

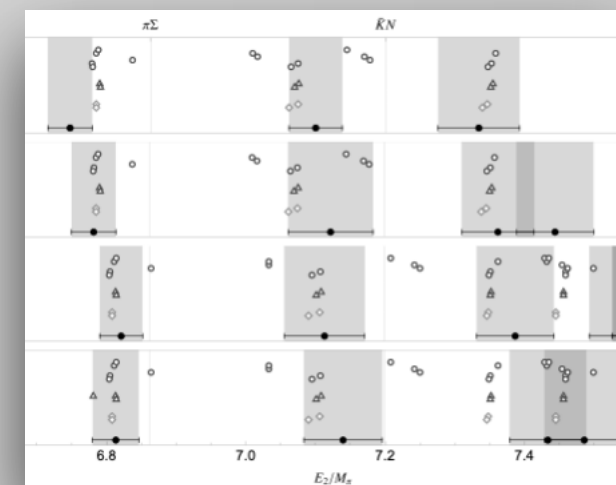
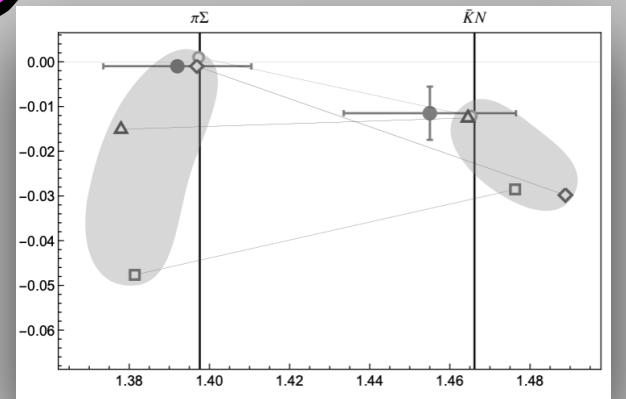
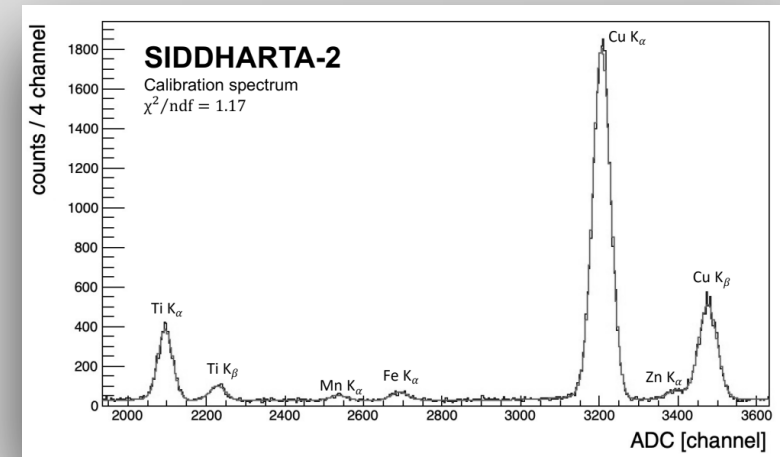
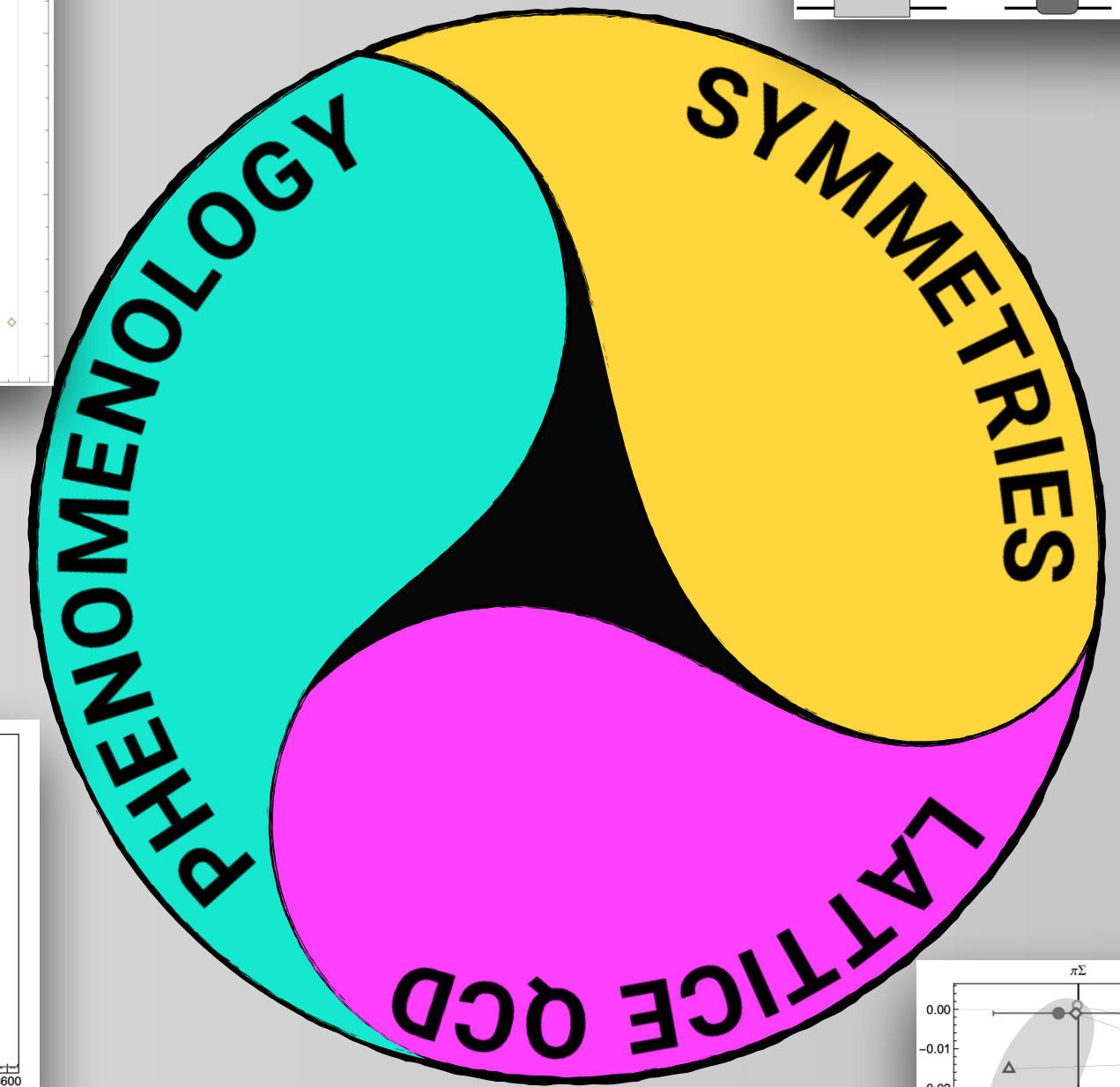
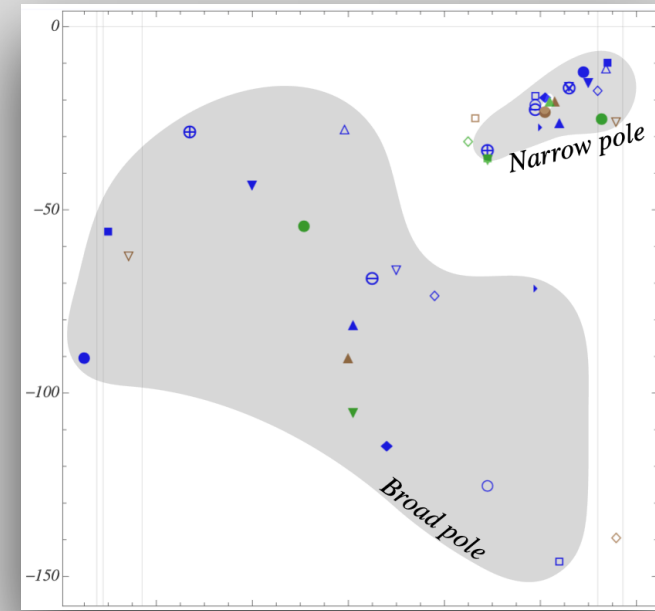
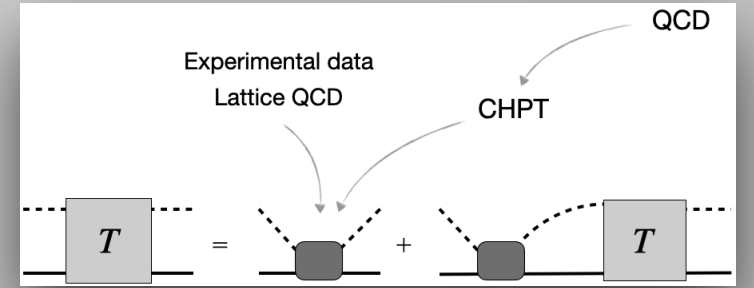
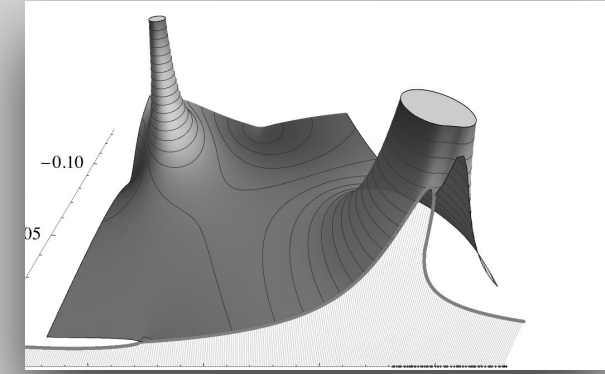
THEORY OF KAON-NUCLEON INTERACTION

26.-30.08.2024 — EXA/LEAP'24

MAXIM MAI

UNIVERSITY OF BERN (MAIN)

