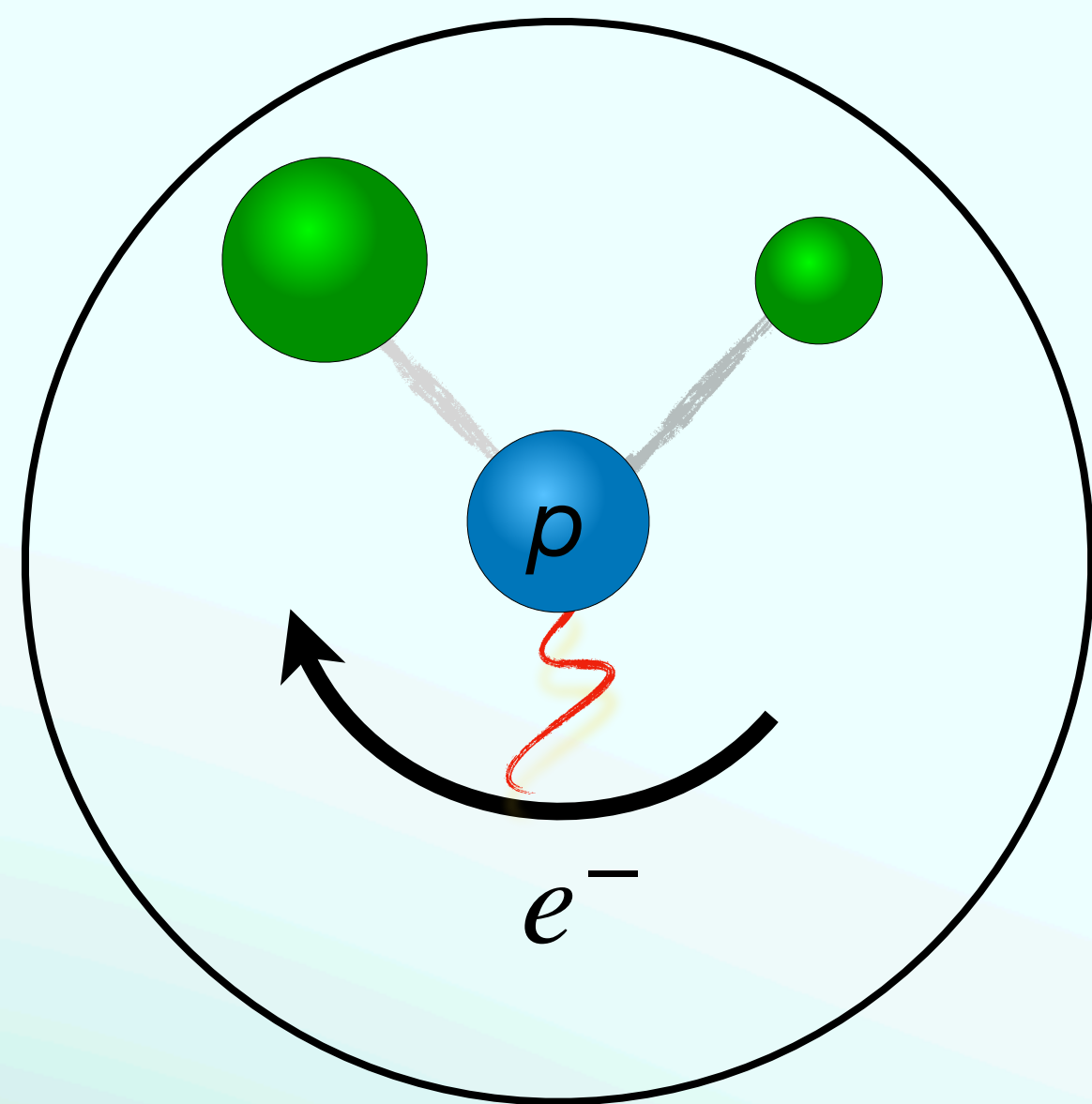


DE-SC0016582  
DE-SC0016583



THE GEORGE  
WASHINGTON  
UNIVERSITY  
WASHINGTON, DC





# INTRODUCTION



# NATURE'S LANGUAGE



## Quantum mechanics

- governs subatomic world
- unconventional language
- various interpretations

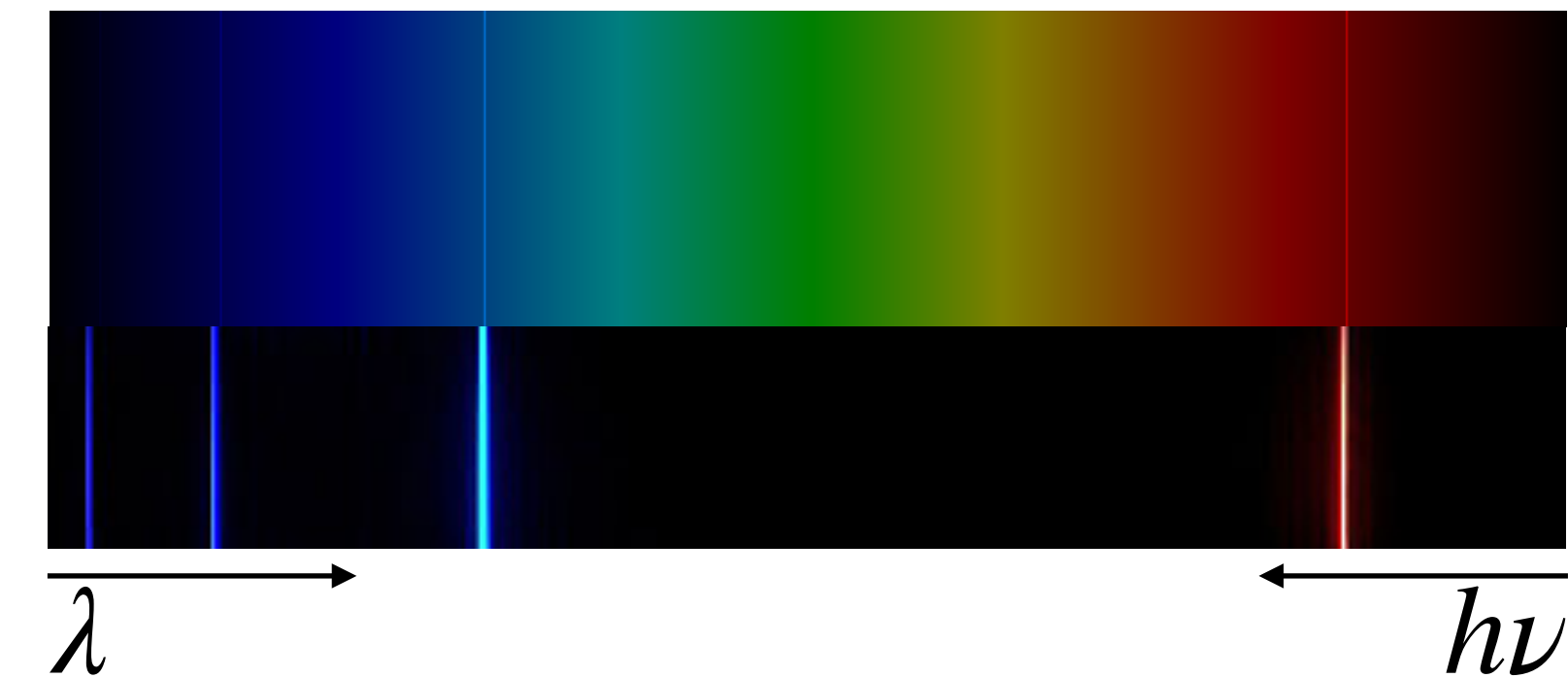
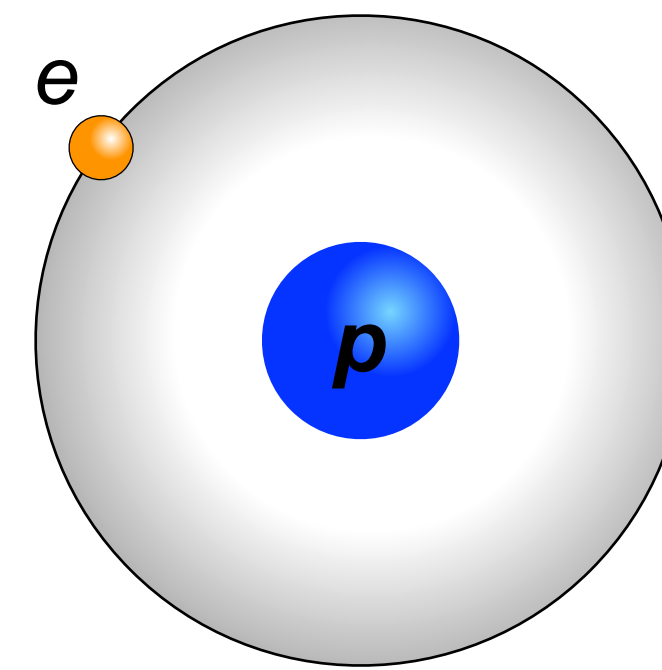
"If you think you understand quantum mechanics then you don't understand quantum mechanics"  
R. P. Feynman

# NATURE'S LANGUAGE



## Breakthrough

- explanation of atomic spectra
- discrete excitation energies
- new paradigm of physics



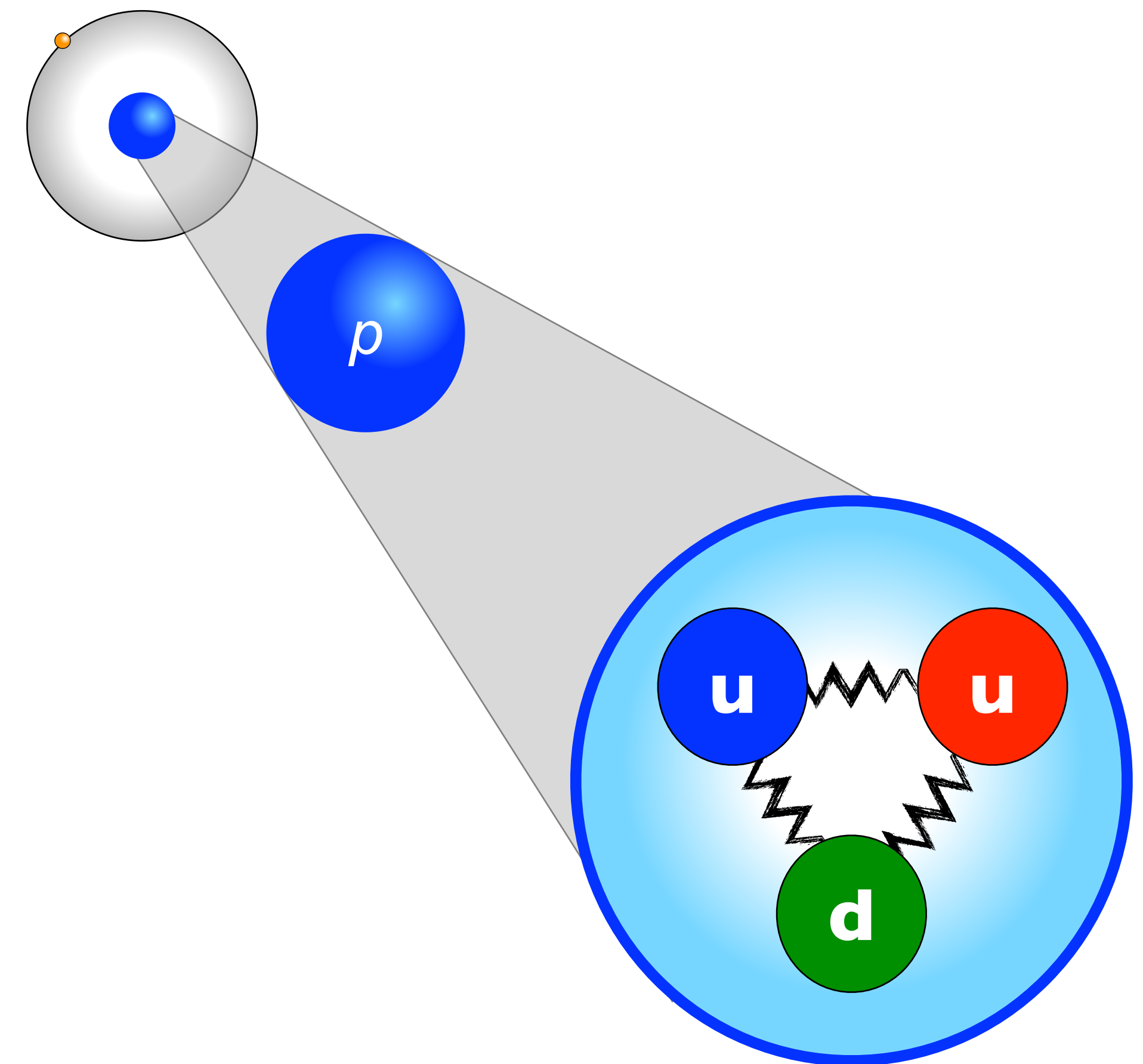
$$\Delta E \sim \frac{1}{n^2} - \frac{1}{m^2}$$

# NATURE'S LANGUAGE



## Protons/neutrons

- 99% of the mass of visible matter in the universe
- bound and interact via **strong force**
- part of a large class of particles: **hadrons**
- building blocks: **quarks & gluons**



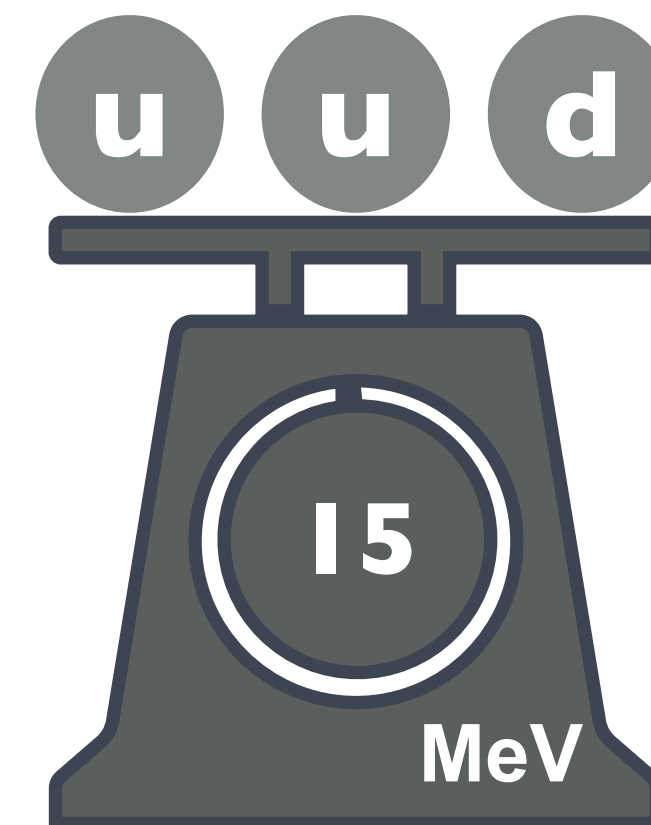


# NATURE'S LANGUAGE

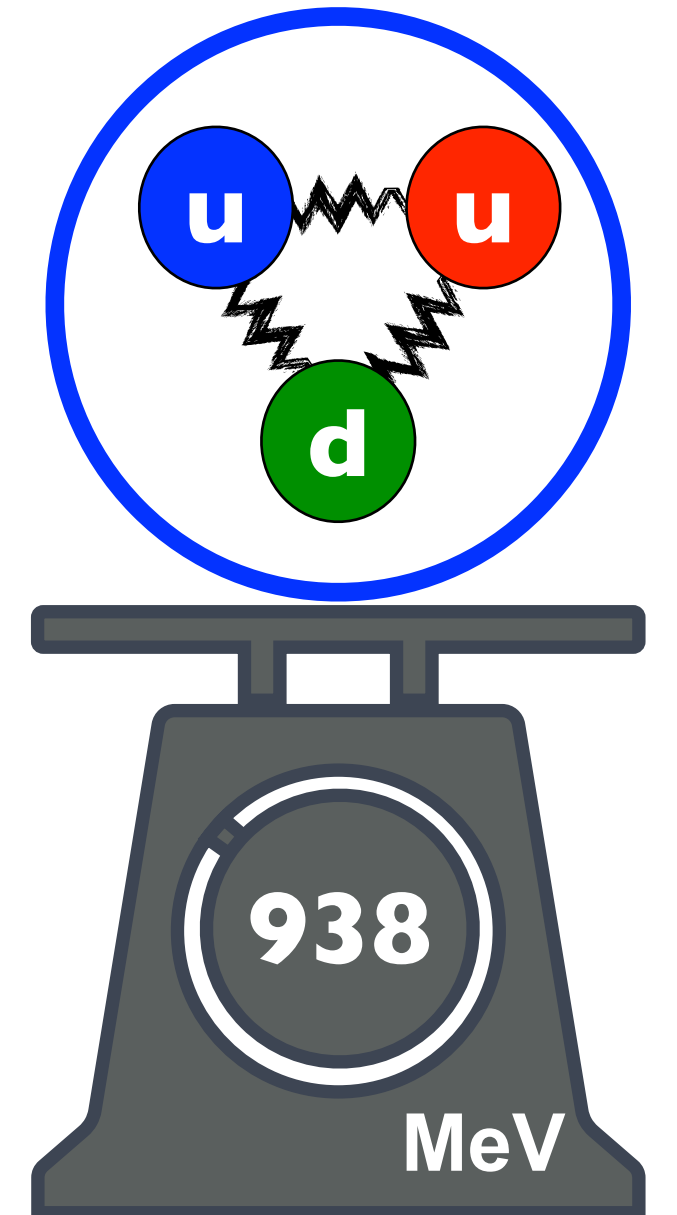


## Mass puzzle:

- quarks are too light  $\Rightarrow$  constituent quark model?
- Lattice QCD<sup>1</sup>: ~90% of mass is generated by dynamical effects