THE GEORGE WASHINGTON UNIVERSITY



TRR110: NSFC Grant No. 12070131001, DFG Project-ID 196253076

DOE: DE-SC0016582, DE-AC05-06OR23177, DE-FG02-95ER40907

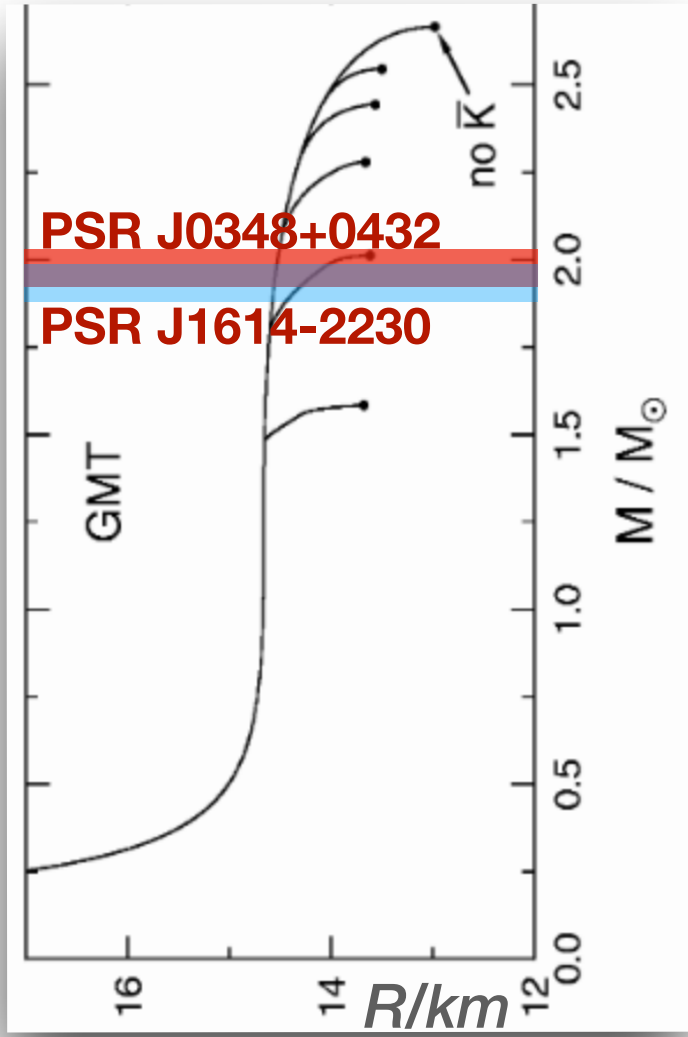
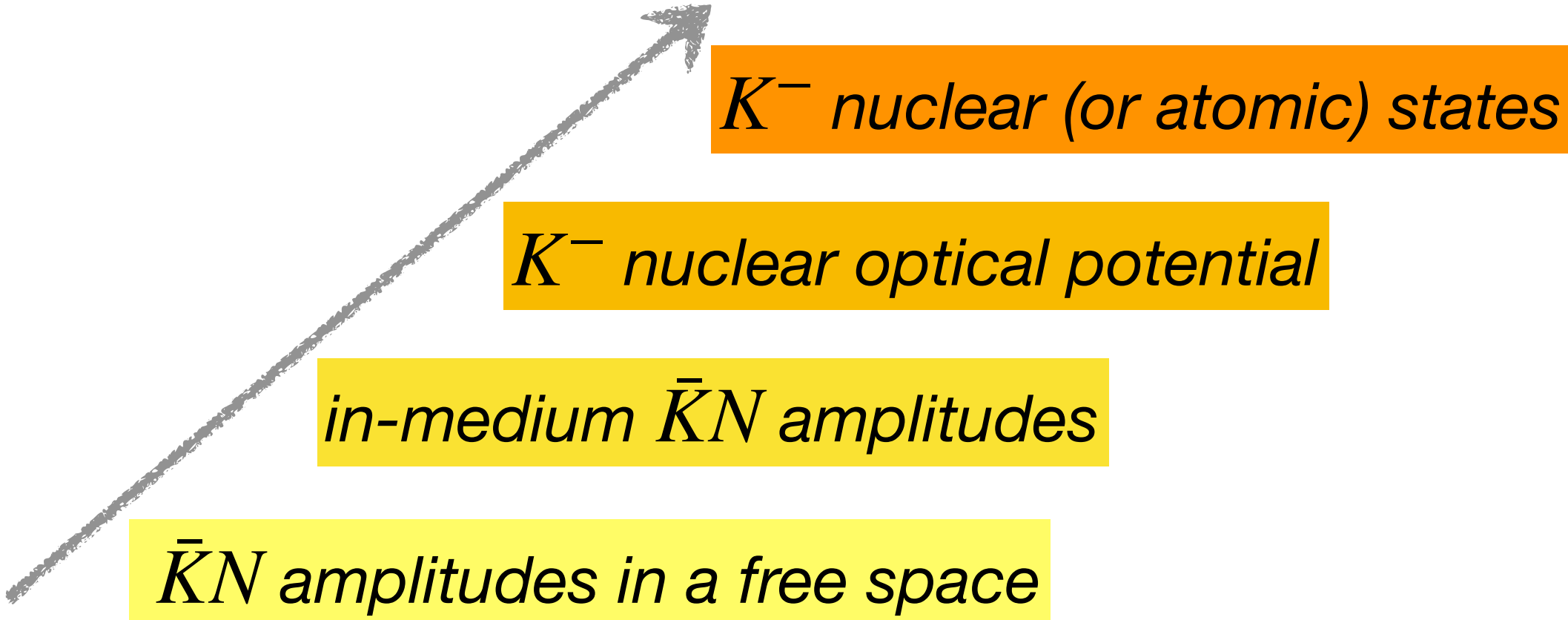
DFG: Heisenberg Programme (project number: 532635001)

NSF: PHY-2012289

OVERARCHING IMPACT

- Test of our understanding of QCD
- $\bar{K}NN$ & $\bar{K}NNN$ bound states^[1]
- K^- in medium^[2]

K^- -condensate can change NS EoS
 ... many theoretical challenges^[3]



Pal et al., Nucl. Phys. A **674**, 553 (2000)

[1] Review by Gal/Hungerford/Millener (2016); **Talk: FRIEDMAN [Tuesday] GAZDA [Friday]**
 [2] Mareš et al. Acta Phys. Polon. B 51, 129 (2020); Hrtánková et al. Phys.Lett. B 785, 90 (2018)
 [3] **Talk: JINNO [Thursday]**

STRANGENESS PROGRAM/HISTORY

*“There is a large experimental program on production of S particles
... But just between us theoretical physicists:
What do we do with all these data?
We can’t do anything.”*

R. P. FEYNMAN

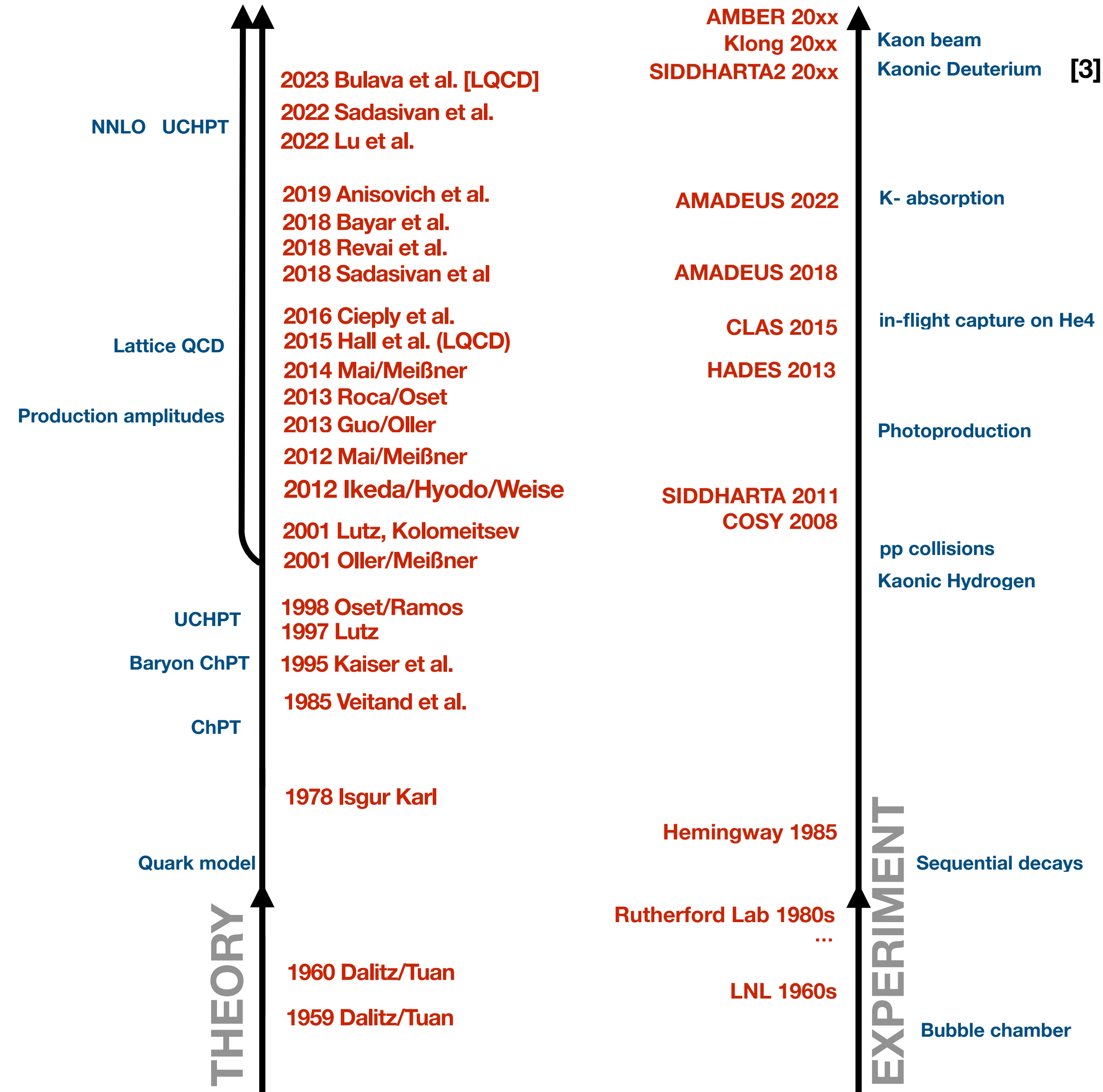
- [1] Sakurai Annals Phys. 11, 1 (1960).
- [2] MM EPJST 230 (2021) “Review of the $\Lambda(1405)$ A curious case of a strangeness resonance”;
- [3] **TALK: SGARAMELLA[Thursday]**
- [4] Oller/Meißner Phys. Lett. B 500, 263 (2001)
- [5] Weise/Oset/Molina/Döring/MM/Hyodo/Ikeda/Geng/Lu/Lutz/...



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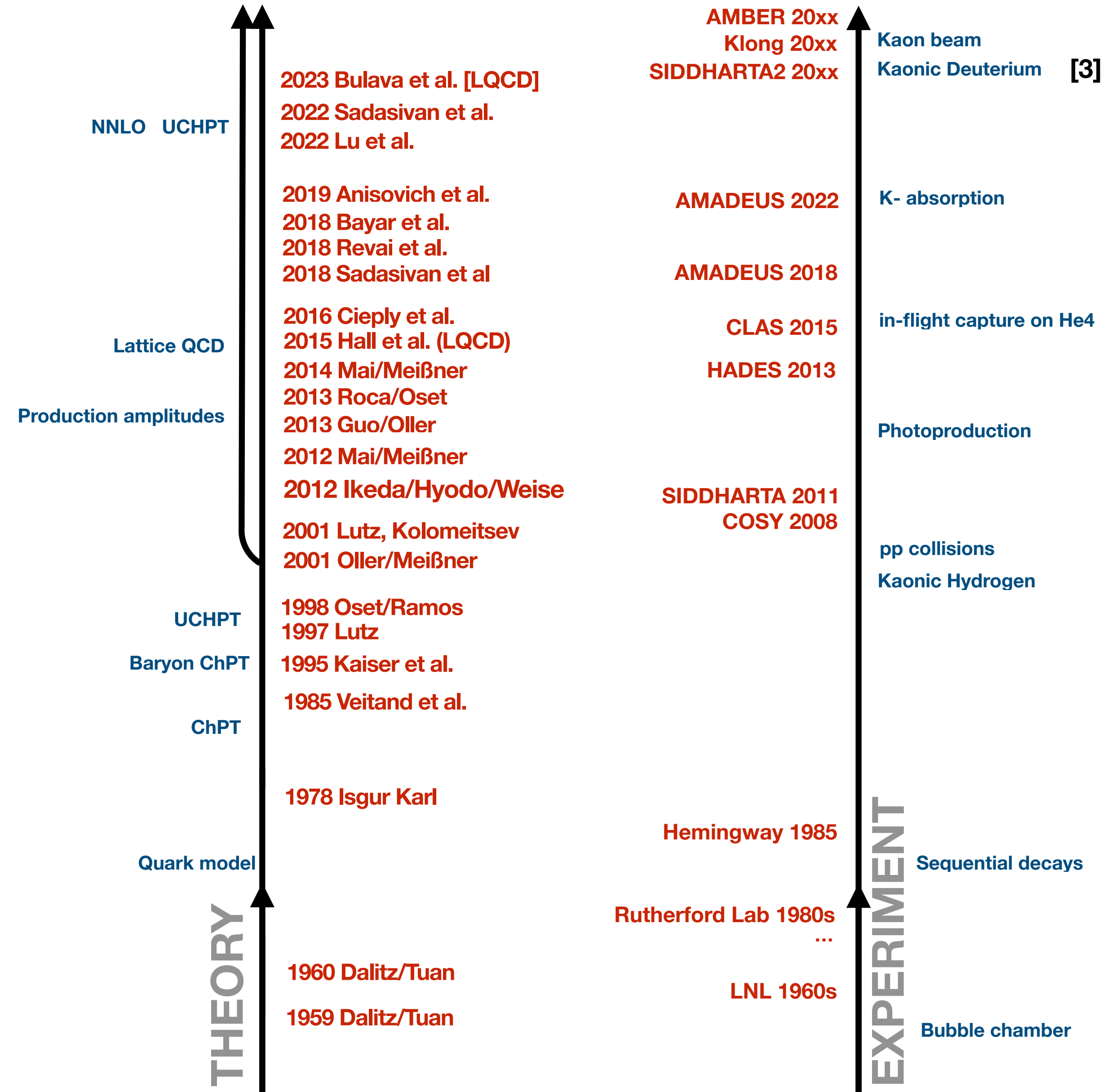
[4] Oller/Meißner Phys. Lett. B 500, 263 (2001)

[5] Weise/Oset/Molina/Döring/MM/Hyodo/Ikeda/Geng/Lu/Lutz/...

NEW STRANGENESS RESONANCES

Sub- $(\bar{K}N)$ -threshold $\Lambda(1405)$ resonance

- second state $\Lambda(1380)$ predicted from UCHPT^[4]
- confirmed by many critical tests^[5] / LQCD



[1] Sakurai Annals Phys. 11, 1 (1960).

[2] MM EPJST 230 (2021) “Review of the $\Lambda(1405)$ A curious case of a strangeness resonance”;

[3] **TALK: SGARAMELLA[Thursday]**

[4] Oller/Meißner Phys. Lett. B 500, 263 (2001)

[5] Weise/Oset/Molina/Döring/MM/Hyodo/ Ikeda/Geng/Lu/Lutz/...

THEORY

QUANTUM CHROMODYNAMICS

Sub- $(\bar{K}N)$ -threshold $\Lambda(1405)$ resonance

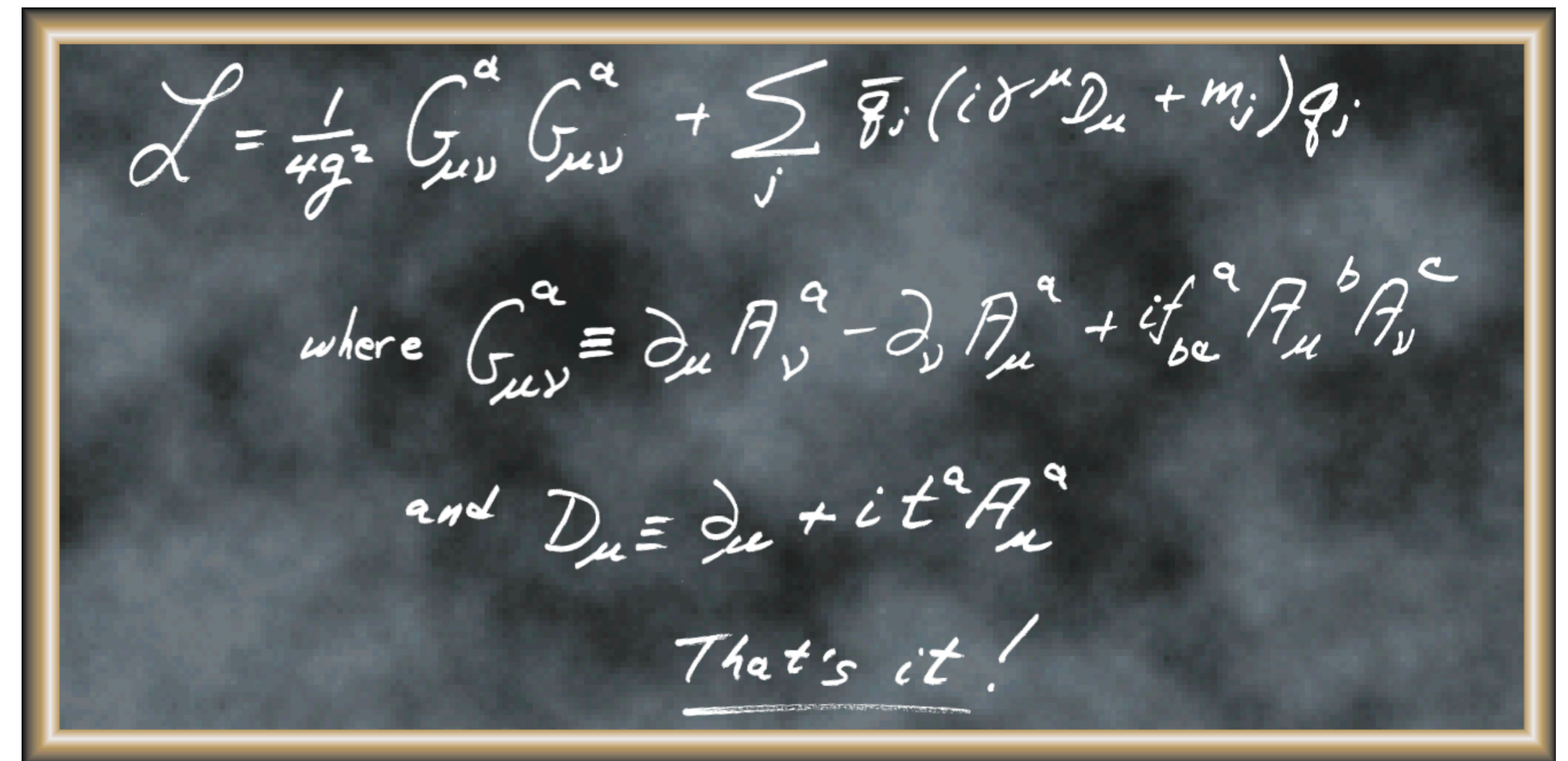
➔ no direct experimental verification

🤔 why not directly from QCD?

➔ non-perturbative energy regime

🤔 why not QCD/EFT?