Higgs mechanism



Dynamics of gluons and quarks

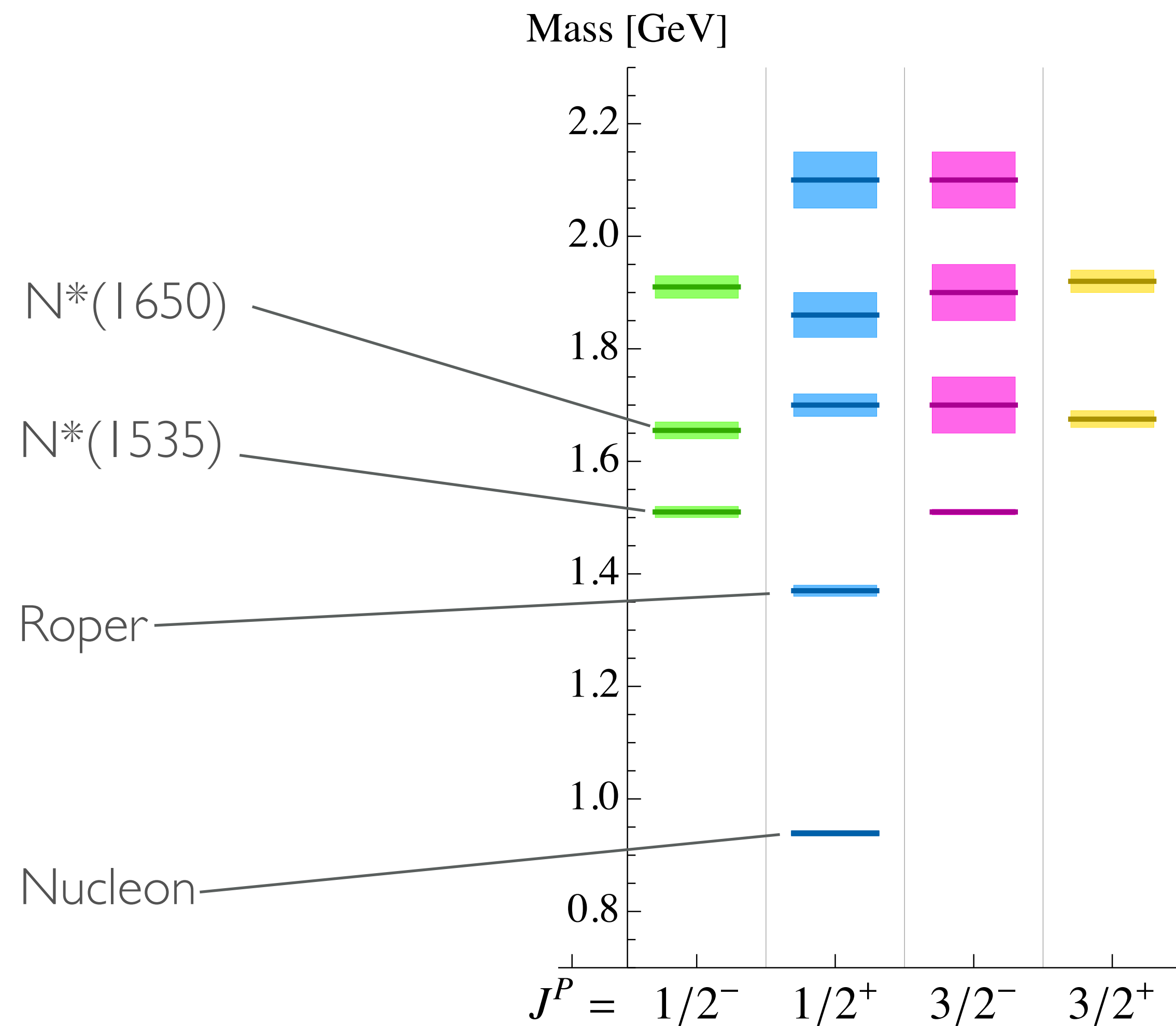
1) Durr et al. *Science* 322 (2008)



# HADRON SPECTRUM



- PDG: ~100(50) excited meson(baryon) states  
(\*\*\*\*)



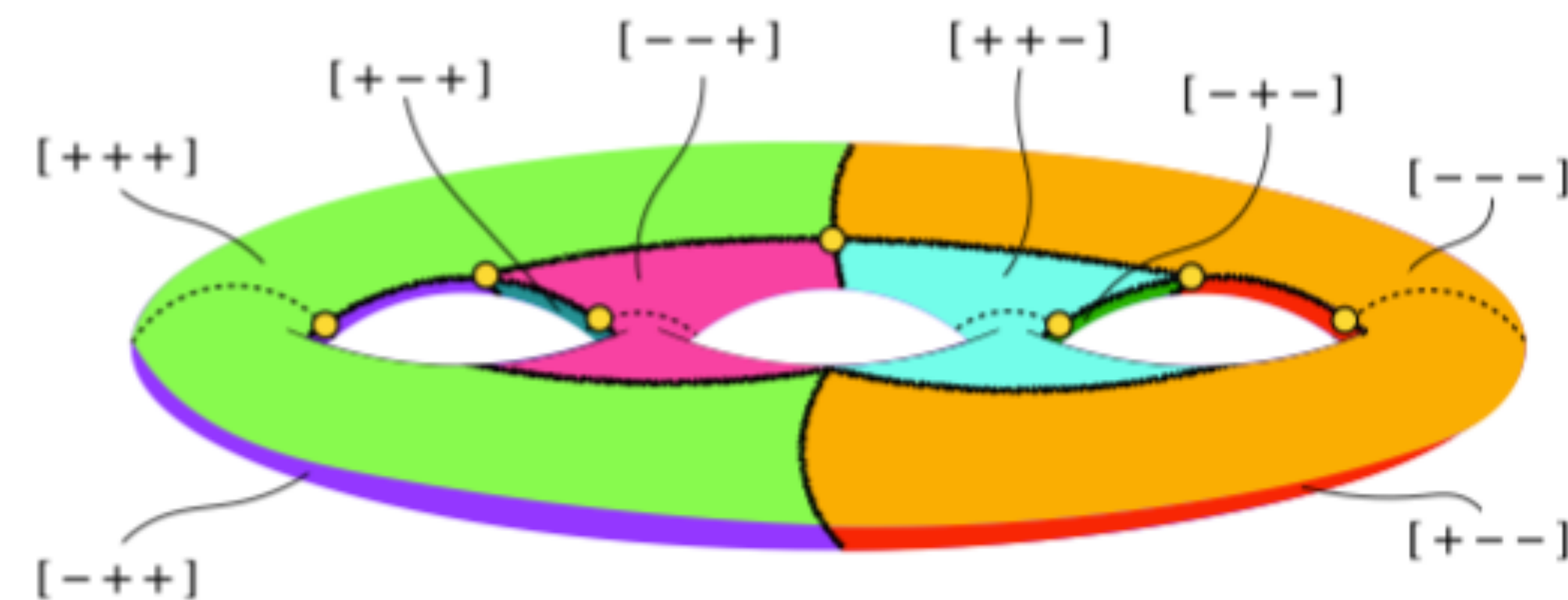
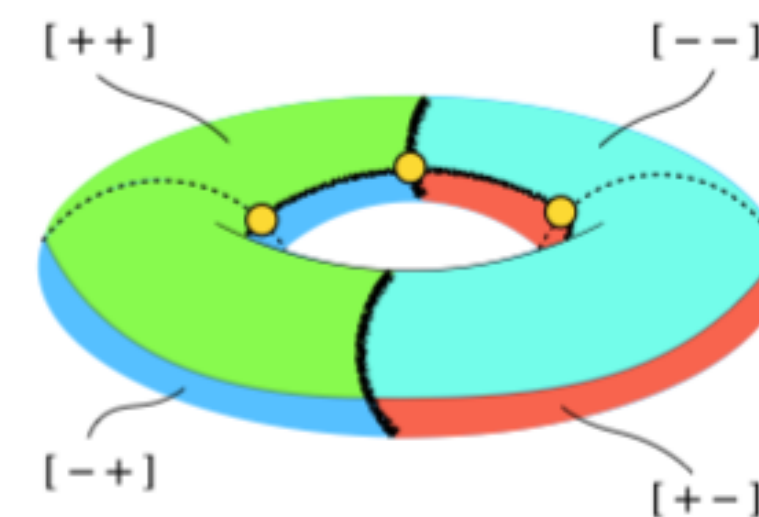
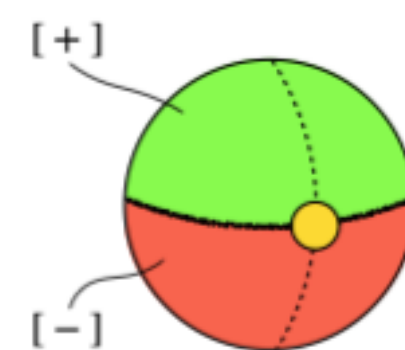
Values.: Particle Data Goup (**Workman** et al.)



# HADRON SPECTRUM



- reaction-independent (*universal*) parameters:  
 > *poles on the Riemann Surface*



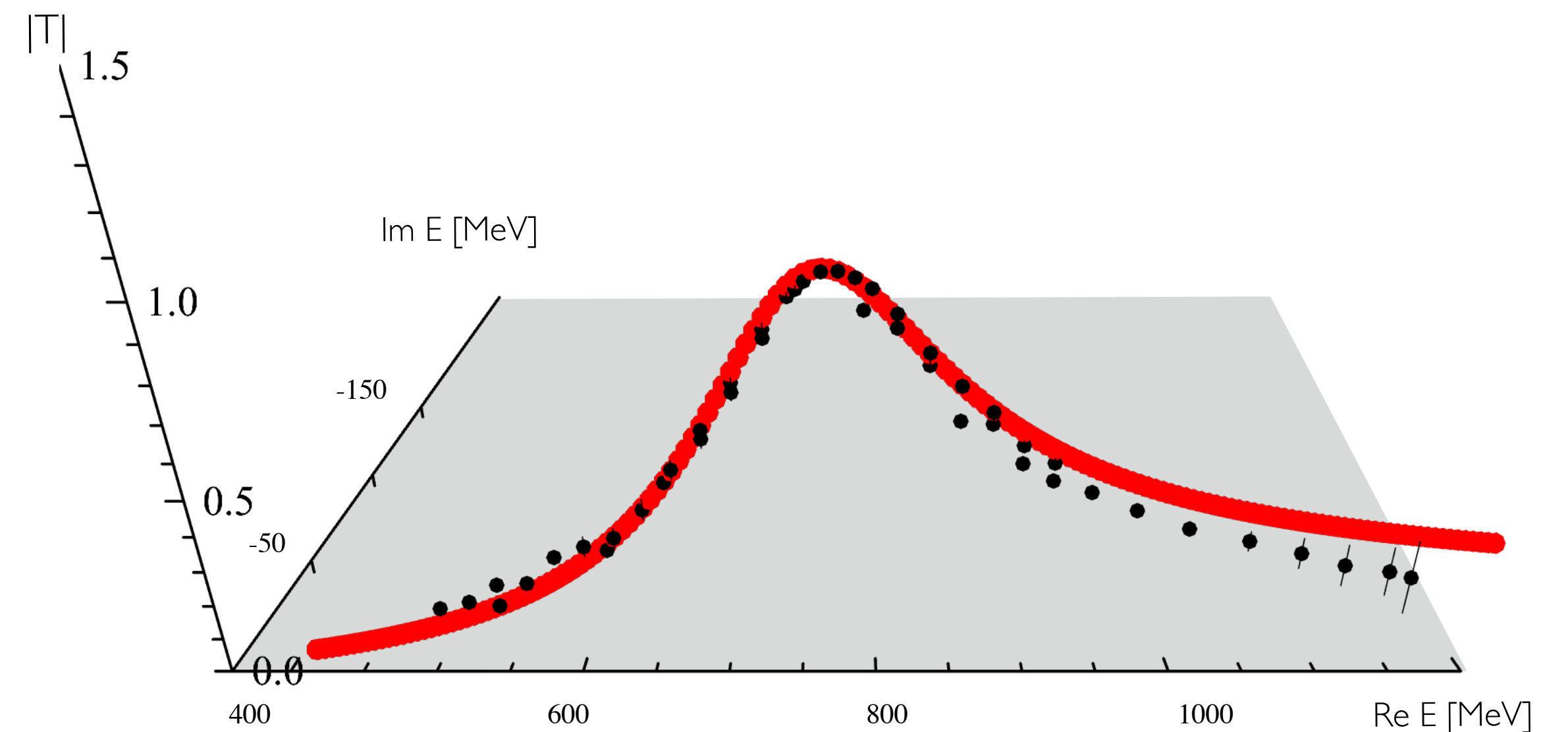
MM/Meißner/Urbach 2206.01477 under review in Phys. Rept.



# HADRON SPECTRUM

- physical information (  $\mathbf{E} \in \mathbb{R}$  )
  - > theory -- Lattice QCD (review<sup>1</sup>)
  - > experiment

$$\rho \rightarrow \pi\pi$$

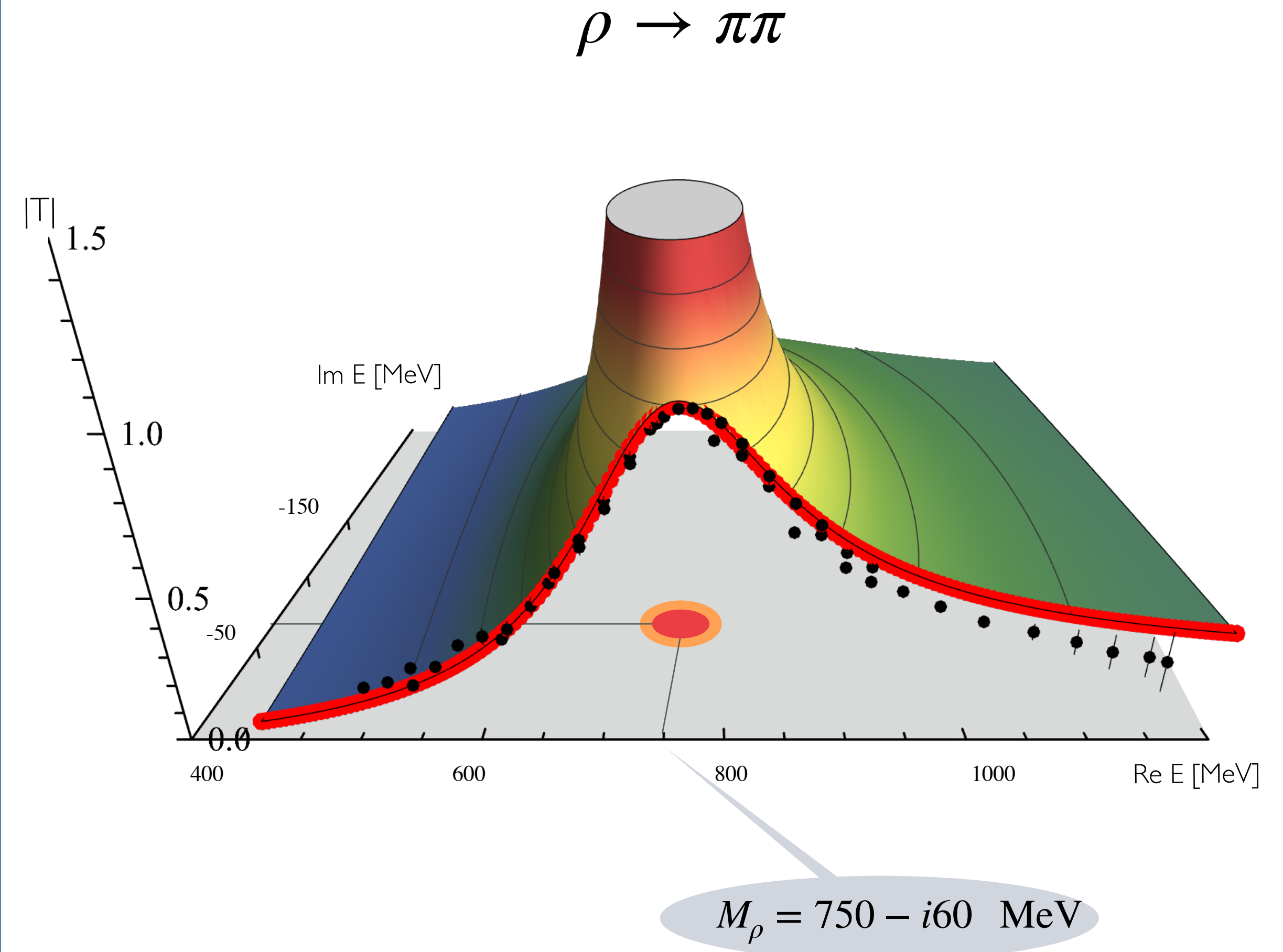


1) MM/Meißner/Urbach 2206.01477 under review in Phys. Rept.

Data: Estabrooks et al. NPB 79 (1974); Protopopescu et al. PRD 7 (1973);

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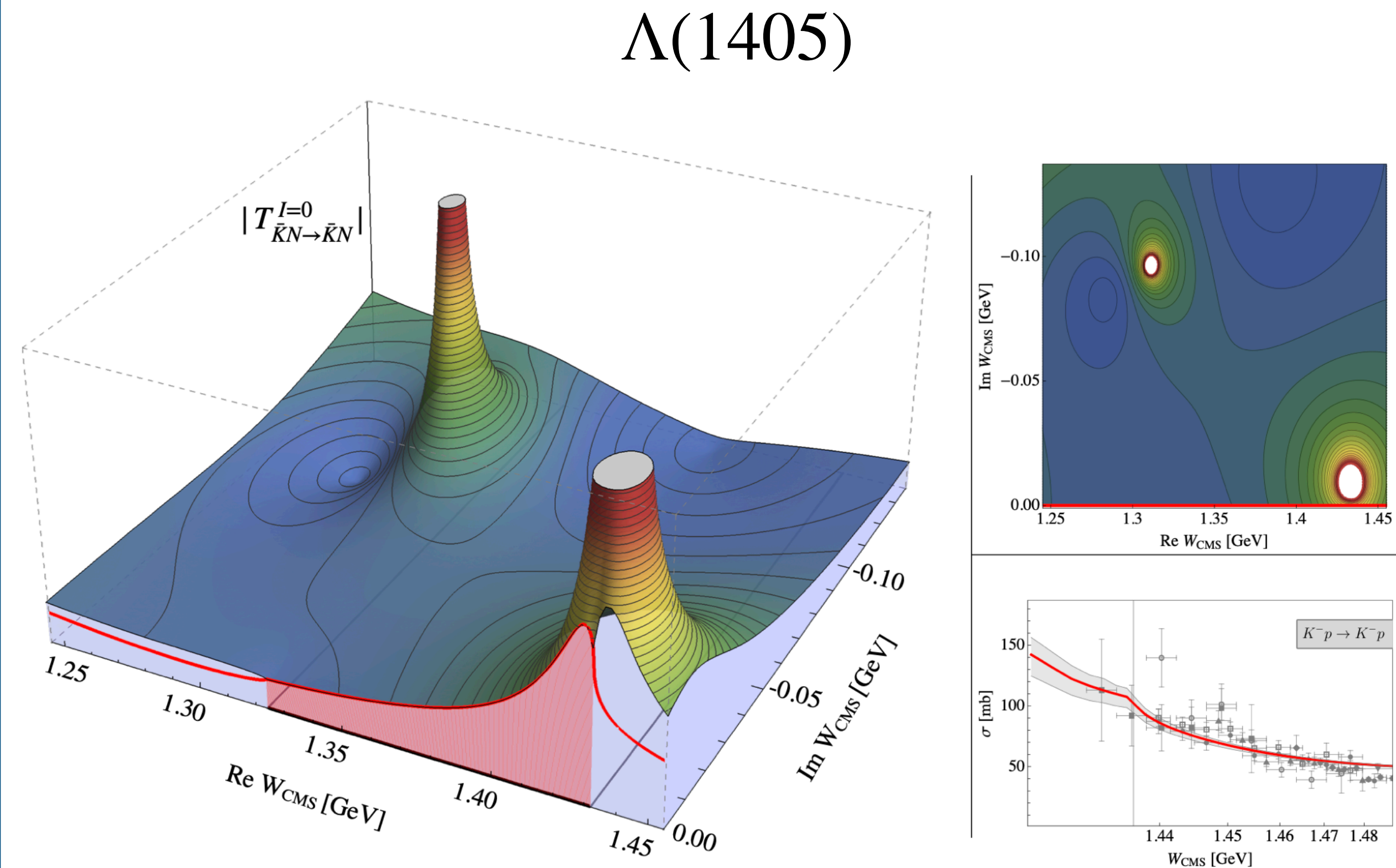


1) MM/Meißner/Urbach 2206.01477 under review in Phys. Rept.

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  - > theory -- Lattice QCD (review<sup>1</sup>)
  - > experiment



1) MM/Meißner/Urbach 2206.01477 under review in Phys. Rept.