➔ resonant interaction



The image shows a chalkboard with handwritten mathematical equations for the QCD Lagrangian. The first equation is $\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_j \bar{q}_j (i\gamma^\mu D_\mu + m_j) q_j$. Below it, the gluon field strength tensor is defined as $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + if_{bc}^a A_\mu^b A_\nu^c$. The covariant derivative is defined as $D_\mu \equiv \partial_\mu + it^a A_\mu^a$. The text "That's it!" is written at the bottom of the board.

http://frankwilczek.com/Wilczek_Easy_Pieces/298_QCD_Made_Simple.pdf

- [1] Sakurai Annals Phys. 11, 1 (1960).
- [2] MM EPJST 230 (2021) "Review of the $\Lambda(1405)$ A curious case of a strangeness resonance";
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TOOLS

Sub- $(\bar{K}N)$ -threshold $\Lambda(1405)$ resonance

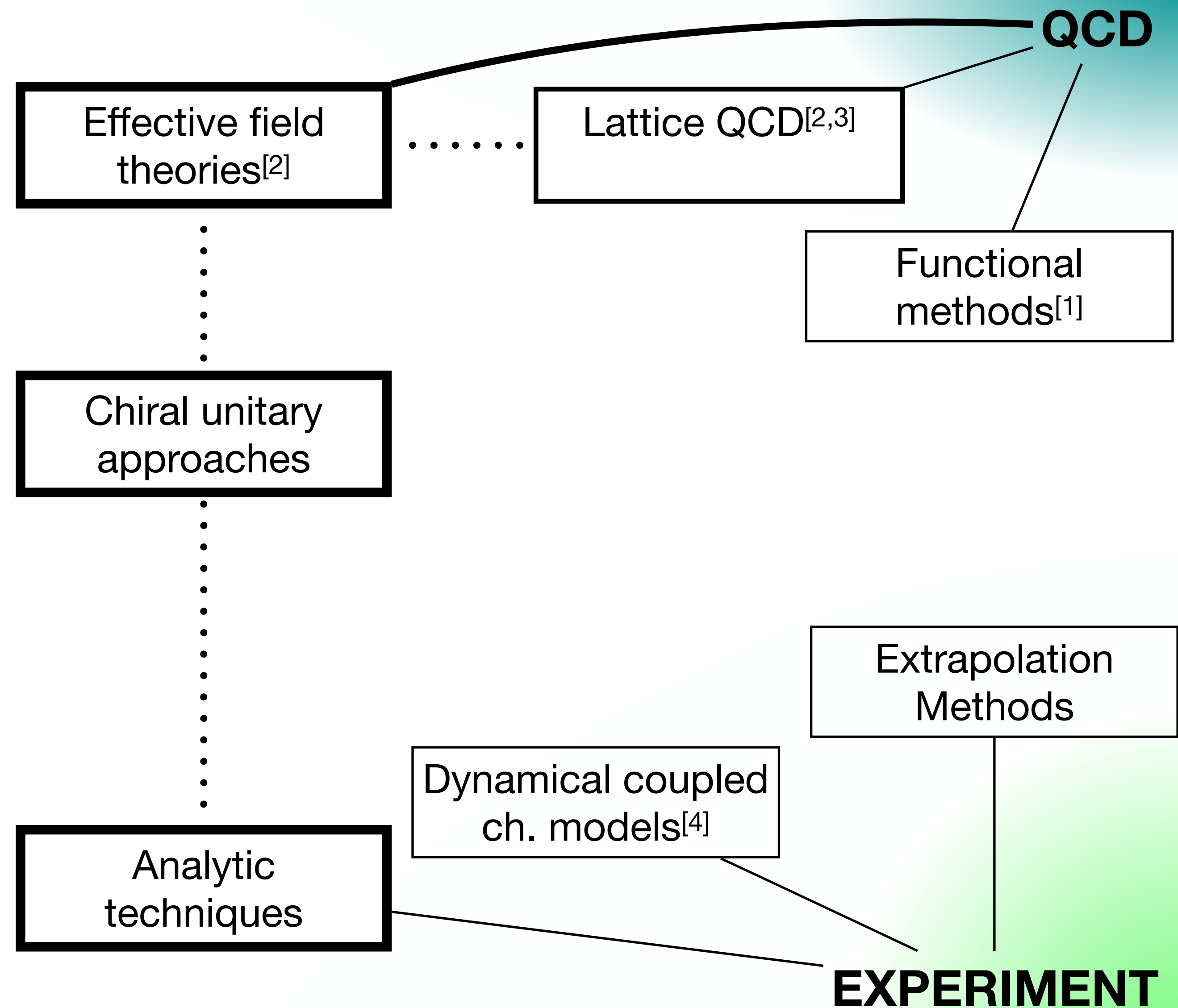
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[1] Review: Eichmann/Sanchis-Alepuz/Alkofer/Fischer Prog.Part.Nucl.Phys. 91 (2016) 1-100

[2] Review: Briceño/Dudek/Young Rev.Mod.Phys. 90 (2018)

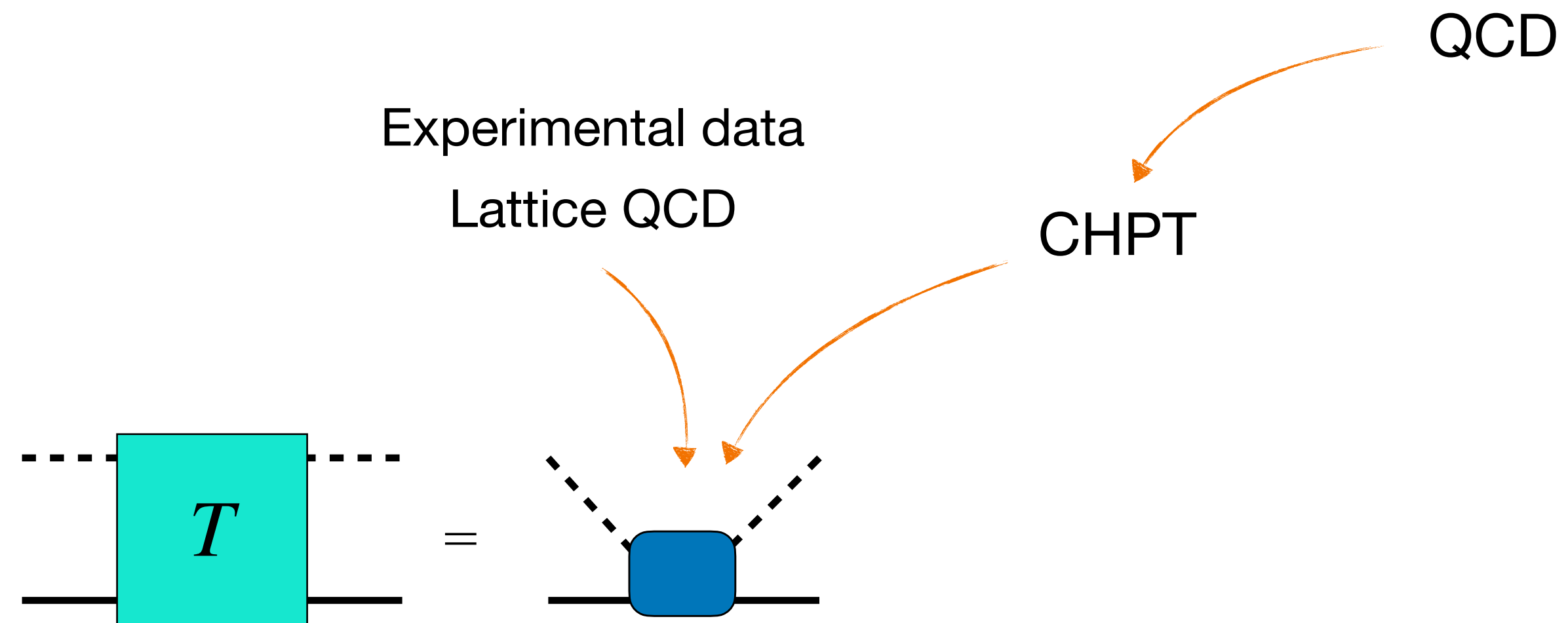
[3] Review: MM/Meißner/Urbach Phys.Rept. 1001 (2023) 1-6

[4] Review: Döring/Haidenbauer/Sato/MM PPNP in progress

UNIVERSAL PARAMETERS

Transition amplitude – chiral unitary approach[1]

Chiral Perturbation Theory (#QCD#EFT)
form of the interaction at low energies



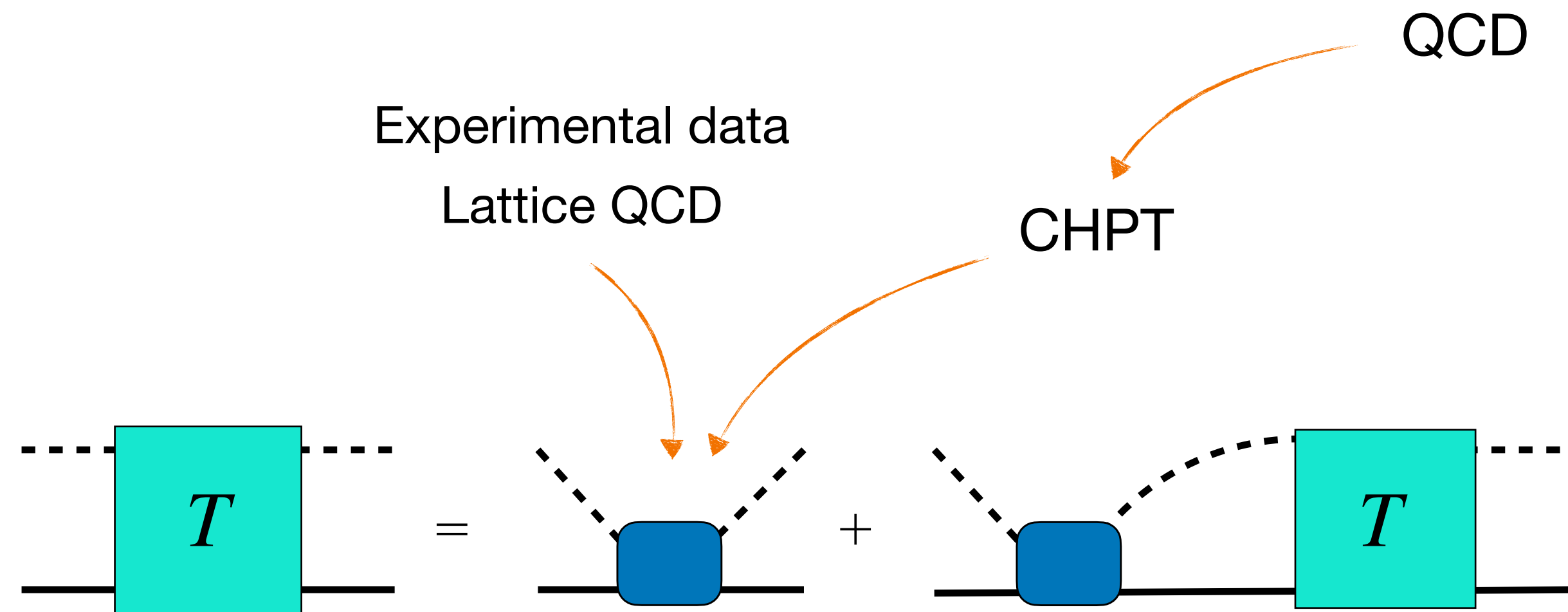
[1] Weise/Kaiser/Meißner/Lutz/Oset/Oller/Ramos/Hyodo/Borasoy...