MM Eur.Phys.J.ST 230 (2021)

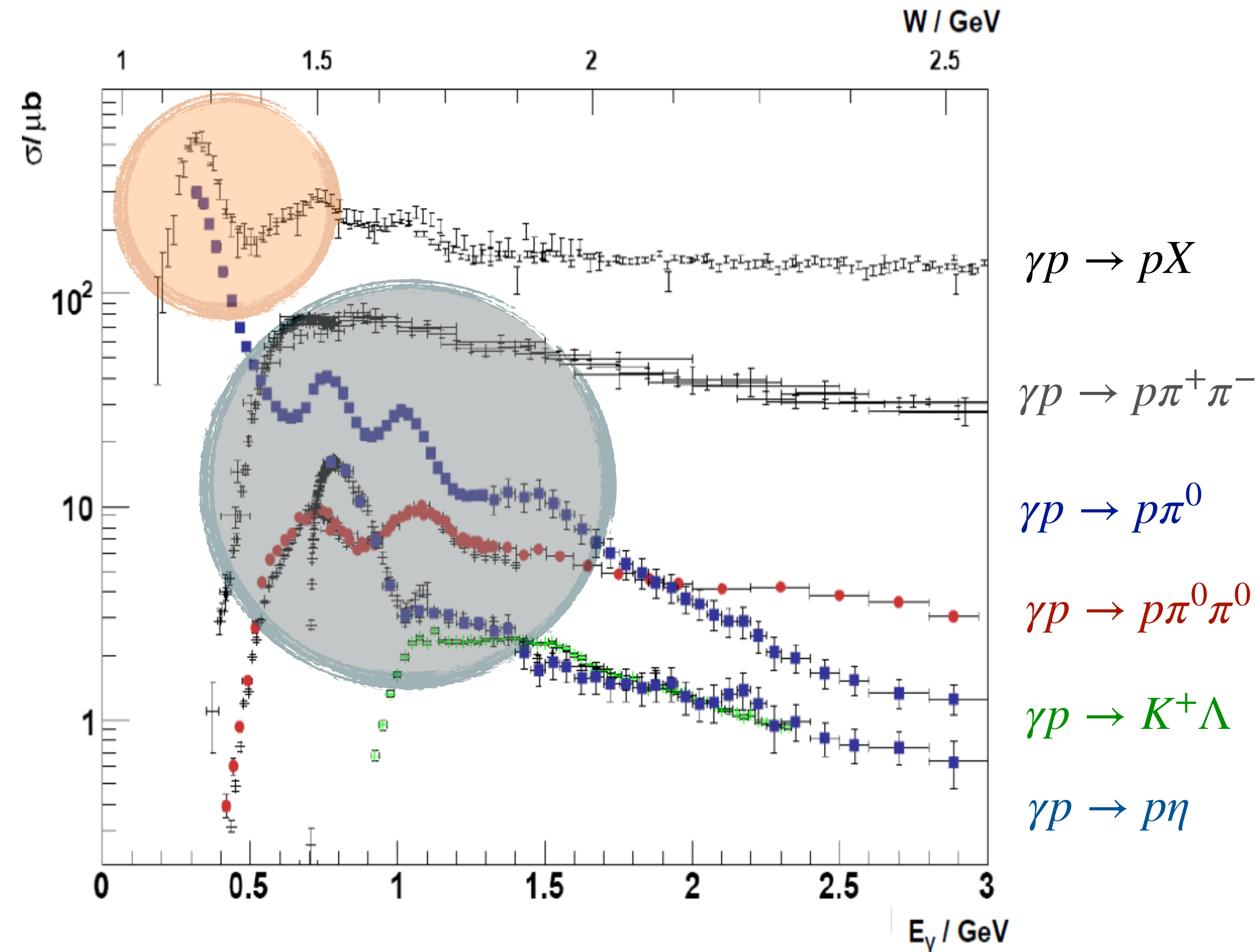
# HADRON SPECTRUM



Photon-induced excitation

via meson photo-/electroproduction

- > large amount of data ( $10^5$  for  $\gamma p \rightarrow \pi N$ )
- > bumps are **not** necessarily resonances
- > many more data to emerge at JLab<sup>1</sup> ( $Q^2=5-12 \text{ GeV}^2$ )



1) Carman, Joo, Mokeev, Few Body Syst. 61, 29 (2020) ... ;  
[CLAS] Phys.Rev.C 105 (2022) 065201; ...

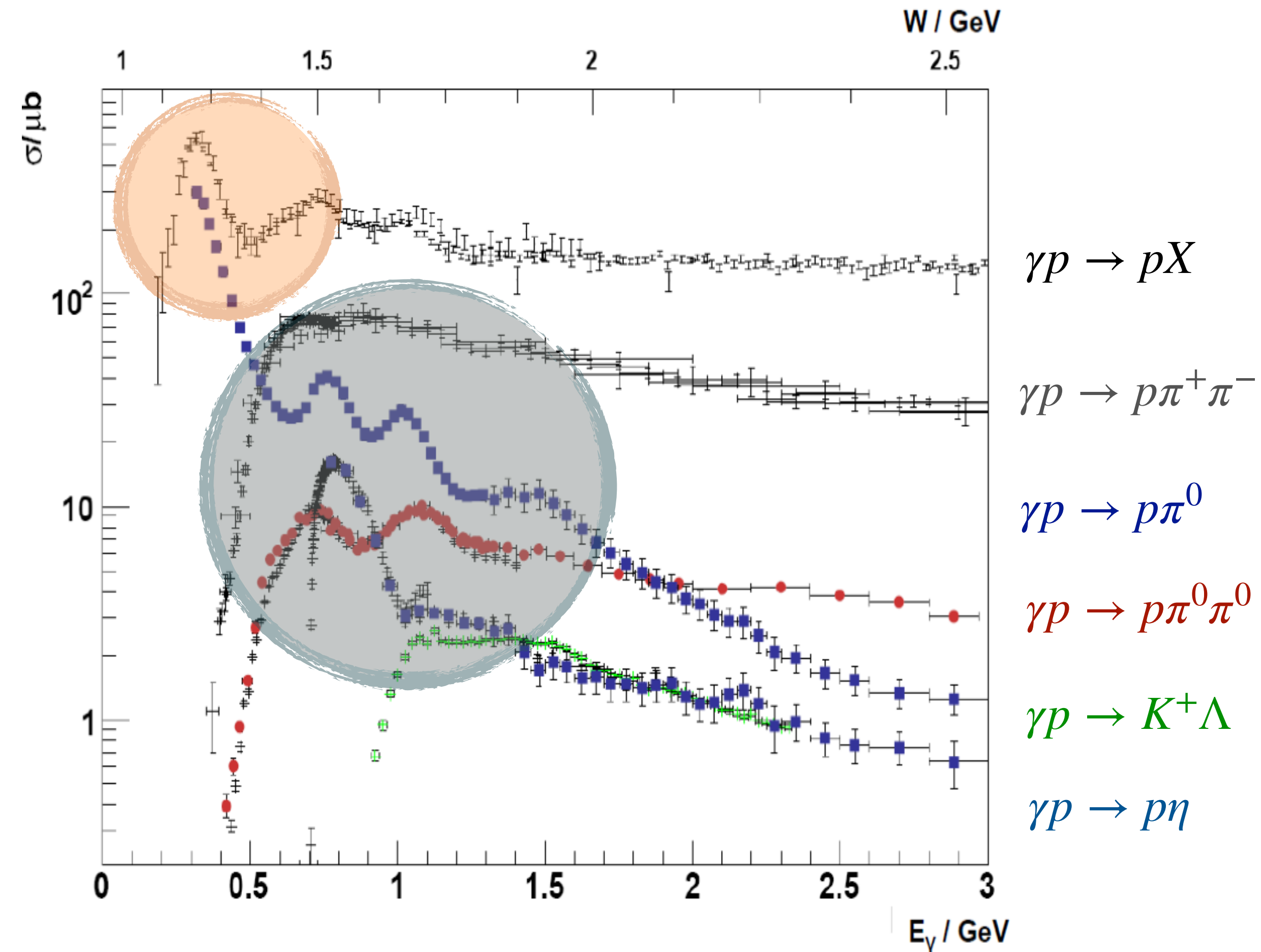
Data: Jefferson Laboratory, ELSA, MAMI

# HADRON SPECTRUM

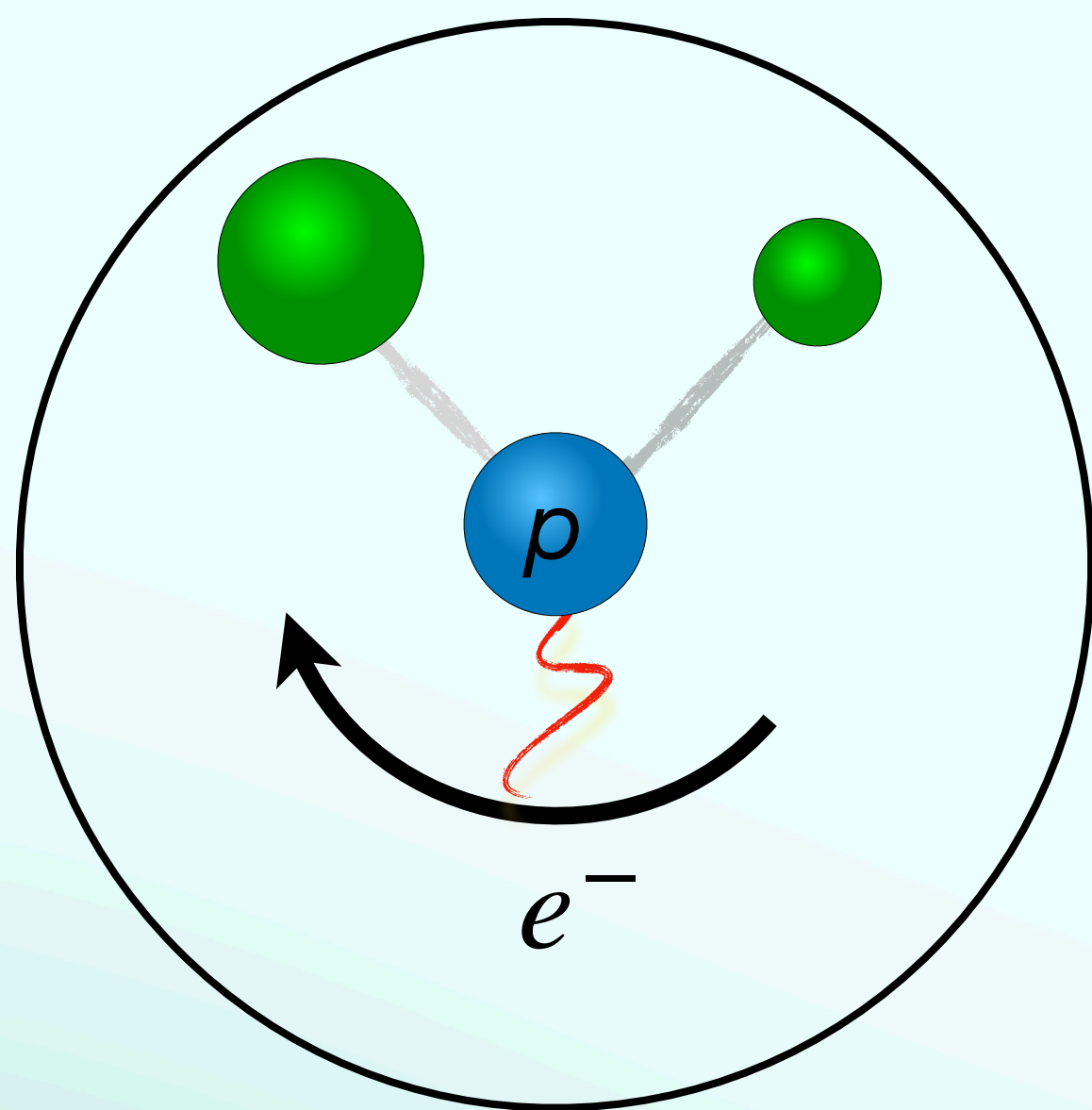


## Key questions:

- > can we describe the data consistently with the scattering data?
- > can we extract universal information about the hadron spectrum?



Data: Jefferson Laboratory, ELSA, MAMI



# THEORY

[JBW] MM, M.Döring, C.Granados, H.Haberzettl, J.Hergenrather,  
U.Meißner, D.Rönchen, I.Strakovsky, R.Workman

Phys.Rev.C 103 (2021) 6, 065204



# EXISTING APPROACHES



- ANL-Osaka<sup>1</sup>
- (eta)(kaon)MAID<sup>2</sup>
- SAID<sup>3</sup> [Ron's talk]
- ...<sup>4</sup>

## Some highlights

- > Simultaneous description of pion photo- and electroproduction (MAID)
- > Low-energy constraints from CHPT (chiral MAID)
- > Roper form factor from single and double pion electroproduction<sup>5</sup>

1) ANL-Osaka PRC 80(2009), Few-Body Syst. 59(2018),...

2) MAID2007, EPJA 34(2007) EtaMAID2018, EPJA 54(2018)

3) SAID, PIN Newsletter 16(2002)

4) Gent group PRC 89(2014),... Aznauryan et al., PRC 80(2009), IJMP(2013),...

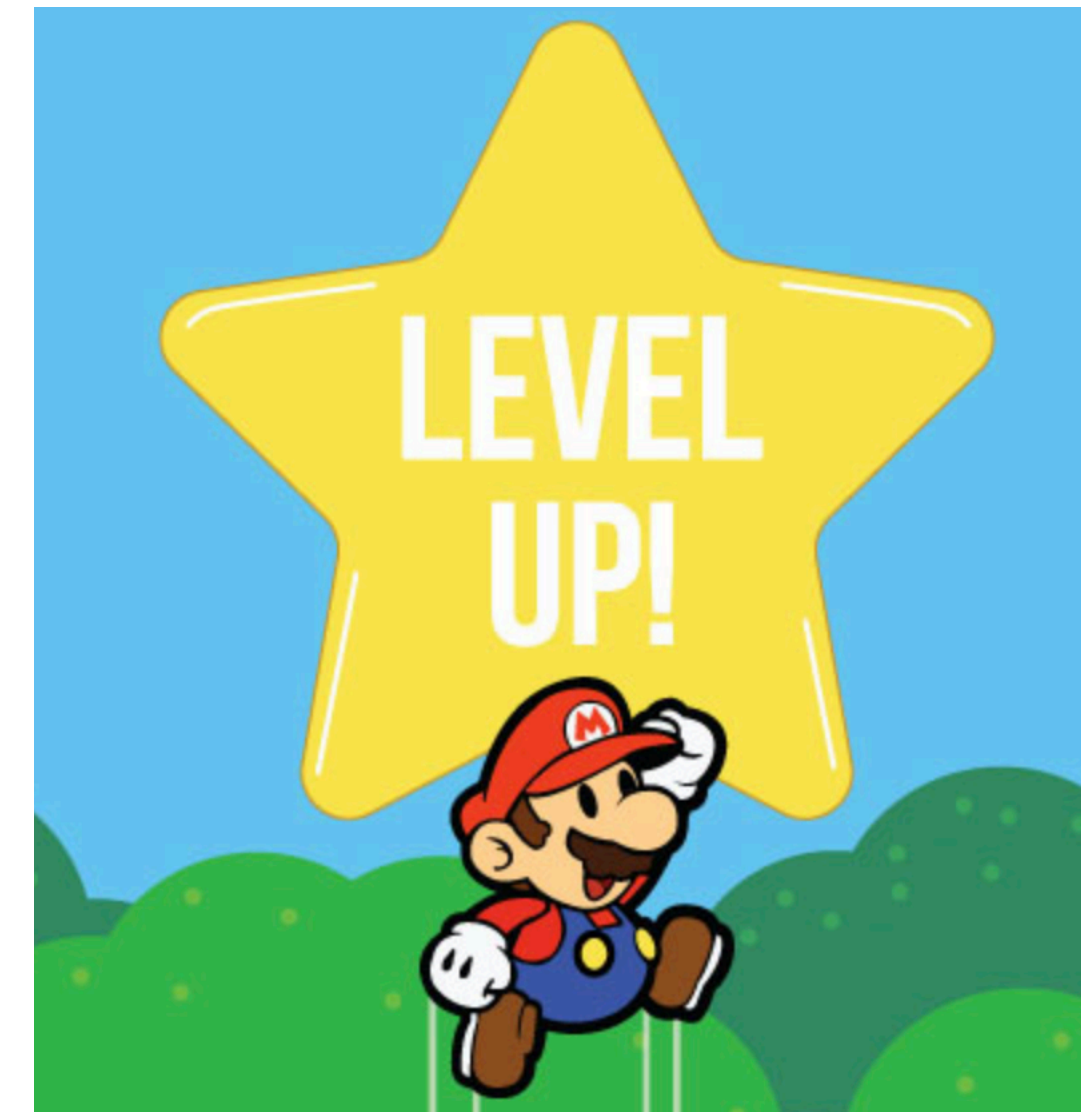
5) Burkert, Roberts, Rev.Mod.Phys. 91 (2019)

# EXISTING APPROACHES



## Level up the game

- coupled-channel approach. **Universality**  $\Leftrightarrow$  simultaneous description of  $\pi N$ ,  $\eta N$ ,  $K\Lambda$  channels
- threshold constraints, gauge invariance, ...
- constraints from scattering data



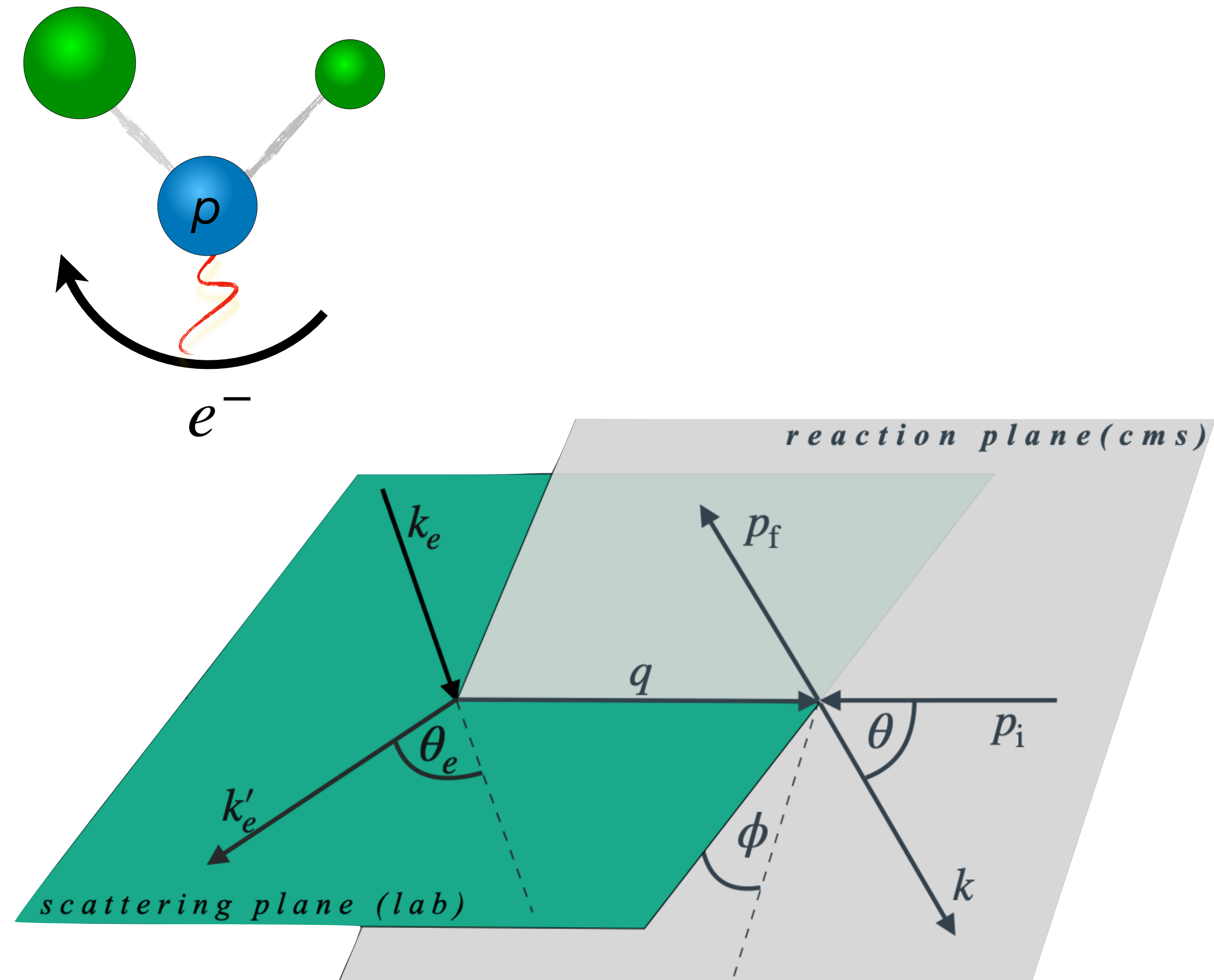


# KINEMATICS



$3 \cdot (2+3) - 10 =$  five independent variables

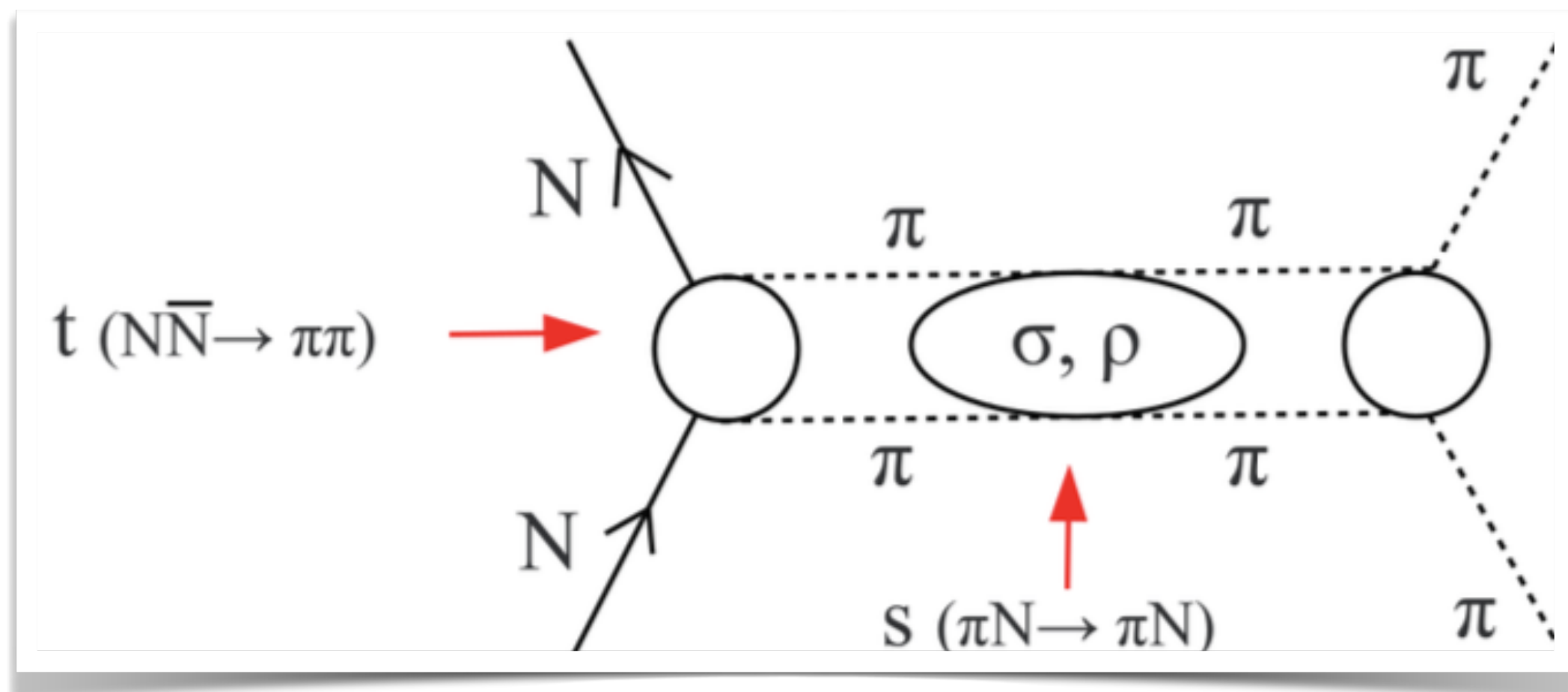
- total energy:  $W$
- photon virtuality:  $Q^2$
- transverse photon polarization:  
$$\epsilon = 1 + 2q_L^2 / Q^2 \tan^2 \theta_e / 2$$
- production angles:  $\theta, \varphi$



# GENERAL PRINCIPLES

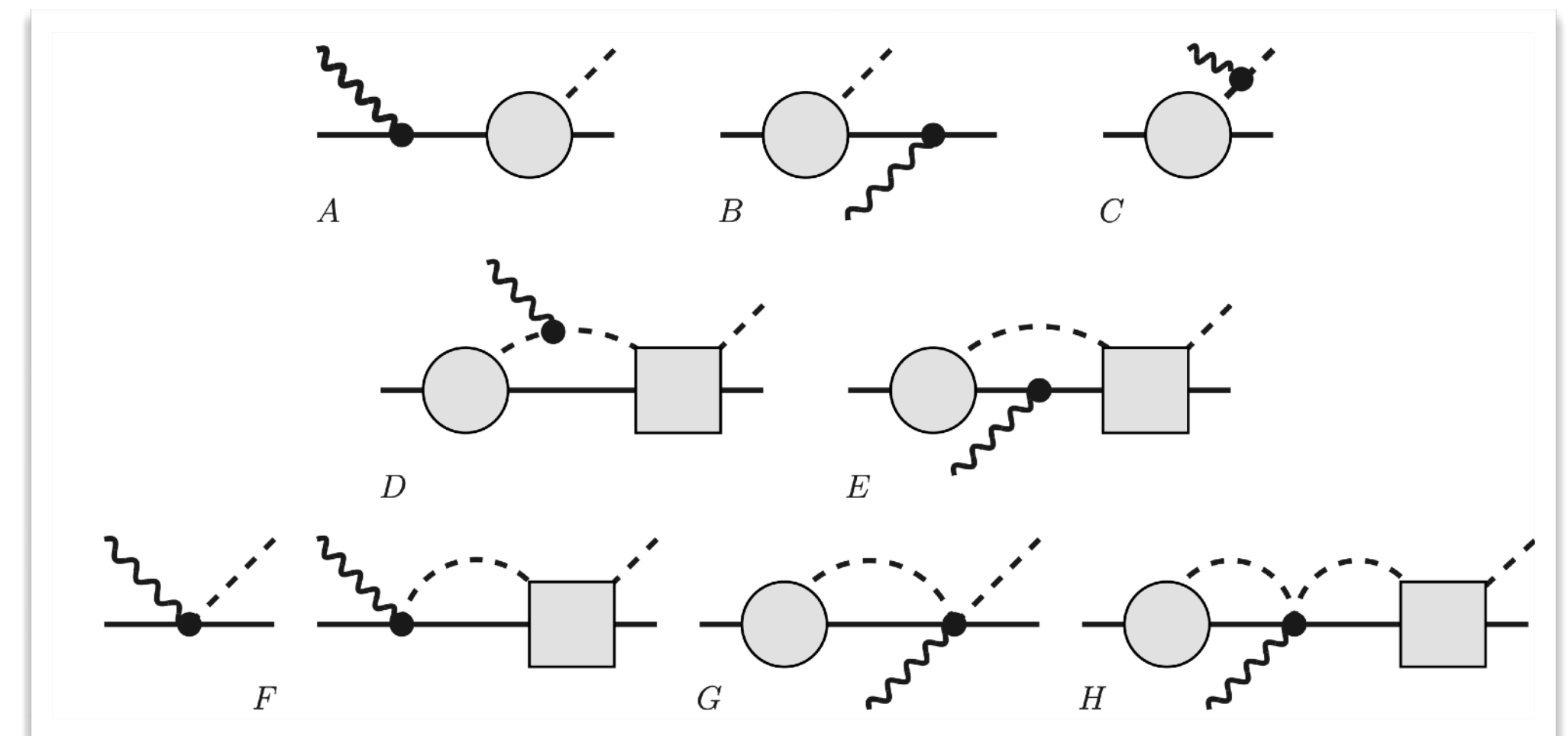
## Pion-induced reactions

- Unitarity/Analyticity/Crossing symmetry
- Underlying objects: scattering amplitudes



## Photon-induced reactions

- Final state unitarity/Gauge invariance<sup>1</sup>
- Underlying objects: transition matrix element



Afnan et al.(1995) Kvinikhidze et al.(1999) Haberzettl(19xx-2021)  
Borasoy et al.(2007) Ruic et al.(2011) MM et al.(2012)



# MULTIPOLES



Observable (e.g. cross section)

$$\frac{d\sigma^{\nu}}{d\Omega}(W, Q^2, \epsilon, \theta, \phi) = \sigma_T + \epsilon\sigma_L + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT}\cos\phi + \dots$$



# MULTIPOLES



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$$\frac{d\sigma^{\nu}}{d\Omega}(W, Q^2, \epsilon, \theta, \phi) = \sigma_T + \epsilon\sigma_L + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT}\cos\phi + \dots$$

Structure functions

$$\sigma_T(W, Q^2, \theta) = k/q_{\gamma} \left( |H_1|^2 + |H_2|^2 + |H_3|^2 + |H_4|^2 \right) / 2, \dots$$



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$$\frac{d\sigma^{\nu}}{d\Omega}(W, Q^2, \epsilon, \theta, \phi) = \sigma_T + \epsilon\sigma_L + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT}\cos\phi + \dots$$

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Helicity amplitudes

$$H_1(W, Q^2, \theta) = \sin\theta \cos\theta / 2 (-\mathcal{F}_3 - \mathcal{F}_4) / \sqrt{2}, \dots$$



# MULTIPOLES



Observable (e.g. cross section)

$$\frac{d\sigma^v}{d\Omega}(W, Q^2, \epsilon, \theta, \phi) = \sigma_T + \epsilon\sigma_L + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT}\cos\phi + \dots$$

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CGLN amplitudes

$$\mathcal{F}_1(W, Q^2, \theta) = \sum_{\ell>0} \ell M_{\ell+}(W, Q^2) P'_{\ell+1}(\cos\theta) + \dots$$

# MULTIPOLES

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CGLN amplitudes

$$\mathcal{F}_1(W, Q^2, \theta) = \sum_{\ell>0} \ell M_{\ell+}(W, Q^2) P'_{\ell+1}(\cos\theta) + \dots$$

Multipoles

$$\{E_{\ell\pm}(W, Q^2), L_{\ell\pm}(W, Q^2), M_{\ell\pm}(W, Q^2)\}$$



# MULTIPOLES



## Gauge invariance

- manifest implementation<sup>1</sup>
- include by design (this work)

Ward-Takahashi identity:

$$k_\mu T^\mu = 0$$
$$H_7 = \sum_{i=1}^6 a_i H_i$$
$$H_8 = \sum_{i=1}^6 b_i H_i$$

<sup>1</sup>) Afnan et al.(1995) Kvinikhidze et al.(1999) Haberzettl(19xx-2021)  
Borasoy et al.(2007) Ruic et al.(2011) MM et al.(2012)



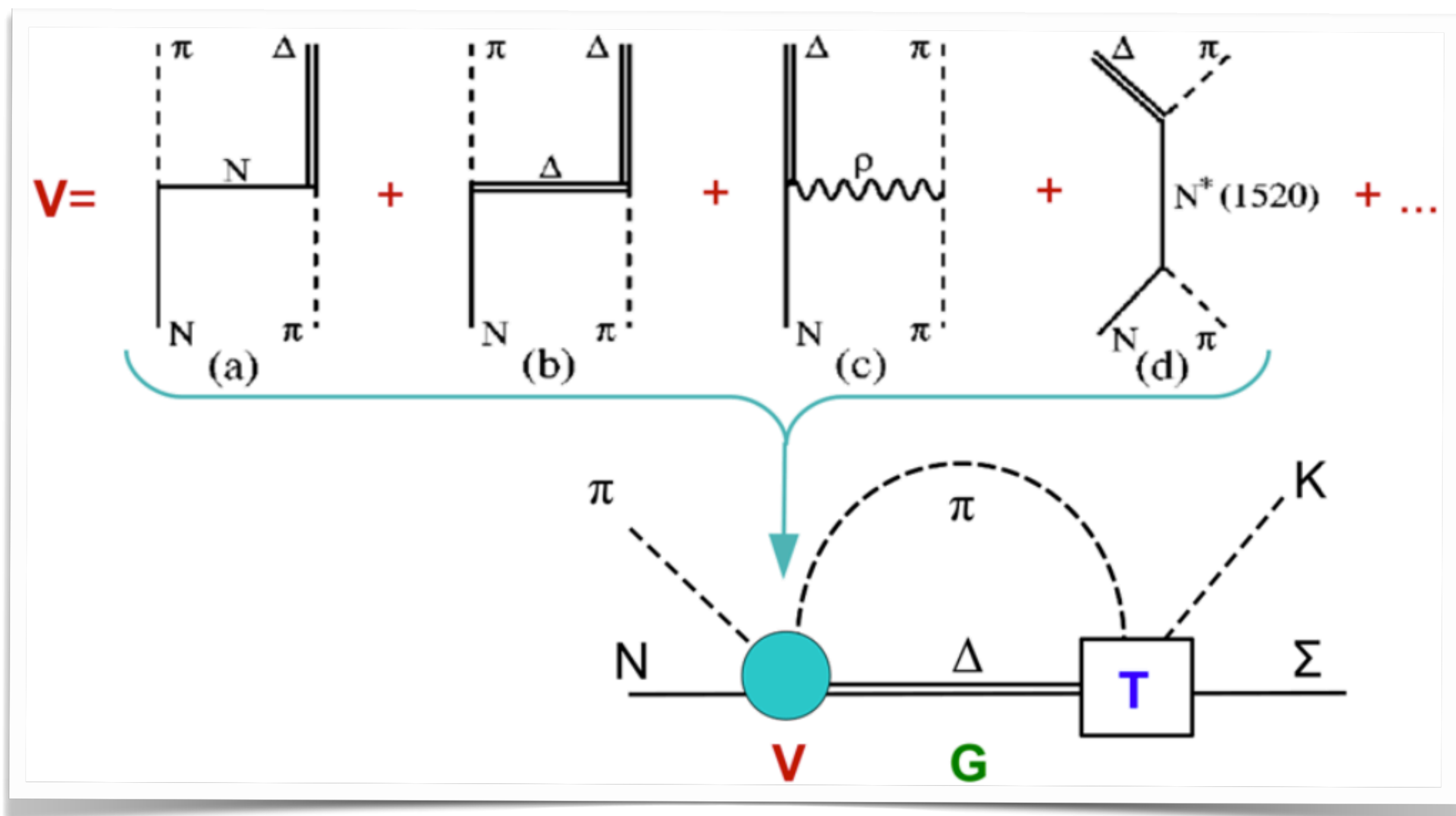
# MULTIPOLES



## Final-state unitarity and photoproduction limit

- start from Jülich-Bonn coupled-channel model<sup>1</sup>
  - > Potential  $V$  from an effective Lagrangian
  - >  $TP$  genuine resonance states in the s-channel diagrams
  - >  $TNP$  dynamically generated poles: t/u-channel

$$\langle L' S' p' | T_{\mu\nu}^{IJ} | L S p \rangle = \langle L' S' p' | V_{\mu\nu}^{IJ} | L S p \rangle + \sum_{\gamma, L'' S''} \int_0^\infty dq \, q^2 / E \langle L' S' p' | V_{\mu\gamma}^{IJ} | L'' S'' q \rangle \frac{1}{E - E_\gamma(q) + i\epsilon} \langle L'' S'' q | T_{\gamma\nu}^{IJ} | L S p \rangle$$



1) Rönchen et al., EPJA 49, 44 (2013)

# MULTIPOLES

$$\mathcal{M}_{\mu\gamma^*}(k, W, Q^2) = R_{\ell'}(\lambda, q/q_\gamma) \left( V_{\mu\gamma^*}(k, W, Q^2) + \sum_{\kappa} \int_0^{\infty} dp p^2 T_{\mu\kappa}(k, p, W) G_{\kappa}(p, W) V_{\kappa\gamma^*}(p, W, Q^2) \right)$$

For  $Q^2=0$  (real photons) identical to  
Jülich-Bonn photoproduction amplitude

$$V_{\mu\gamma^*}(k, W, Q^2) = V_{\mu\gamma}^{\text{JUBO}}(k, W) \cdot \tilde{F}_D(Q^2) \cdot e^{-\beta_\mu^0 Q^2/m_p^2} \left( 1 + Q^2/m_p^2 \beta_\mu^1 + (Q^2/m_p^2)^2 \beta_\mu^2 \right)$$

- 1) Siegert(1973) Amaldi et al.(1979) Tiator(2016)
- 2) Tiator et al.(2017)
- 3) Landay et al.(2017) (2019)

# MULTIPOLES

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Siegerts's theorem<sup>1</sup>  
...at pseudo-threshold:

$$V^{L_{\ell\pm}} = (\text{const.}) \cdot V^{E_{\ell\pm}}$$

- 1) Siegert(1973) Amaldi et al.(1979) Tiator(2016)
- 2) Tiator et al.(2017)
- 3) Landay et al.(2017) (2019)

# MULTIPOLES

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(Pseudo)-threshold behavior with meson/photon momenta

$$\begin{aligned} \lim_{k \rightarrow 0} E_{\ell+} &= k^{\ell} \\ \lim_{q \rightarrow 0} L_{\ell+} &= q^{\ell} \\ &\dots \end{aligned}$$

For  $Q^2=0$  (real photons) identical to Jülich-Bonn photoproduction amplitude

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Siegert's theorem<sup>1</sup>  
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- 1) Siegert(1973) Amaldi et al.(1979) Tiator(2016)
- 2) Tiator et al.(2017)
- 3) Landay et al.(2017) (2019)

# MULTIPOLES

$$\mathcal{M}_{\mu\gamma^*}(k, W, Q^2) = R_{\ell'}(\lambda, q/q_\gamma) \left( V_{\mu\gamma^*}(k, W, Q^2) + \sum_{\kappa} \int_0^{\infty} dp p^2 T_{\mu\kappa}(k, p, W) G_{\kappa}(p, W) V_{\kappa\gamma^*}(p, W, Q^2) \right)$$