[2] Kaiser/Siegel/Weise Phys.Lett.B 362 (1995) Lutz/Soyeur Nucl.Phys.A 773 (2006); MM et al. Phys.Lett.B 697 (2011); ...

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Unitary amplitude from the Bethe-Salpeter equation

(Fit free parameters to experimental data or LQCD)

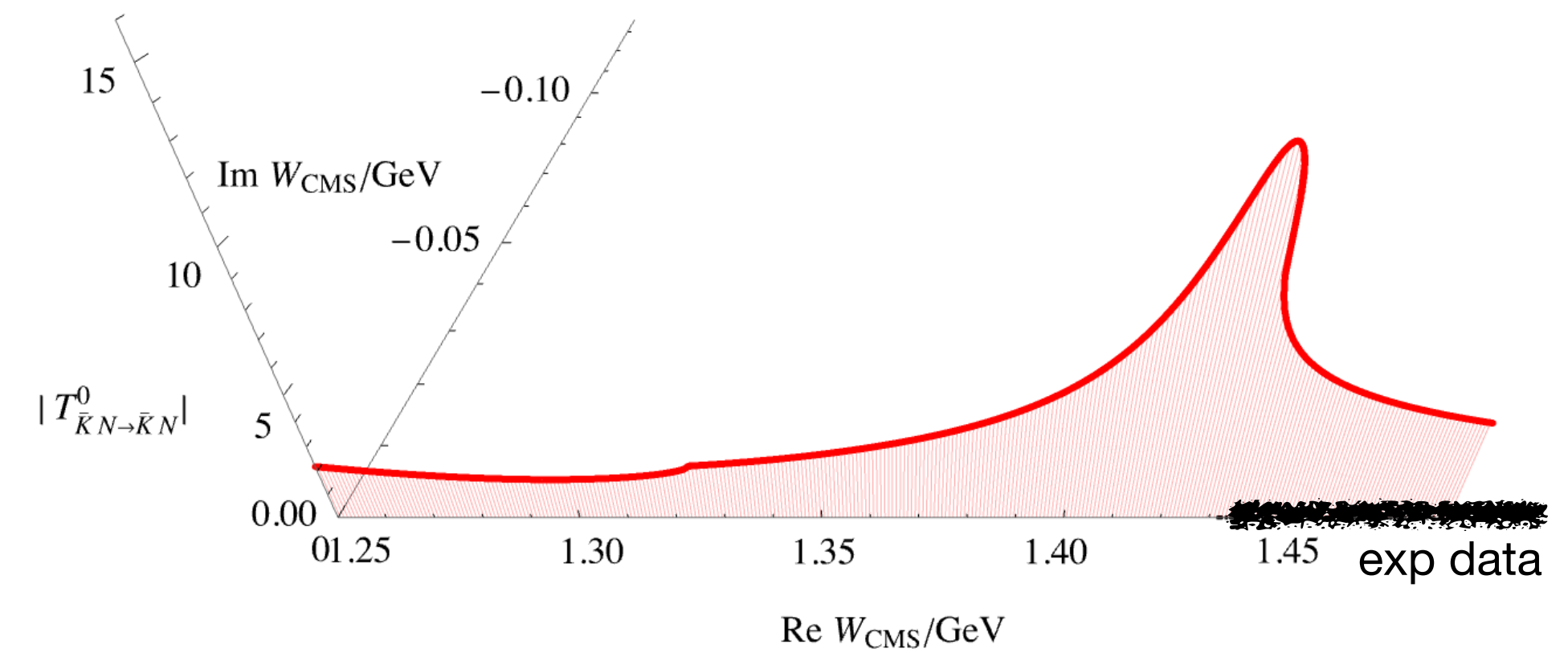
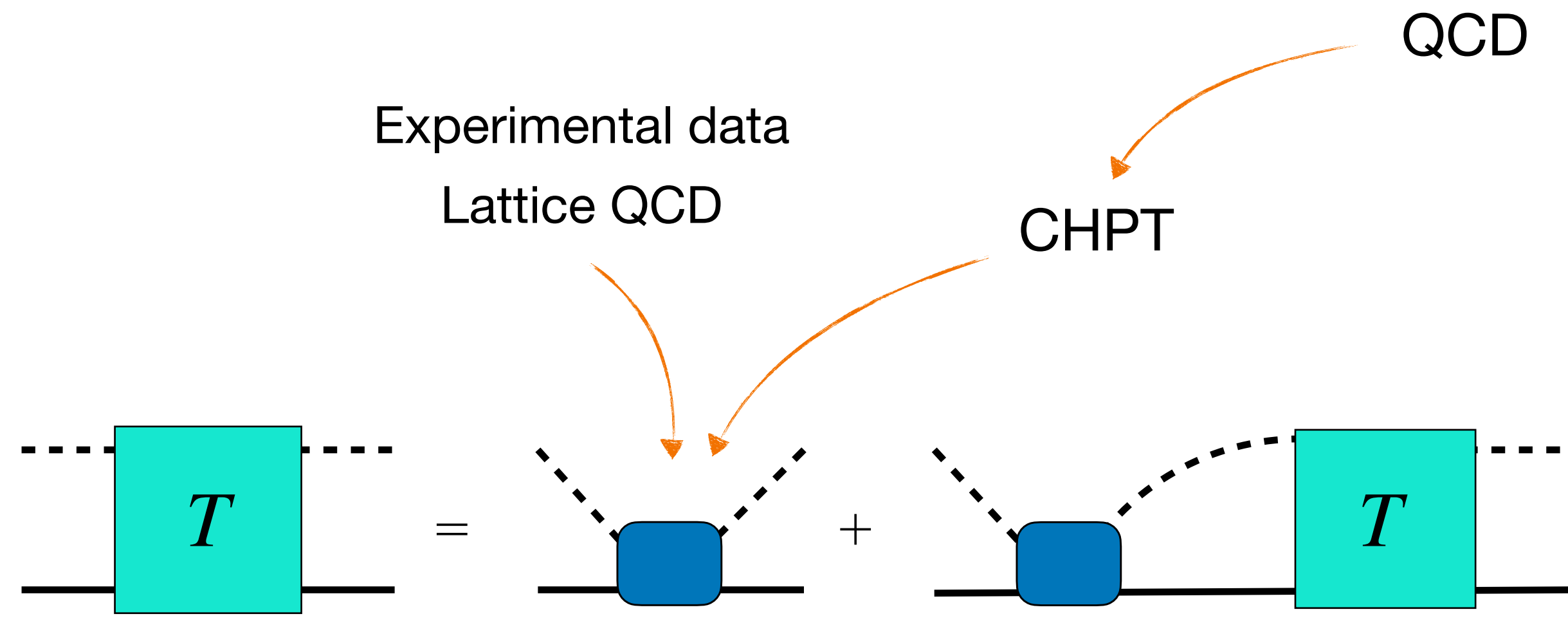
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UNIVERSAL PARAMETERS

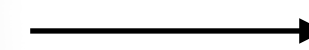
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S-matrix principles

analyticity, unitarity, Riemann sheets, ...

[1] Weise/Kaiser/Meißner/Lutz/Oset/Oller/Ramos/Hyodo/Borasoy...