(Pseudo)-threshold behavior with meson/photon momenta

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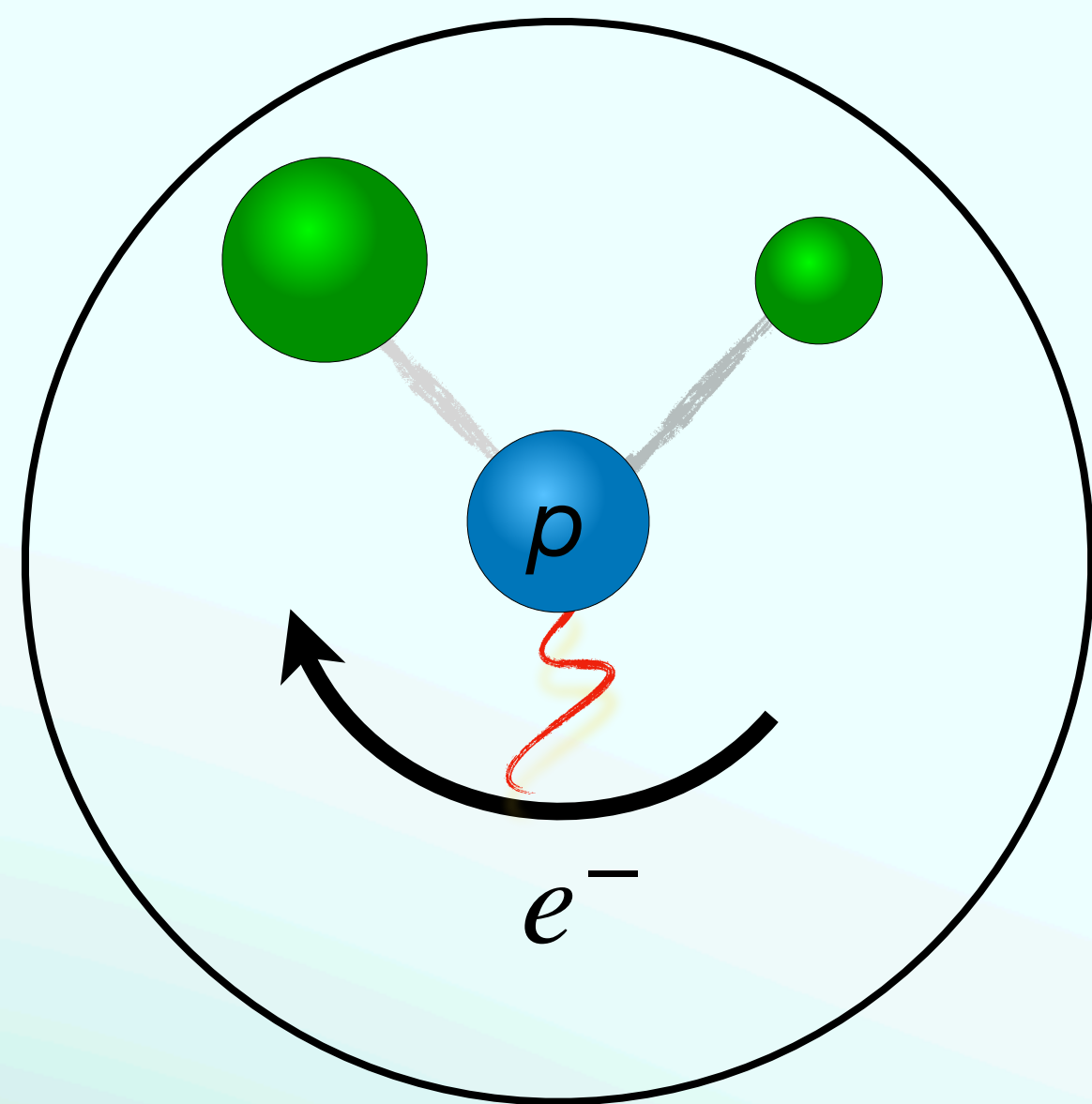
Siegert's theorem<sup>1</sup>  
...at pseudo-threshold:

$$V^{L_{\ell^\pm}} = (\text{const.}) \cdot V^{E_{\ell^\pm}}$$

## Parametrization dependence due to incomplete data

- > even for a truncated complete electroproduction experiment<sup>2</sup>
- > in future: Bias-variance tradeoff with statistical criteria<sup>3</sup>

1) Siegert(1973) Amaldi et al.(1979) Tiator(2016)  
2) Tiator et al.(2017)  
3) Landay et al.(2017) (2019)



# RESULTS

[JBW] MM, M.Döring, C.Granados, H.Haberzettl, J.Hergenrather, Ulf-G. Meißner, D.Rönchen, I.Strakovsky, R.Workman

Phys.Rev.C 103 (2021) 6, 065204  
Phys.Rev.C 106 (2022) 015201

INTERACTIVE WEB INTERFACE: <https://jbw.phys.gwu.edu>



# DEGREES OF FREEDOM

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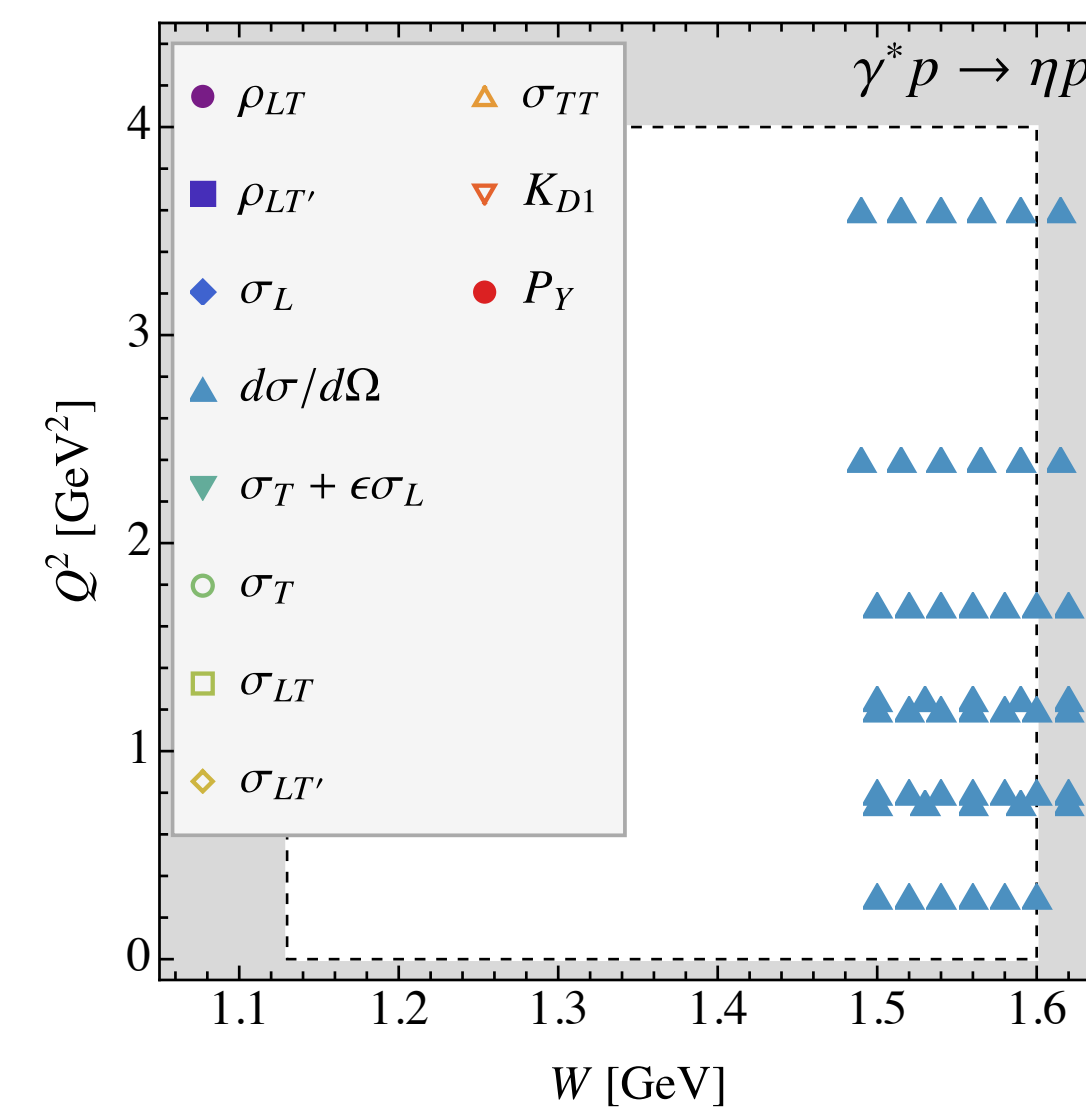
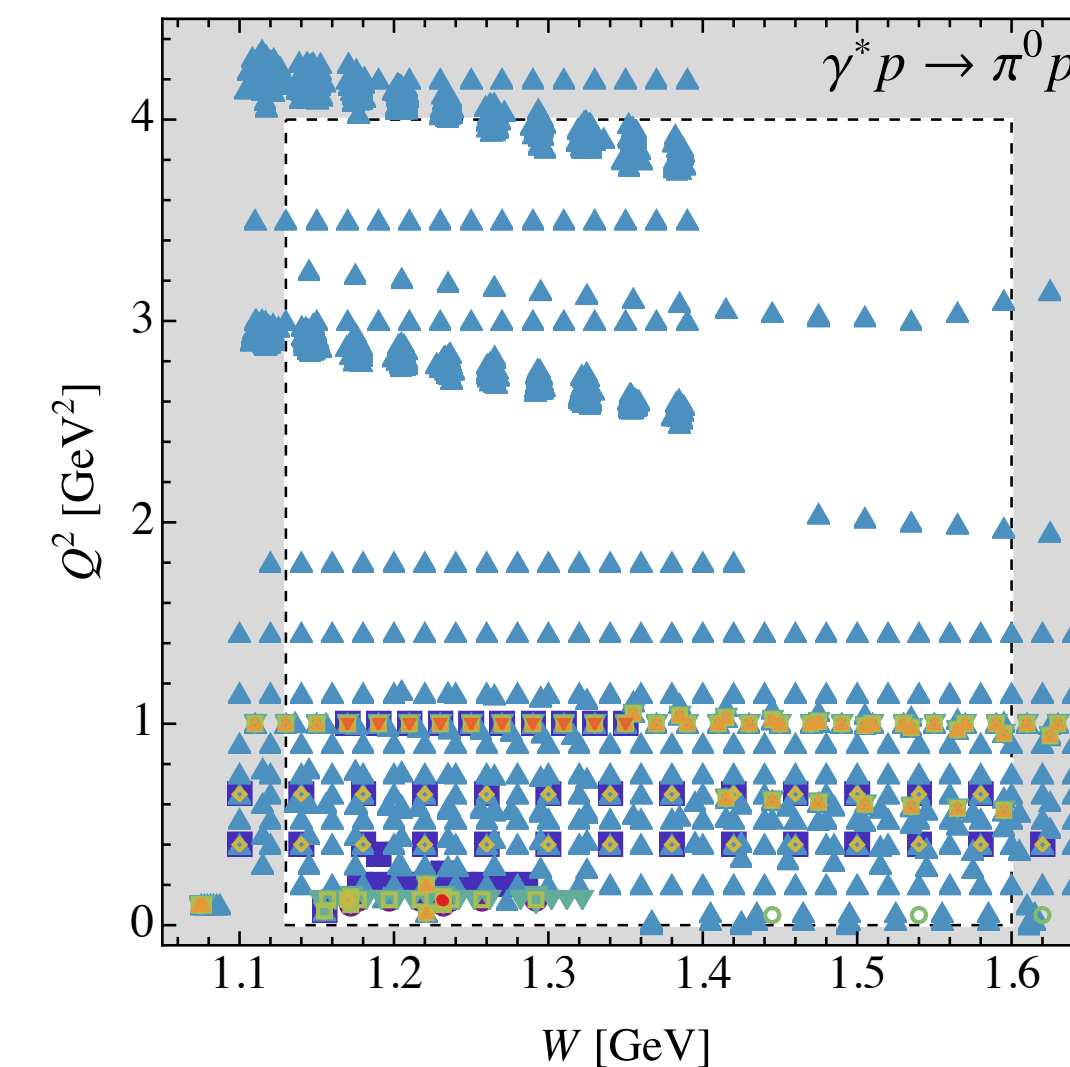
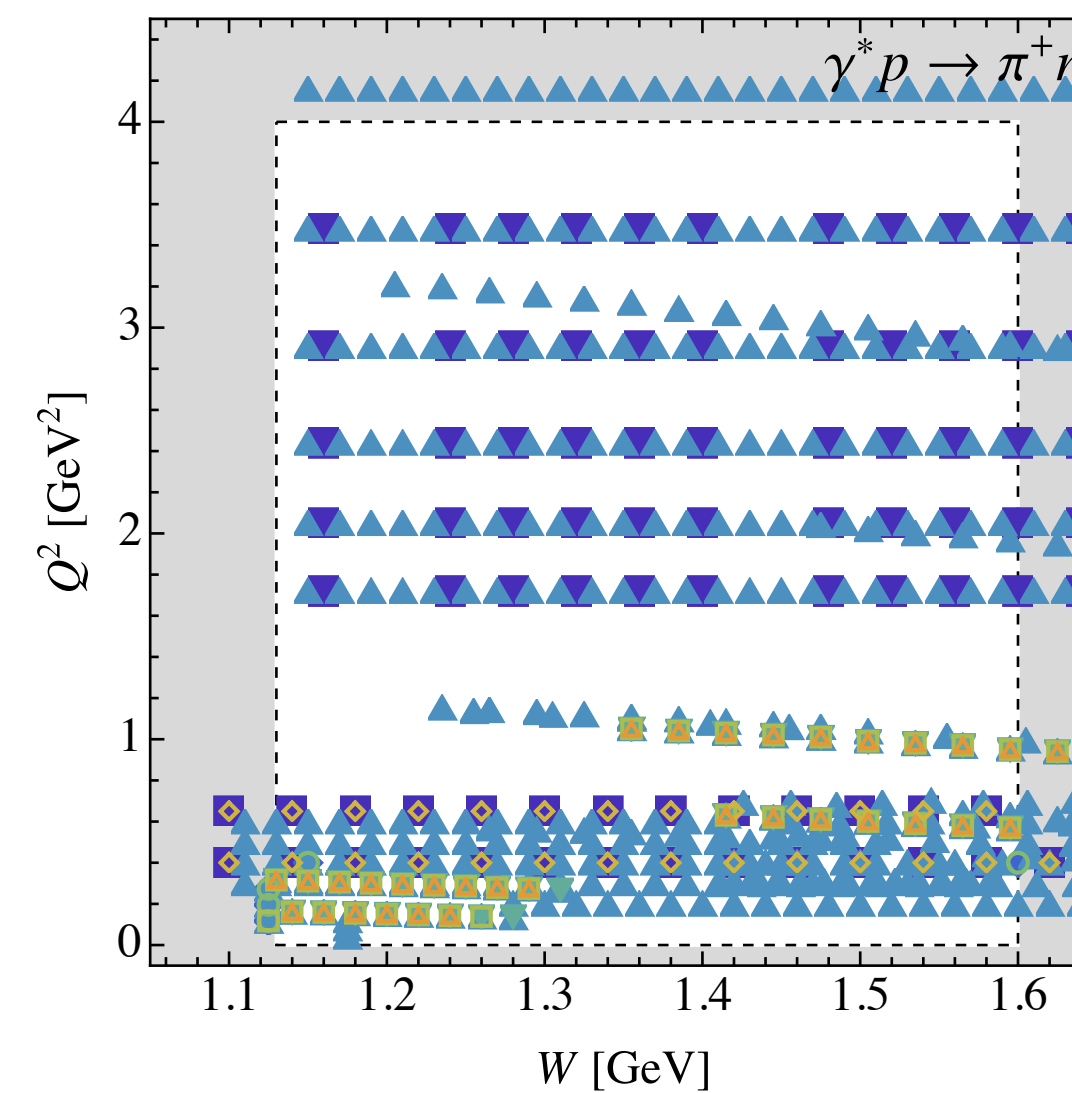
# DEGREES OF FREEDOM



Data ( $1.13 < W/\text{GeV} < 1.6$ ,  $Q^2 < 4 \text{ GeV}^2$ )

$45\text{k}(\pi^0 p) + 37\text{k}(\pi^+ n) + 2\text{k}(\eta p) = 84\text{k}$  data

11 observable types





# DEGREES OF FREEDOM



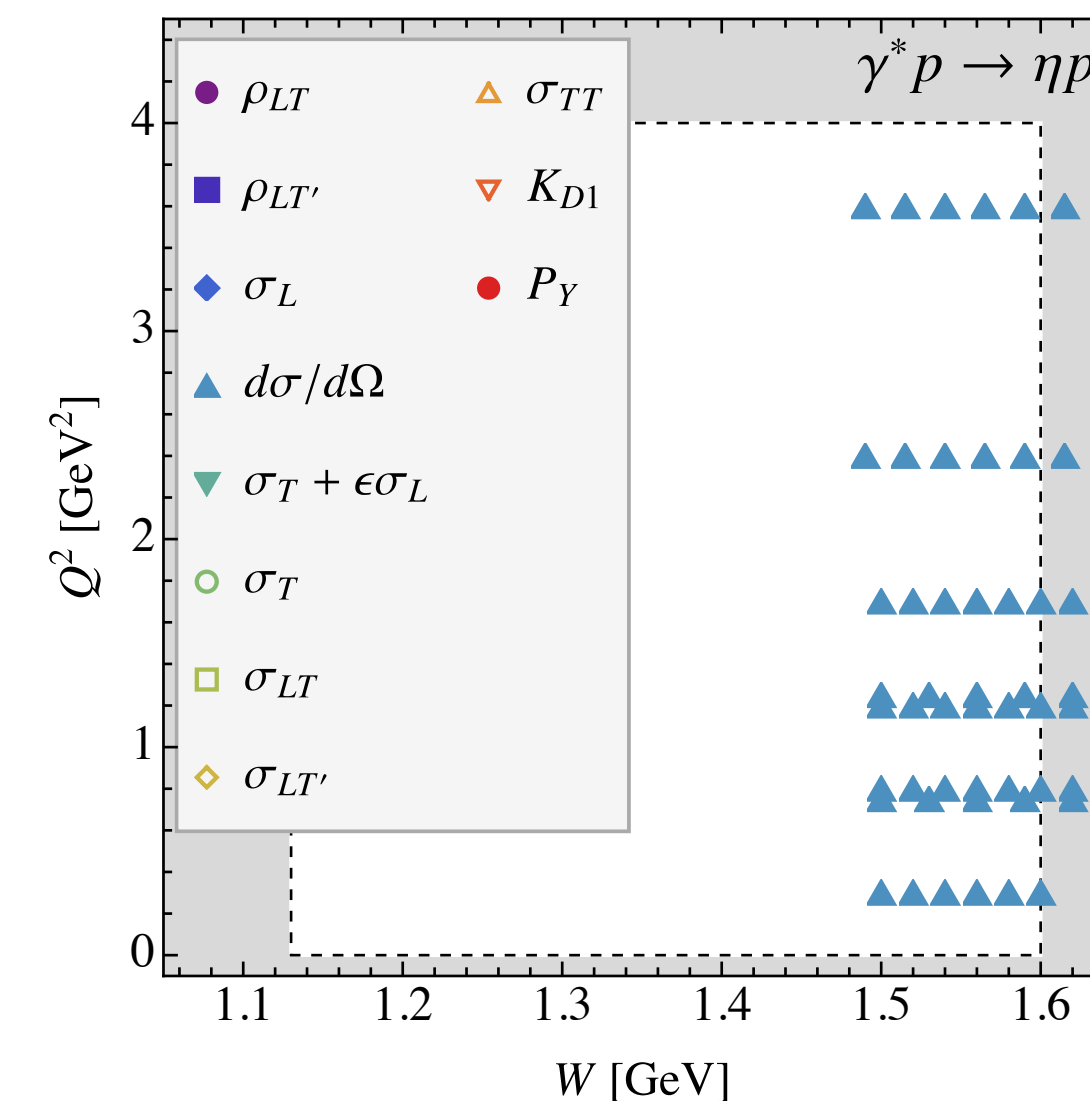
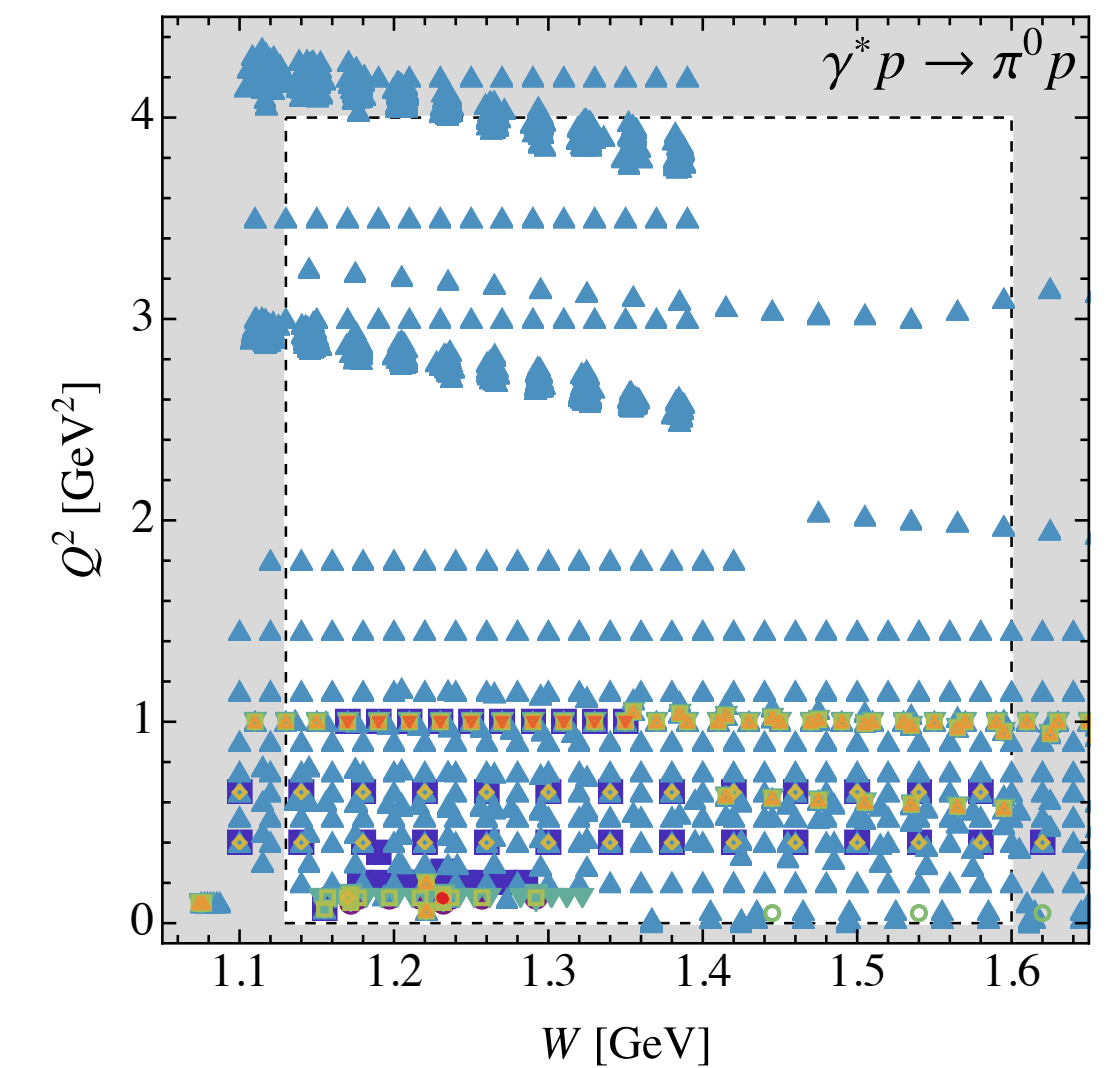
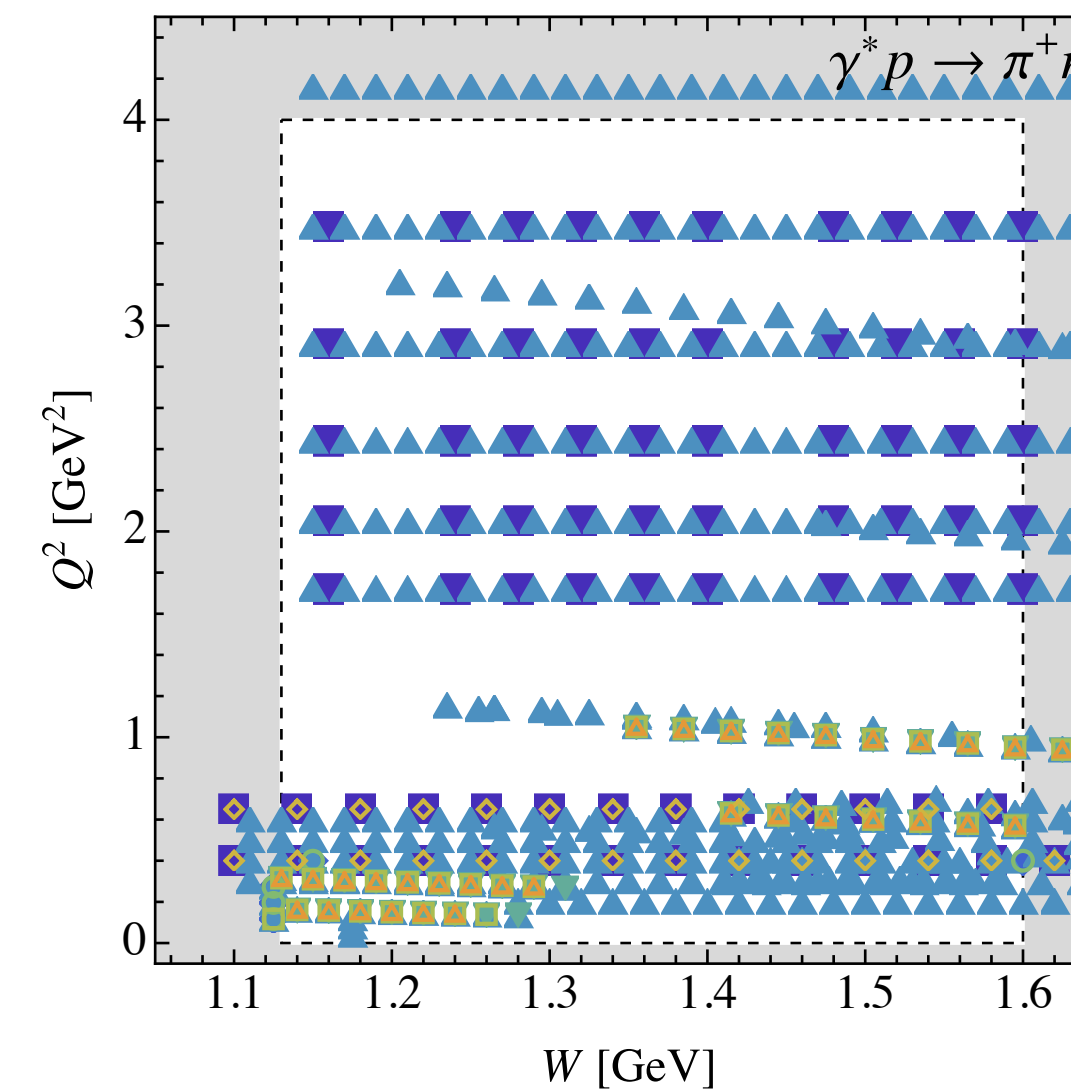
**Data ( $1.13 < W/\text{GeV} < 1.6$ ,  $Q^2 < 4 \text{ GeV}^2$ )**

$45\text{k}(\pi^0 p) + 37\text{k}(\pi^+ n) + 2\text{k}(\eta p) = 84\text{k data}$

11 observable types

**Parameters (S/P/D waves)**

26 multipoles \* (10..13 pars) = 257 pars



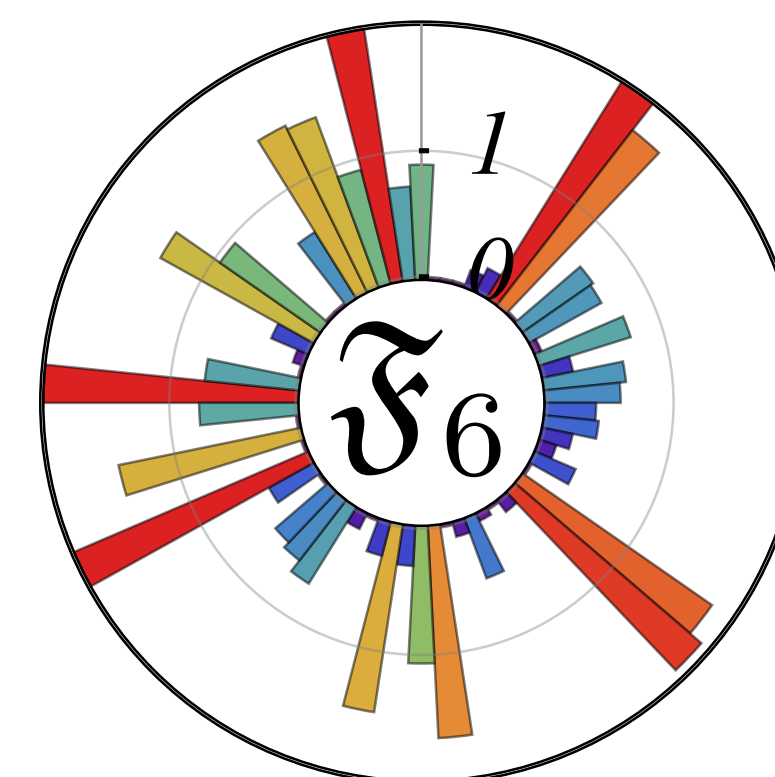
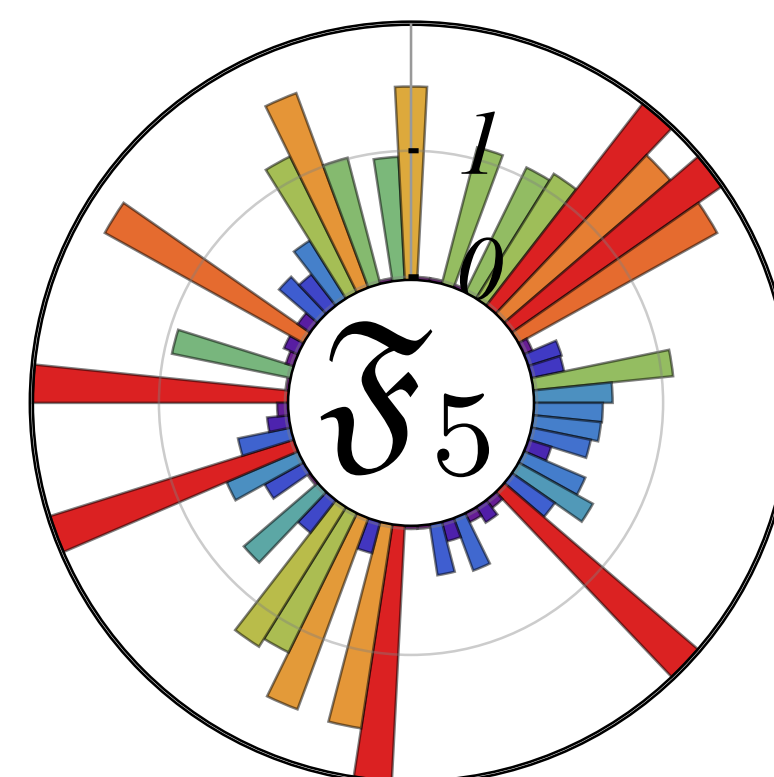
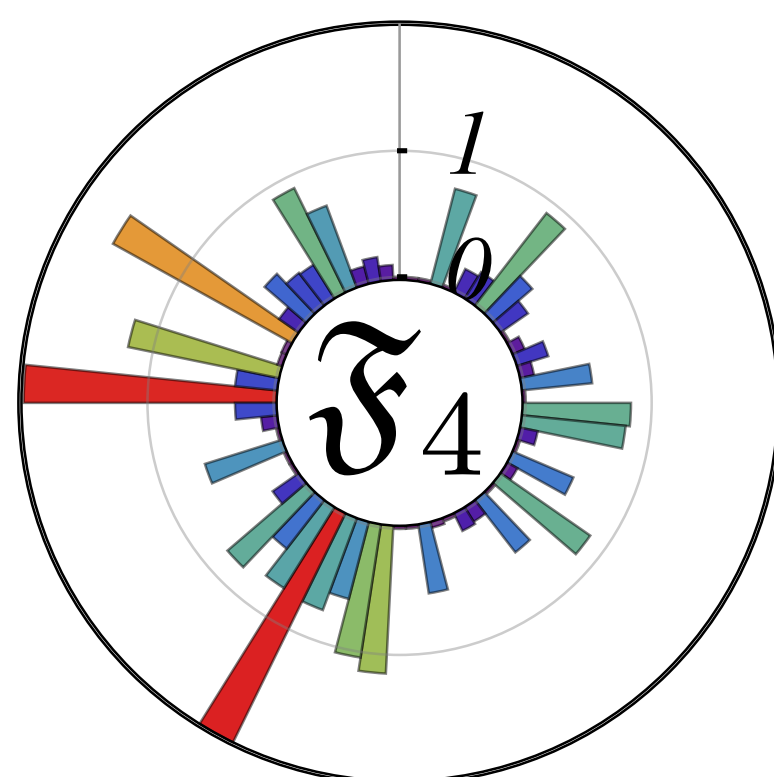
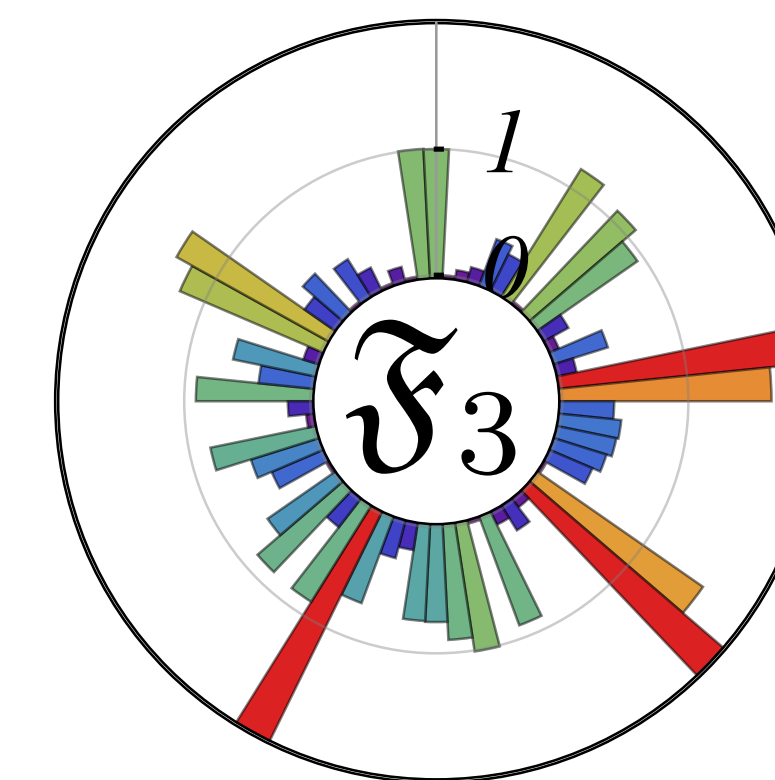
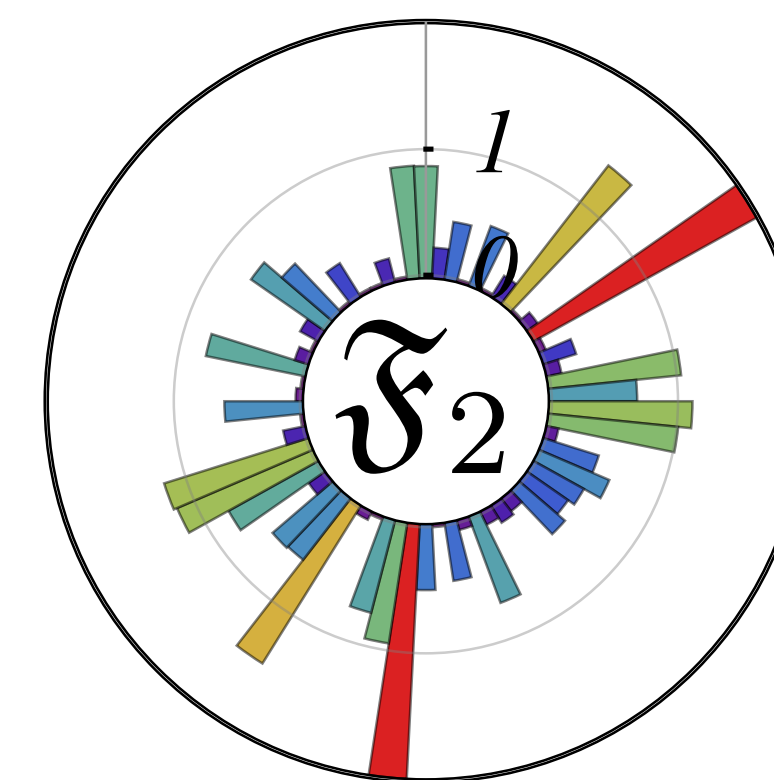
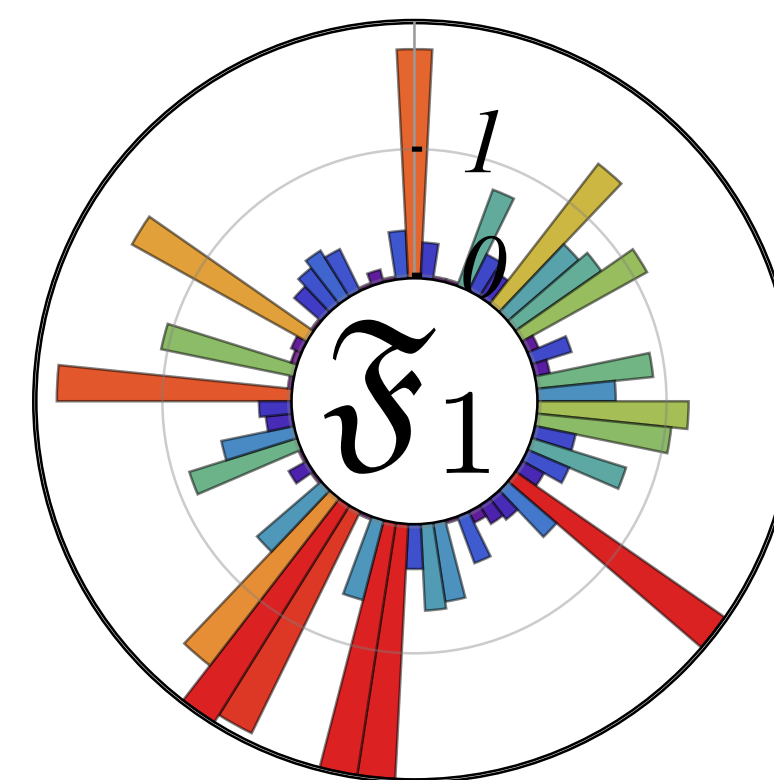


# SYSTEMATICS



**Many local minima:**

> different fit strategies (sequential, all-in fits)



# DEGREES OF FREEDOM

**piN data is dominant:**

> weighted or unweighted fits

$$\chi_{\text{reg}}^2 = \sum_{i=1}^{N_{\text{all}}} \left( \frac{\mathcal{O}_i^{\text{exp}} - \mathcal{O}_i}{\Delta_i^{\text{stat}} + \Delta_i^{\text{syst}}} \right)^2$$

$$\chi_{\text{wt}}^2 = \sum_{j \in \{\pi^0 p, \pi^+ n, \eta p\}} \frac{N_{\text{all}}}{3N_j} \sum_{i=1}^{N_j} \left( \frac{\mathcal{O}_{ji}^{\text{exp}} - \mathcal{O}_{ji}}{\Delta_{ji}^{\text{stat}} + \Delta_{ji}^{\text{syst}}} \right)^2$$

# RESULTS



## $\pi N$ data fits:

- > all strategies converge
- > different minima (systematic uncertainties)