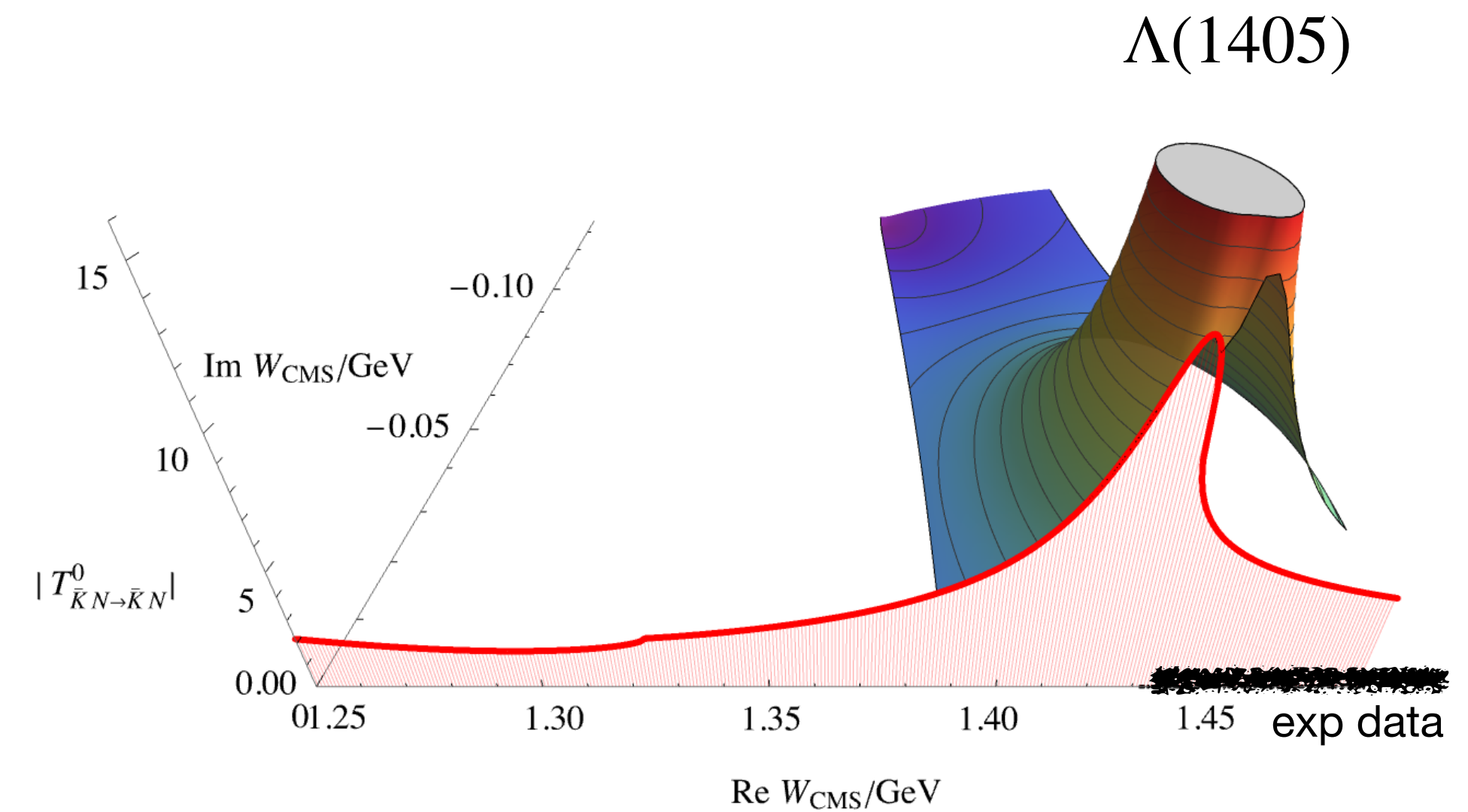
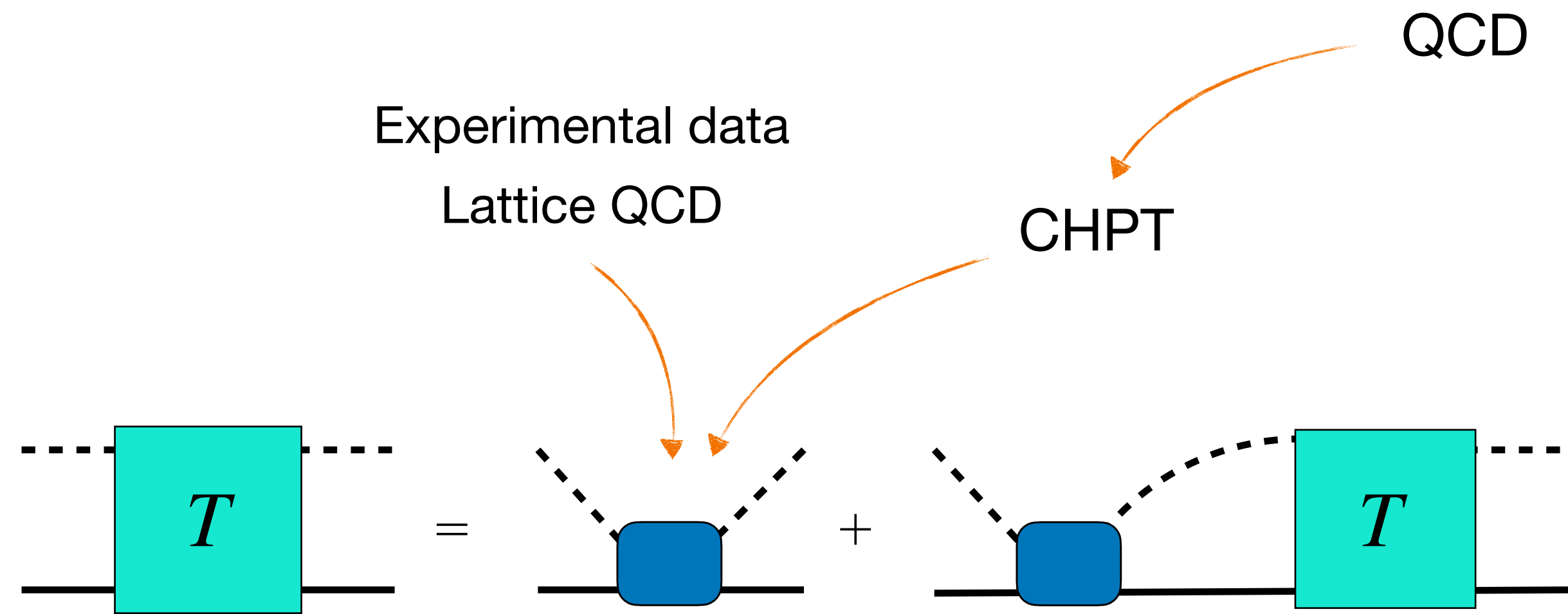
[2] Kaiser/Siegel/Weise Phys.Lett.B 362 (1995) Lutz/Soyeur Nucl.Phys.A 773 (2006); MM et al. Phys.Lett.B 697 (2011); ...

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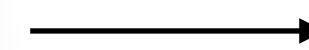
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*universal
reaction-independent parameters*