Fit	$\sigma_L$		$d\sigma/d\Omega$		$\sigma_T + \epsilon\sigma_L$		$\sigma_T$		$\sigma_{LT}$		$\sigma_{LT'}$		$\sigma_{TT}$		$K_{D1}$		$P_Y$		$\rho_{LT}$		$\rho_{LT'}$		$\chi^2_{\text{dof}}$
	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	$\pi^0 p$	$\pi^+ n$	
$\mathfrak{F}_1$	-	9	65355	53229	870	418	87	88	1212	133	862	762	4400	251	4493	-	234	-	525	-	3300	10294	1.77
$\mathfrak{F}_2$	-	4	69472	55889	1081	619	65	78	1780	150	1225	822	4274	237	4518	-	325	-	590	-	3545	10629	1.69
$\mathfrak{F}_3$	-	8	66981	54979	568	388	84	95	1863	181	1201	437	3934	339	4296	-	686	-	687	-	3556	9377	1.81
$\mathfrak{F}_4$	-	22	63113	52616	562	378	153	107	1270	146	1198	1015	4385	218	5929	-	699	-	604	-	3548	11028	1.78
$\mathfrak{F}_5$	-	20	65724	53340	536	528	125	81	1507	219	1075	756	4134	230	5236	-	692	-	554	-	3580	11254	1.81
$\mathfrak{F}_6$	-	18	71982	58434	1075	501	29	68	1353	135	1600	1810	3935	291	5364	-	421	-	587	-	3932	11475	1.78

[JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201

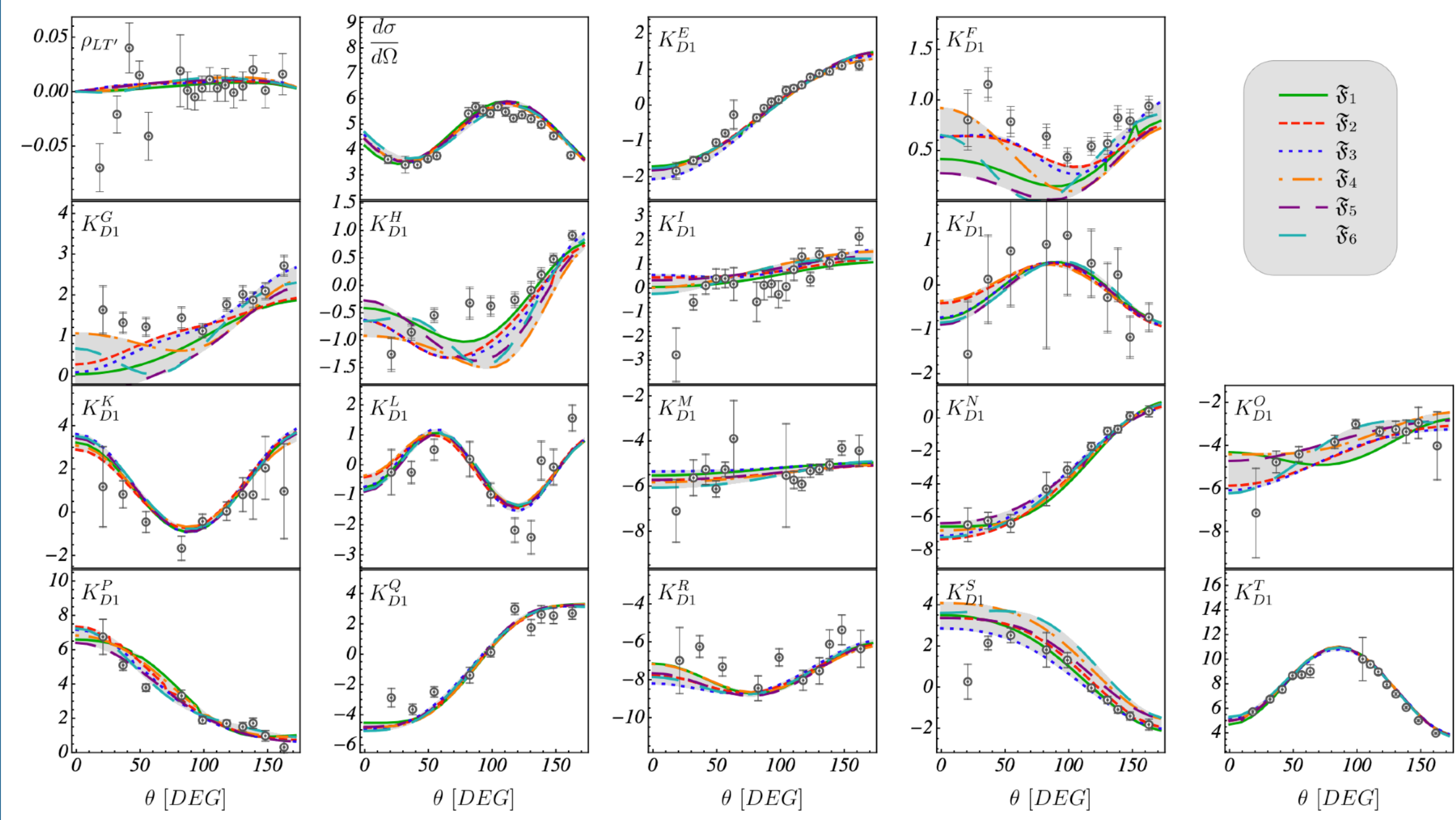
Data: Kelly et al.(2005)

# RESULTS



## $\pi N$ data fits<sup>1</sup>:

- > all strategies converge
- > different minima (systematic uncertainties)
- > Kelly data<sup>2</sup>



1) [JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201  
 2) Jefferson Lab Hall A Collaboration *Phys.Rev.Lett.* 95 (2005) 102001

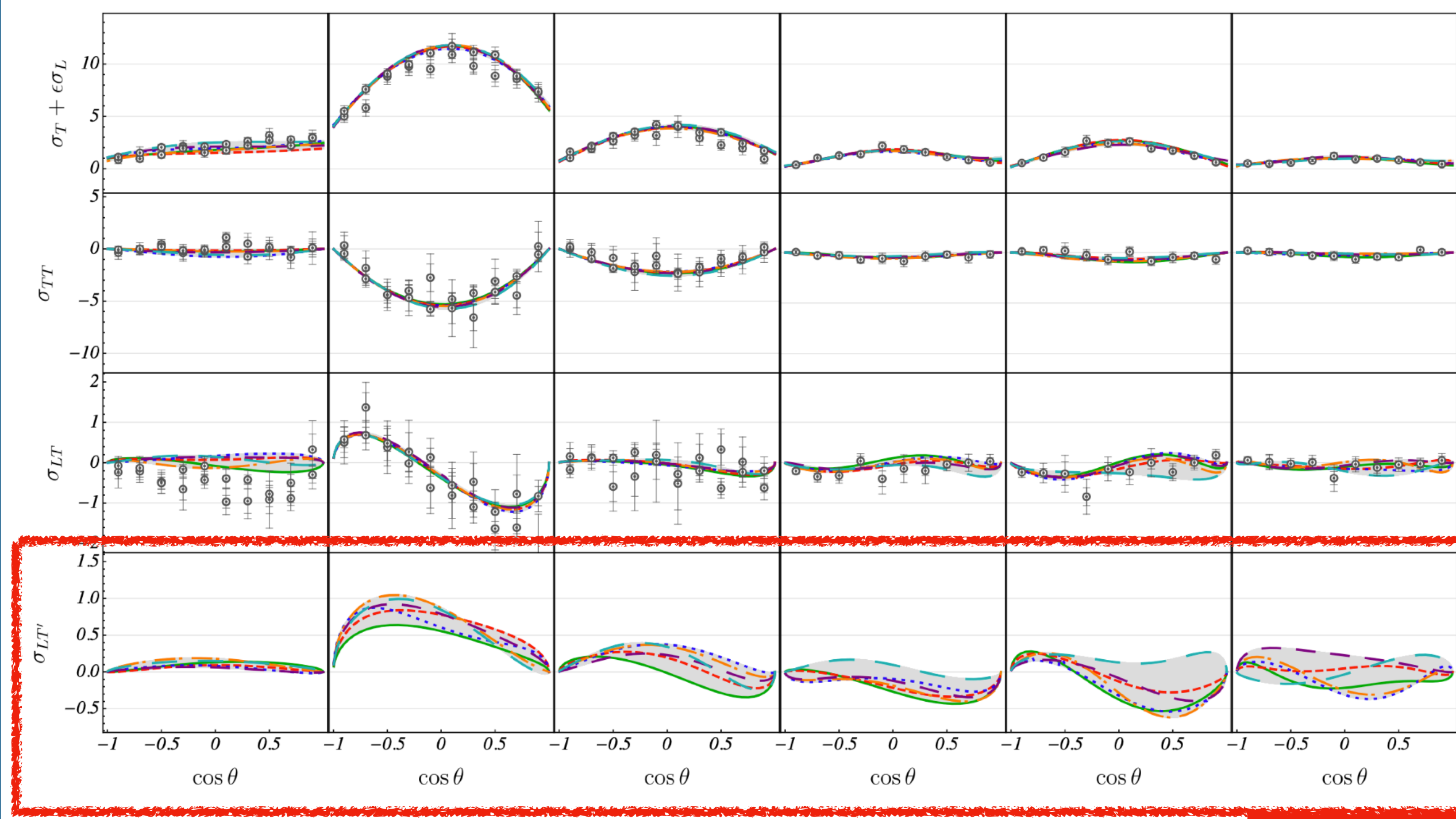


# RESULTS



## $\pi N$ data fits<sup>1</sup>:

- > all strategies converge
- > different minima (systematic uncertainties)
- > Joo data<sup>2</sup>



PREDICTION

1) [JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201  
 2) Joo et al. [CLAS] *PRC* (2003), *PRL* (2002)



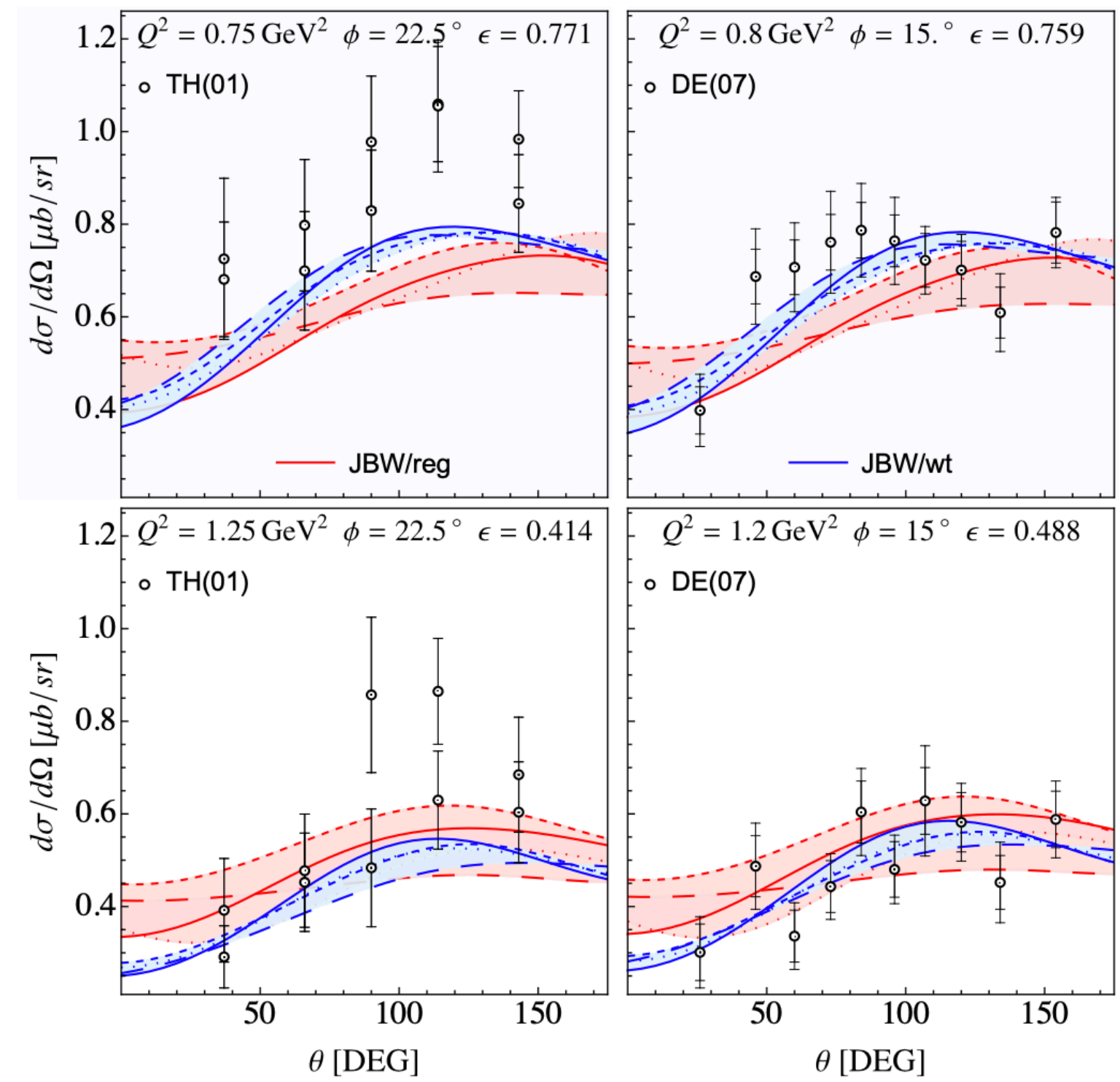
# RESULTS



	$\chi^2/\text{dof}$	$\chi^2_{\pi^0 p/\text{data}}$	$\chi^2_{\pi^+ n/\text{data}}$	$\chi^2_{\eta p/\text{data}}$
$\mathfrak{F}_1^{\text{reg}}$	1.66	1.68	1.61	1.77
$\mathfrak{F}_2^{\text{reg}}$	1.73	1.71	1.71	2.29
$\mathfrak{F}_3^{\text{reg}}$	1.69	1.69	1.66	1.89
$\mathfrak{F}_4^{\text{reg}}$	1.69	1.7	1.64	2.05
$\mathfrak{F}_1^{\text{wt}}$	1.54	1.74	1.63	1.25
$\mathfrak{F}_2^{\text{wt}}$	1.63	1.82	1.79	1.27

## $\eta N$ data fits<sup>1</sup>:

- > all strategies converge
- > different minima (systematic uncertainties)
- > many ambiguities in data<sup>2</sup>



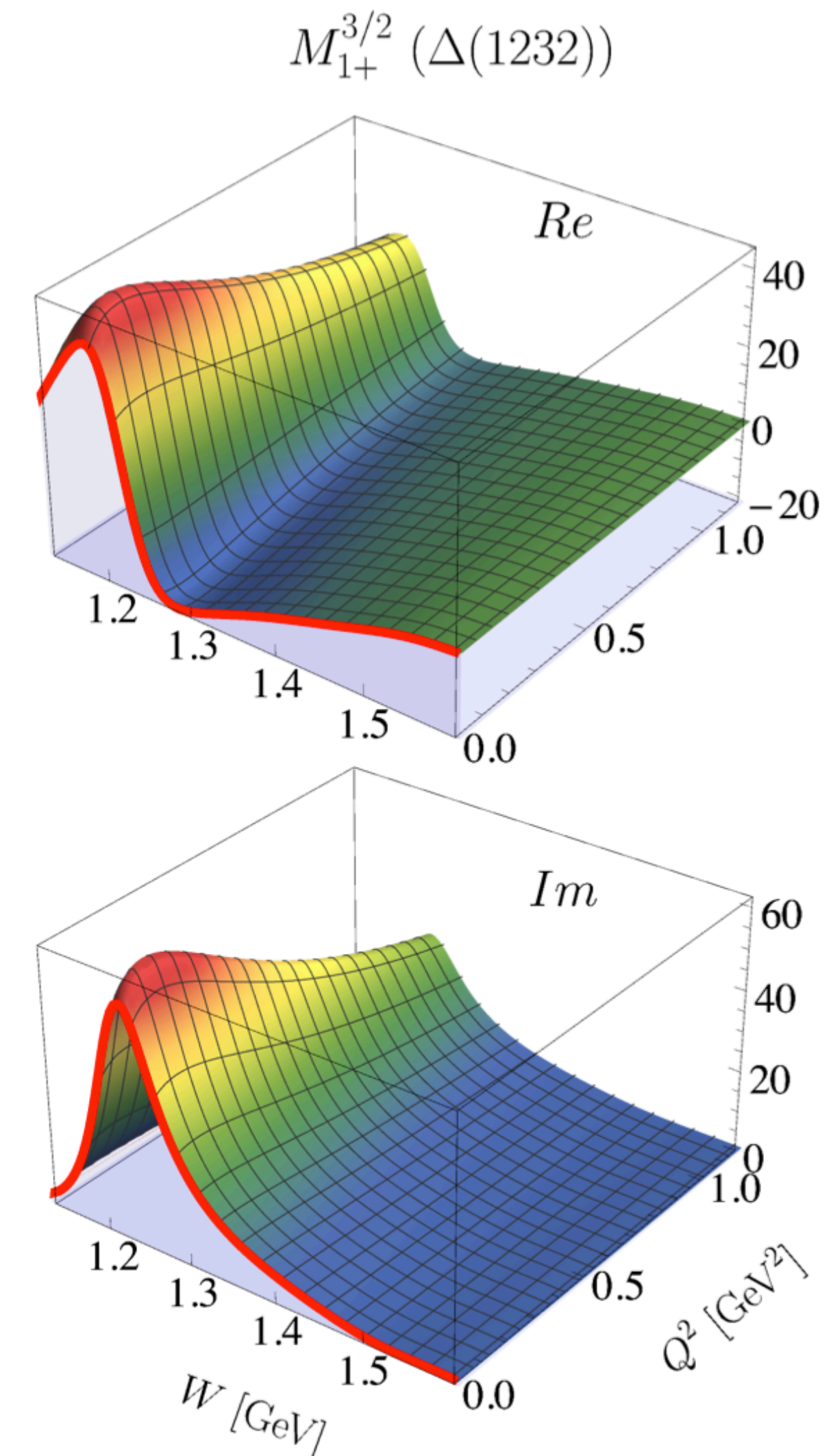
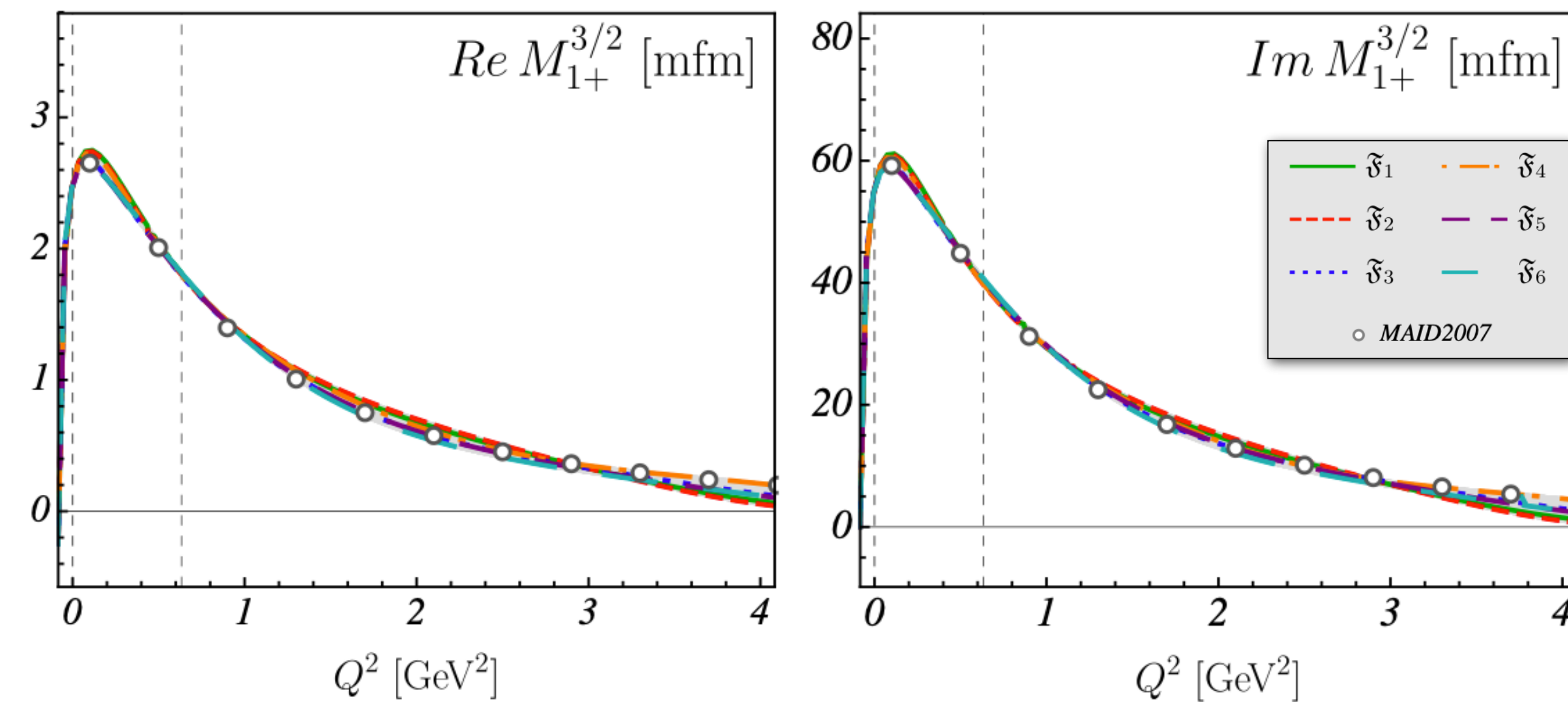
1) [JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201  
 2) H. Denizli et al. (CLAS) *PRC* 76, 015204 (2007); Thompson et al. (CLAS), *PRL*86, 1702–1706 (2001); ...