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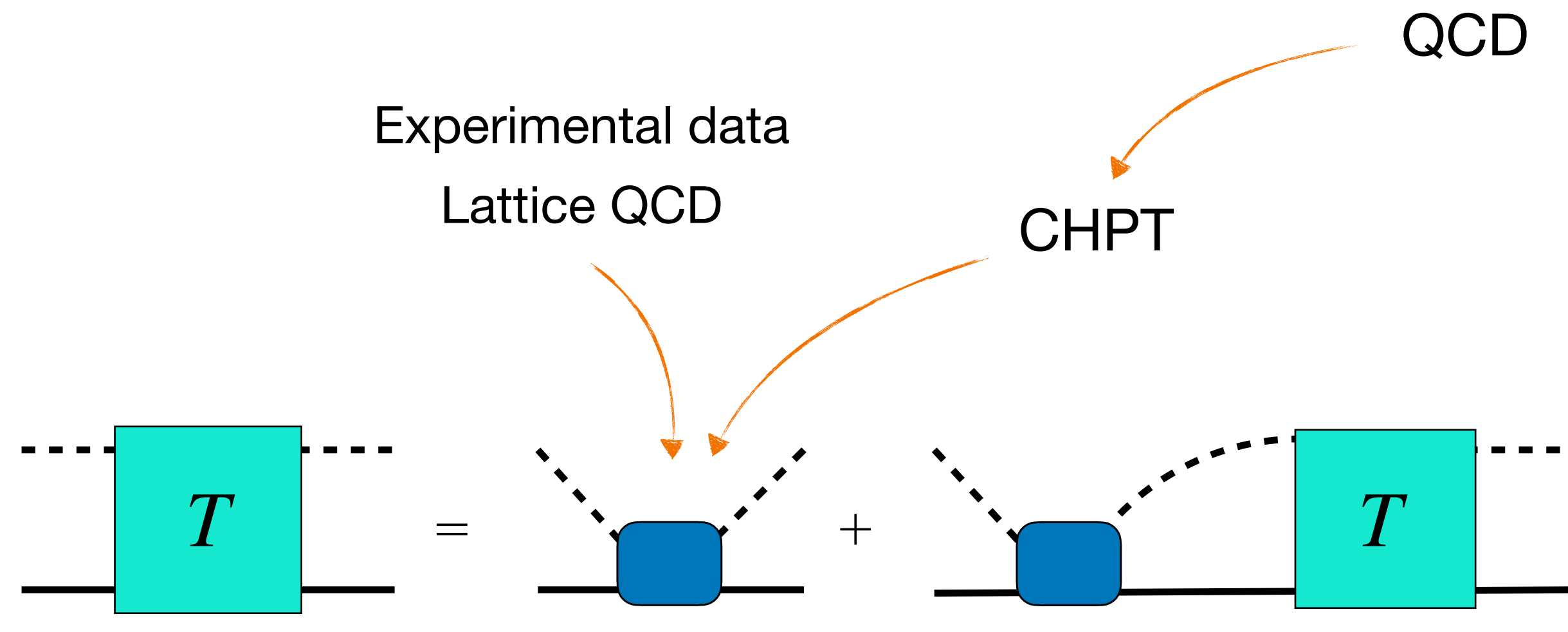
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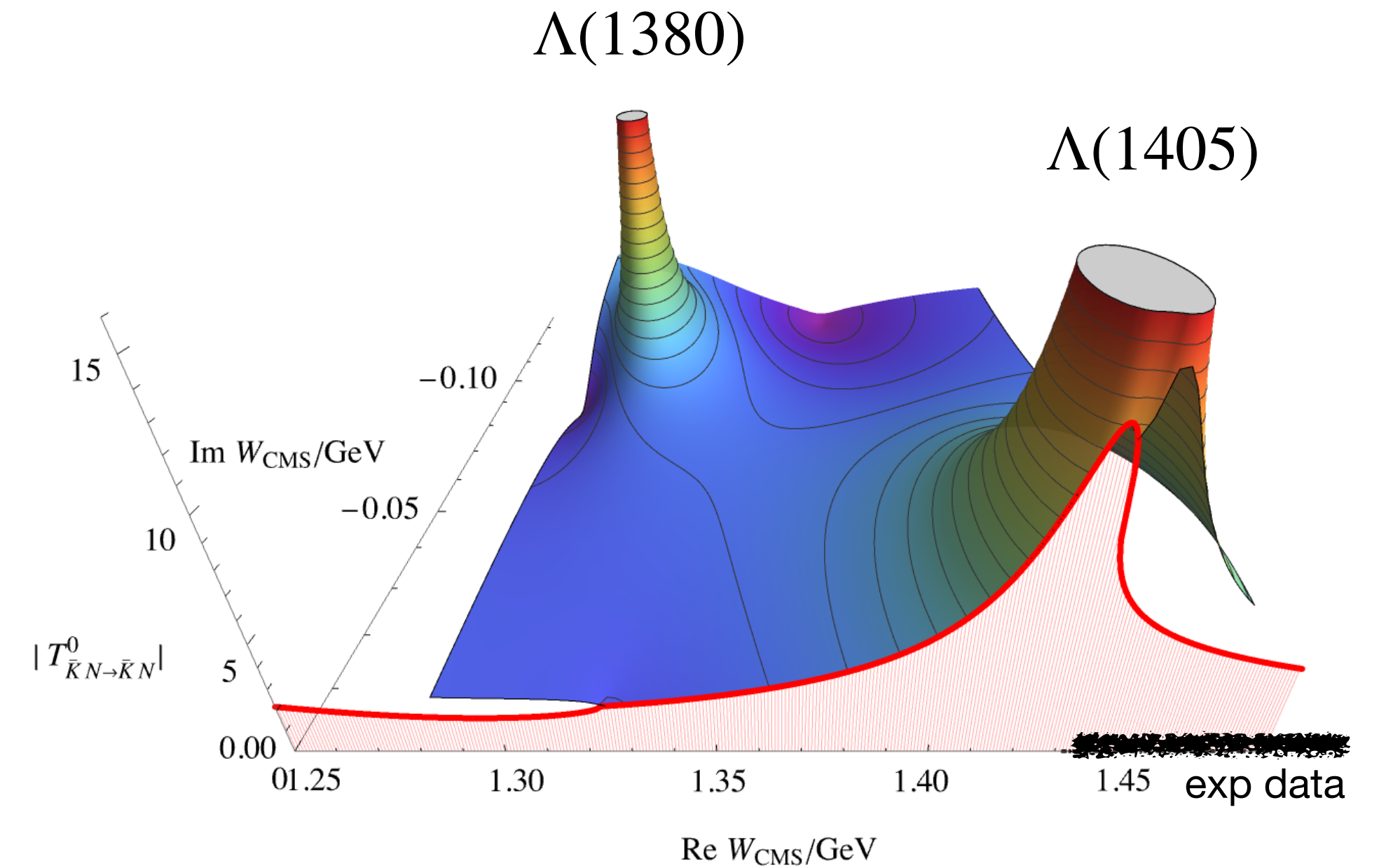
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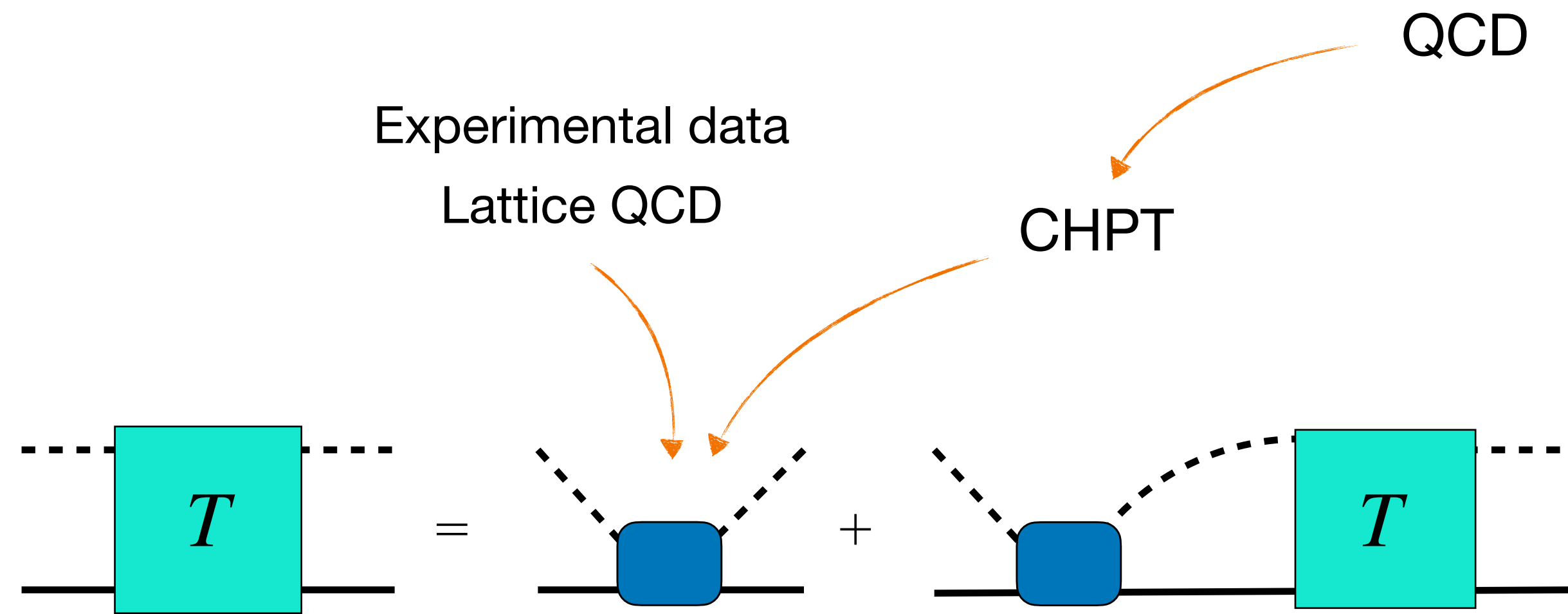
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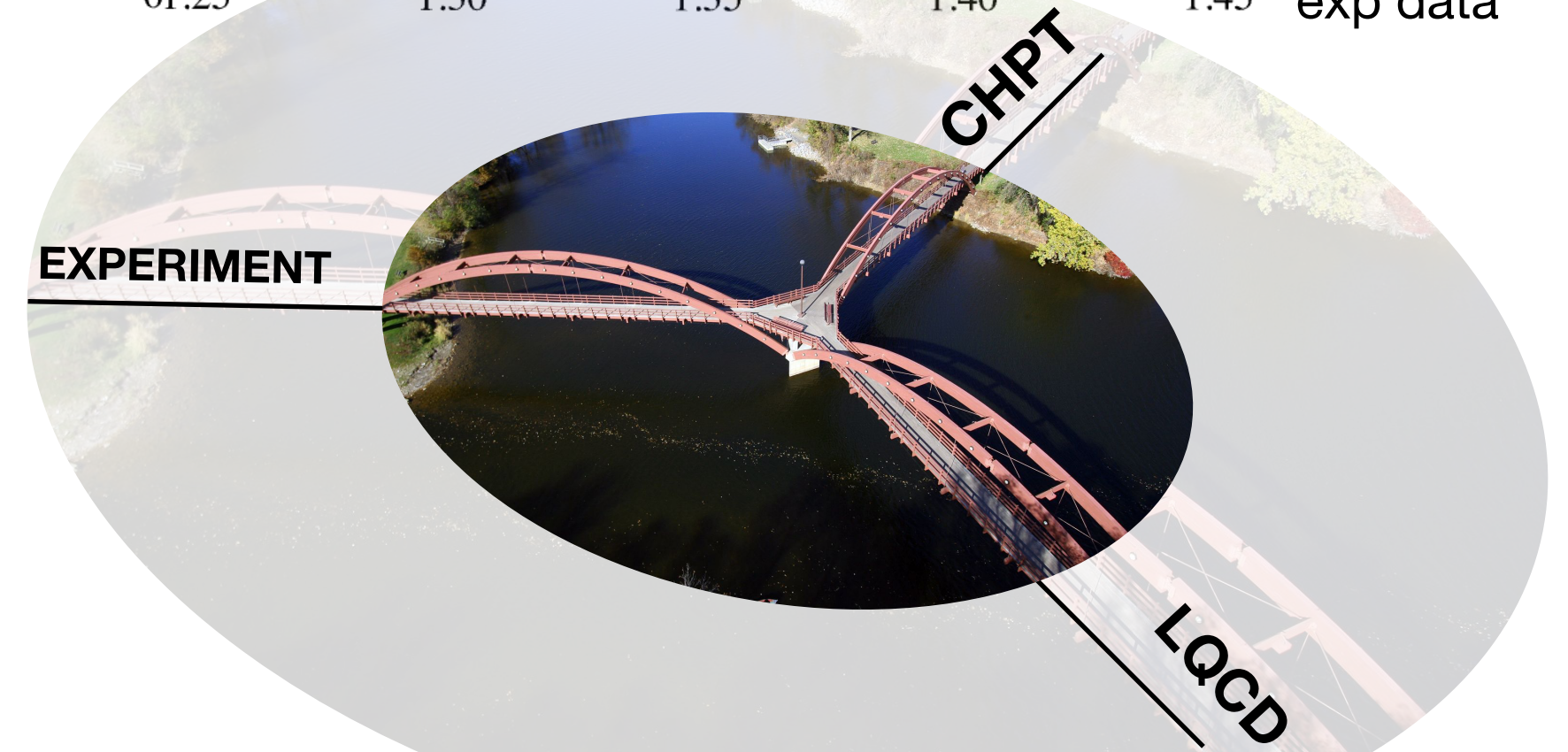
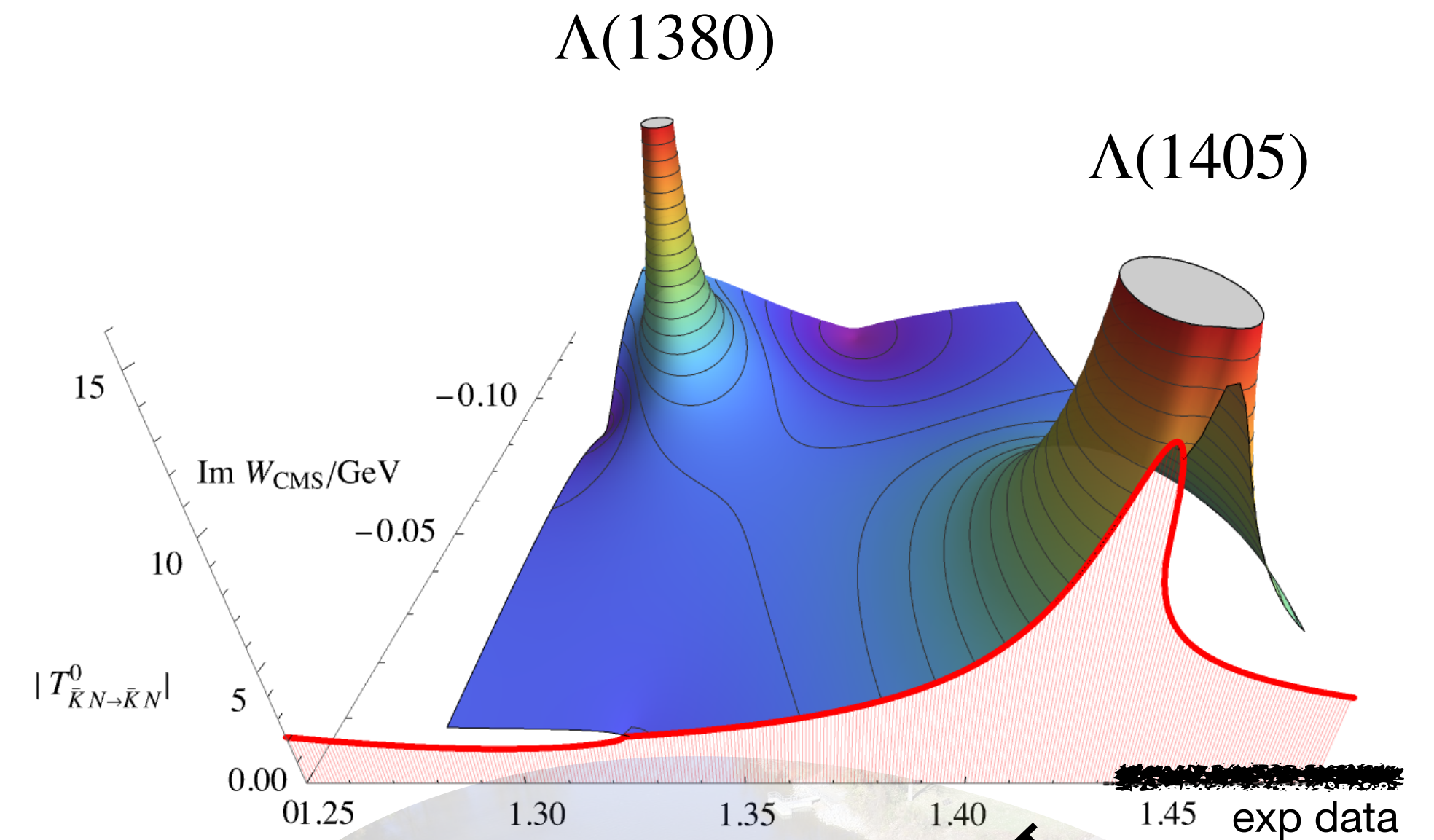
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APPLICATIONS