# MULTIPOLES

## Delta:

- Large multipoles well determined small systematic uncertainties

$W = 1230$  MeV



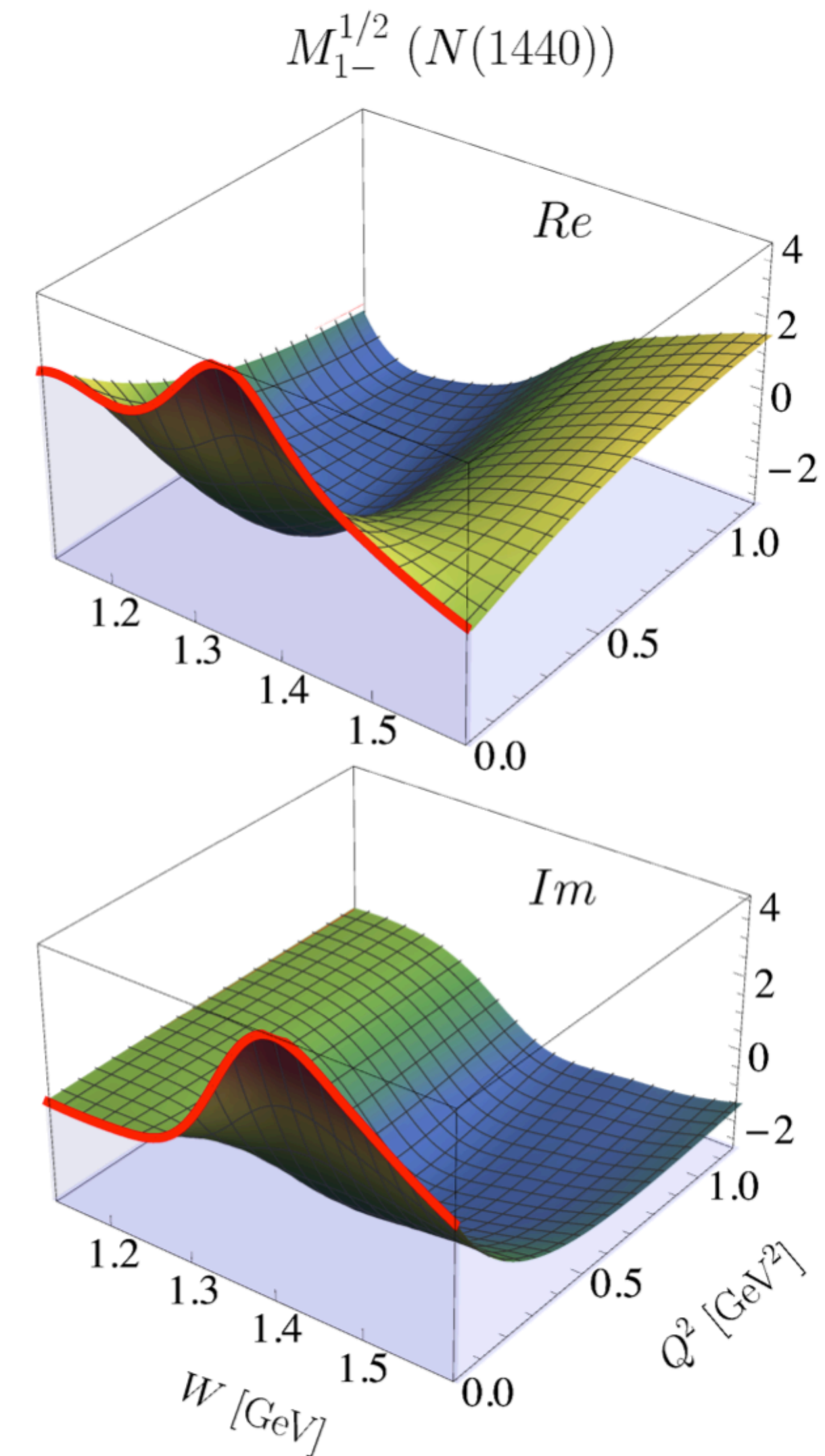
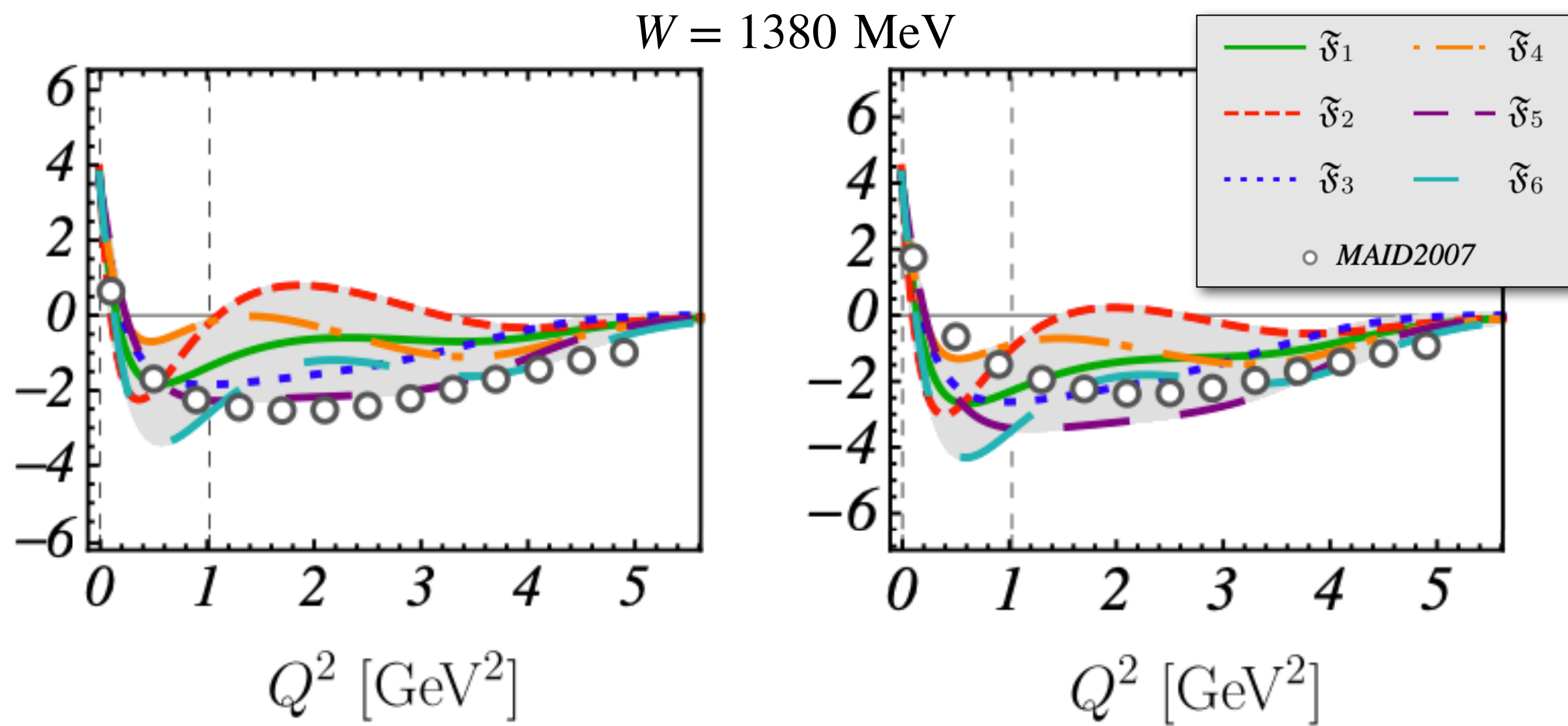
[JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201



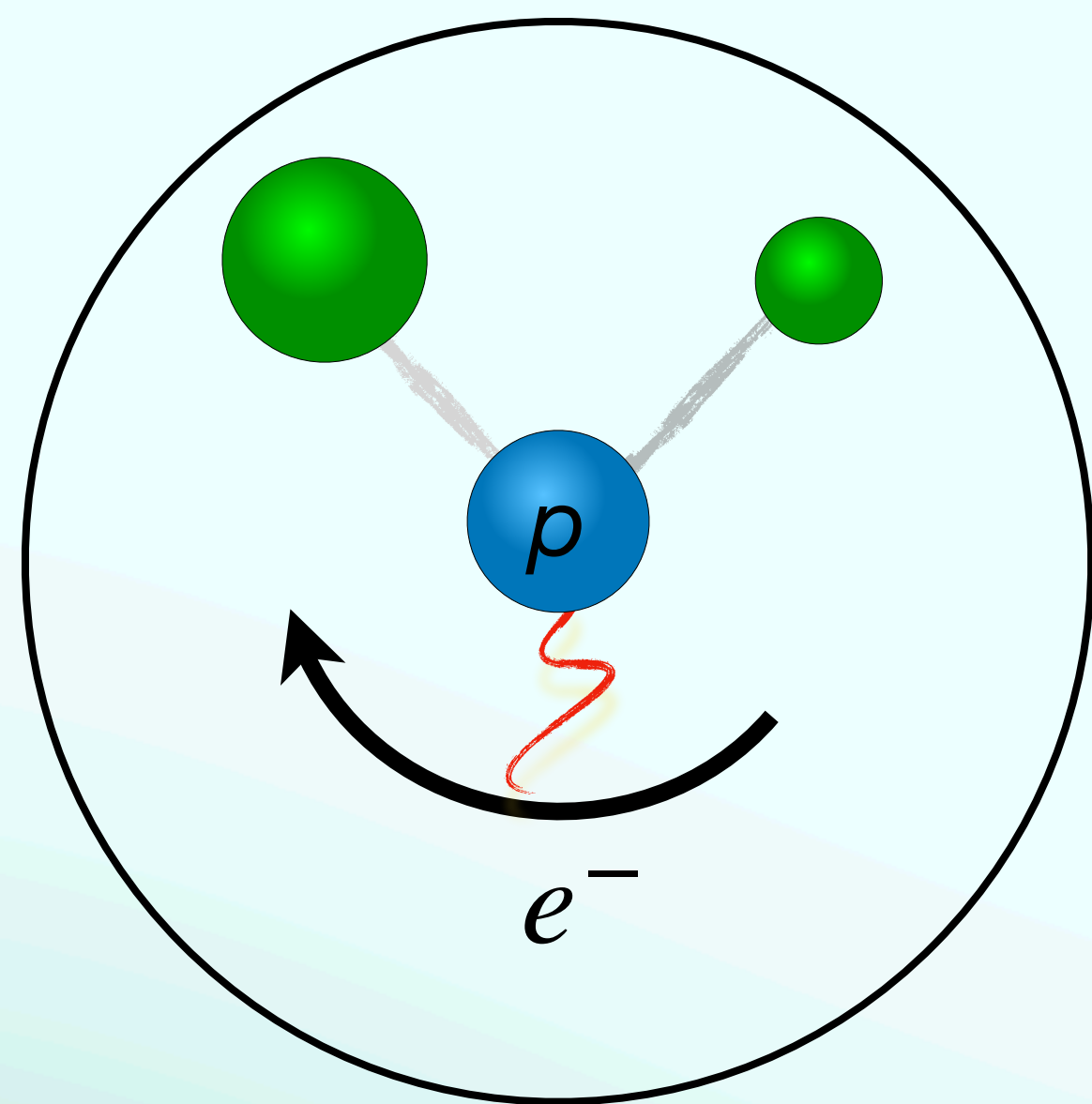
# MULTIPOLES

## Roper:

- Non-trivial  $Q^2$  behavior
- Zero transition



[JBW] MM et al. *Phys.Rev.C* 103 (2021) 6; *Phys.Rev.C* 106 (2022) 015201



# SUMMARY

# SUMMARY

## Jülich-Bonn-Washington model

- ➔ new model developed
- ➔ constraints from scattering, photoproduction data and fundamental principles
- ➔ fits to  $\pi N/\eta N$  data finished

## ➔ WEB INTERFACE:

<https://jbw.phys.gwu.edu>



# OUTLOOK

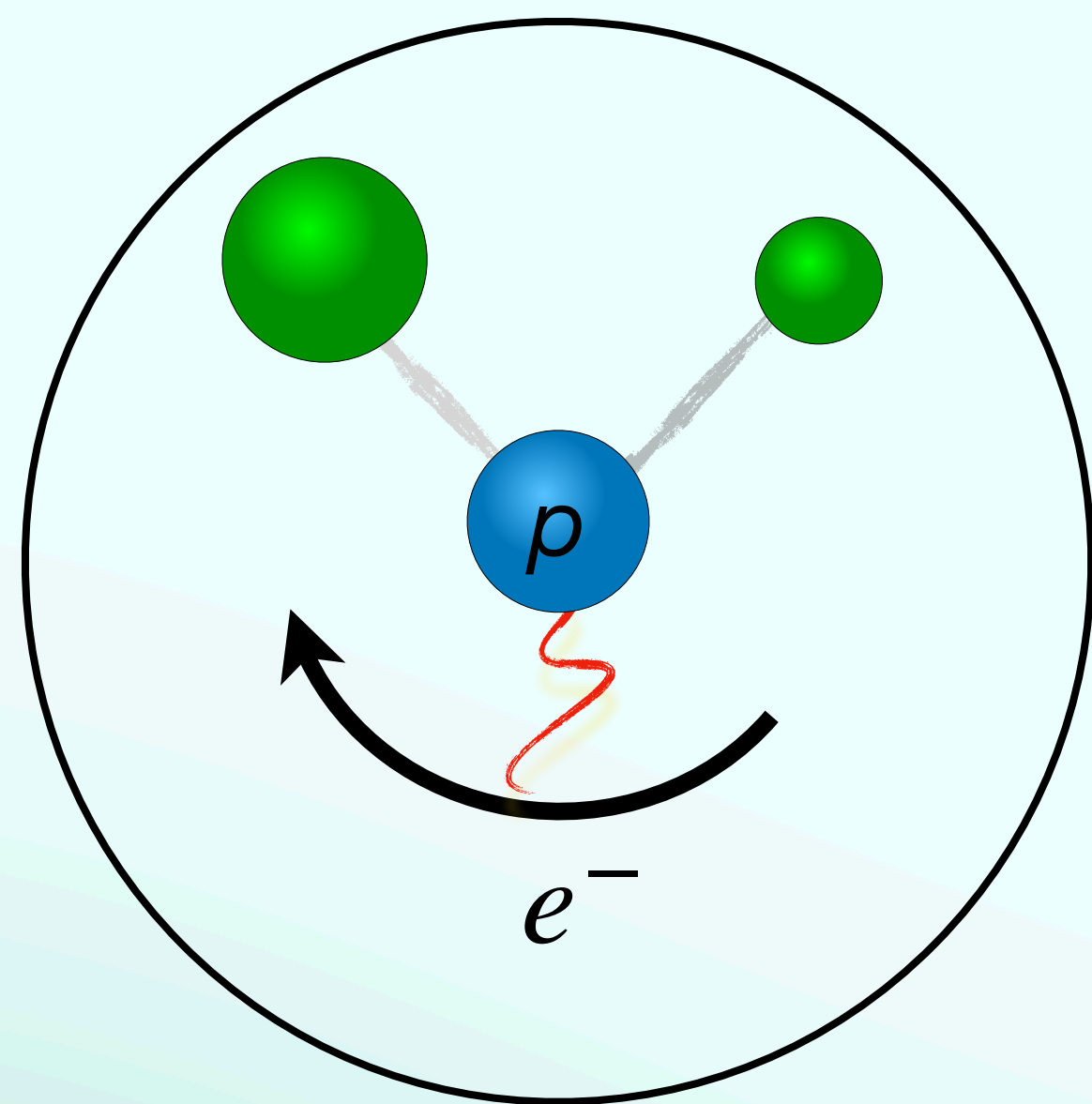
[this year]  $\pi N/\eta N/K\Lambda$  fits (nearly world data)

[this decade] simultaneous fit to scattering and photoproduction data

[this decade] statistical studies of parameter importance (LASSO, Machine Learning, ...)

Landay et al., Phys.Rev.D (2019), 1810.00075 [nucl-th]

[this decade] energy independent analysis(?)



**THANKS**



# Outlook for electroproduction analysis

Reaction	Observable	$Q^2$ [GeV]	$W$ [GeV]	Ref.
$ep \rightarrow e'p'\eta$	$\sigma_U, \sigma_{LT}, \sigma_{TT}$	1.6 – 4.6	2.0 – 3.0	[132]
	$\sigma_U, \sigma_{LT}, \sigma_{TT}$	0.13 – 3.3	1.5 – 2.3	[137]
	$d\sigma/d\Omega$	0.25 – 1.5	1.5 – 1.86	[138]
$ep \rightarrow e'K^+\Lambda$	$P_N^0$	0.8 – 3.2	1.6 – 2.7	[139]
	$\sigma_U, \sigma_{LT}, \sigma_{TT}, \sigma_{LT'}$	1.4 – 3.9	1.6 – 2.6	[140]
	$P'_x, P'_z$	0.7 – 5.4	1.6 – 2.6	[141]
	$\sigma_T, \sigma_L, \sigma_{LT}, \sigma_{TT}$	0.5 – 2.8	1.6 – 2.4	[142]
	$P'_x, P'_z$	0.3 – 1.5	1.6 – 2.15	[143]

**Table 1:** Overview of  $\eta p$  and  $K^+\Lambda$  electroproduction data measured at CLAS for different photon virtualities  $Q^2$  and total energy  $W$ . Based on material provided by courtesy of D. Carman (JLab) and I. Strakovsky (GW).

- Many of these (and similar) data await analysis.
- Many more data to emerge at Jlab ( $Q^2 = 5 - 12 \text{ GeV}^2$ )  
 e.g.: Carman, Joo, Moiseev, **Few Body Syst. 61, 29 (2020)**
- Approved Jlab experiments to study
  - Higher-lying nucleon resonances
  - Hybrid baryons
  - High- $Q^2$  transition between nonperturbative and perturbative QCD regimes