MESON-BARYON SCATTERING

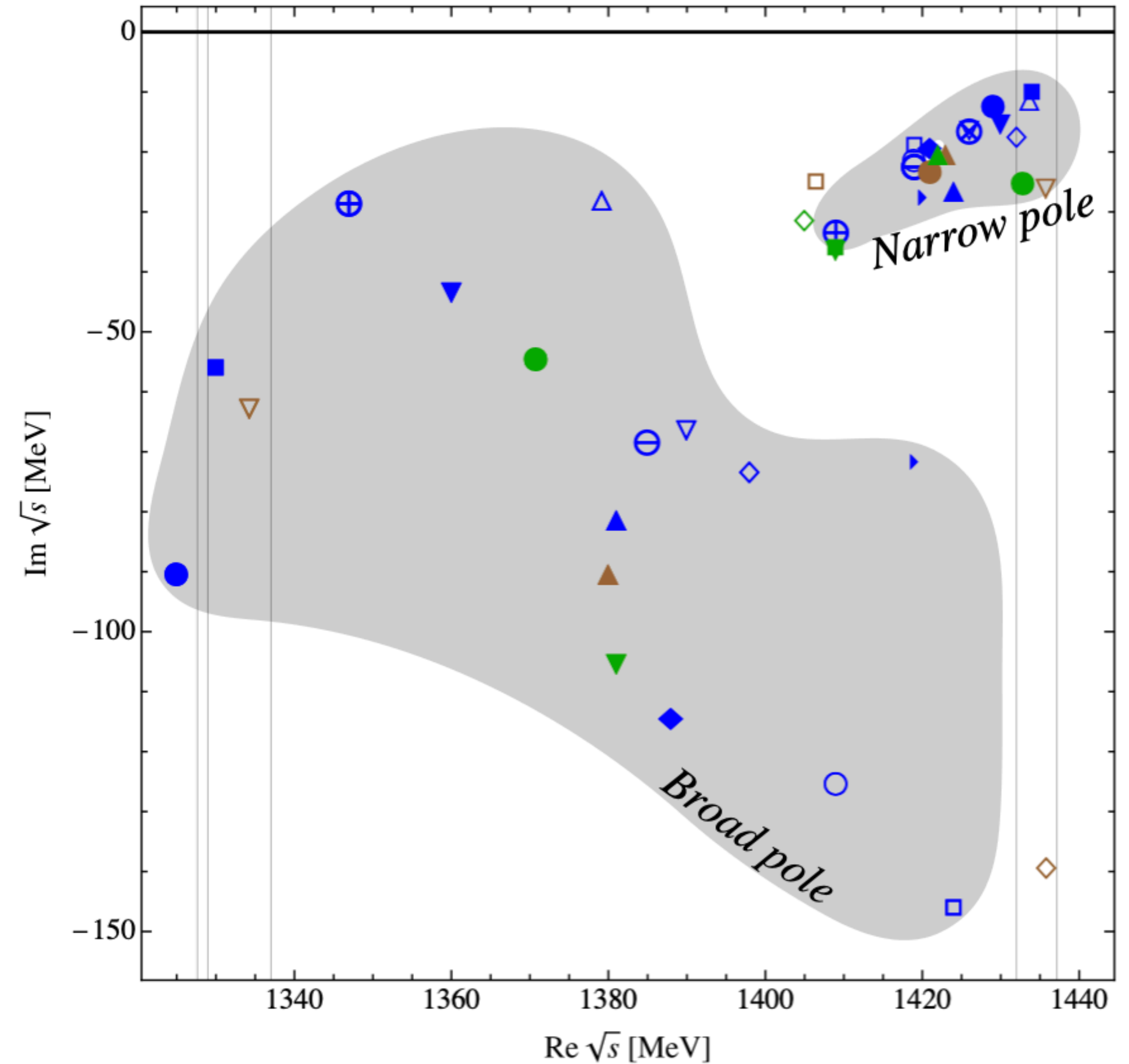
Review: MM Eur.Phys.J.ST 230 (2021)

Various implementations

- many scenarios with NLO kernel^[1]
- NNLO calculation^[2] including $\bar{K}N/\pi N/KN$

Common feature

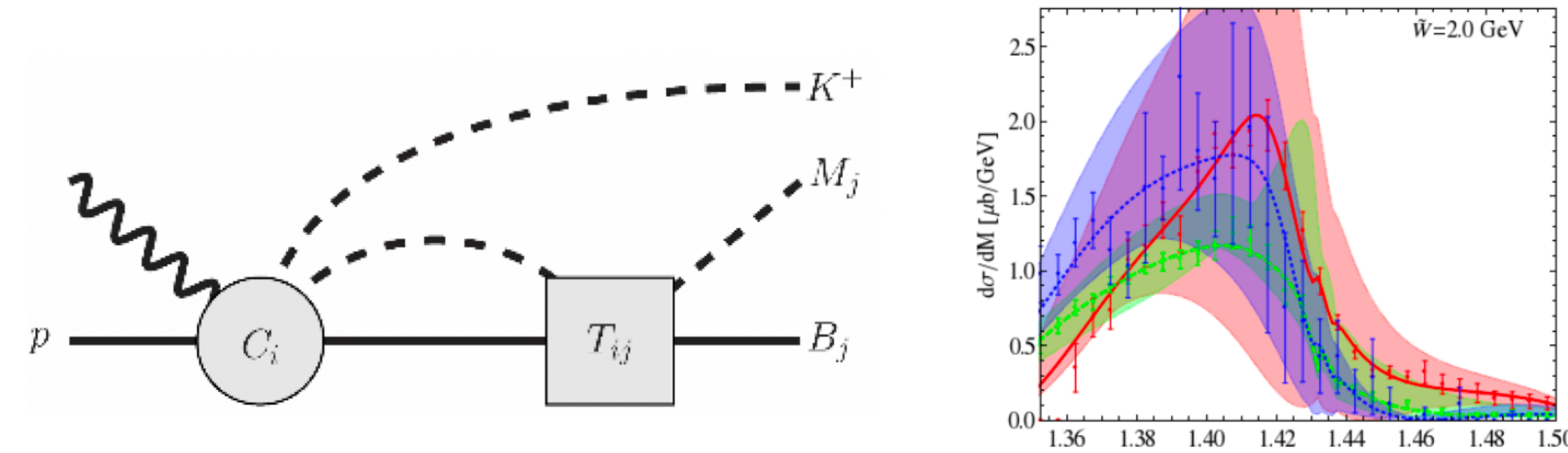
- fit to threshold and scattering data
- two poles persist



[1] Ikeda/Hyodo/Weise (2012); Guo/Oller (2013); MM/Meißner (2013,14); Sadasivan et al. (2019)

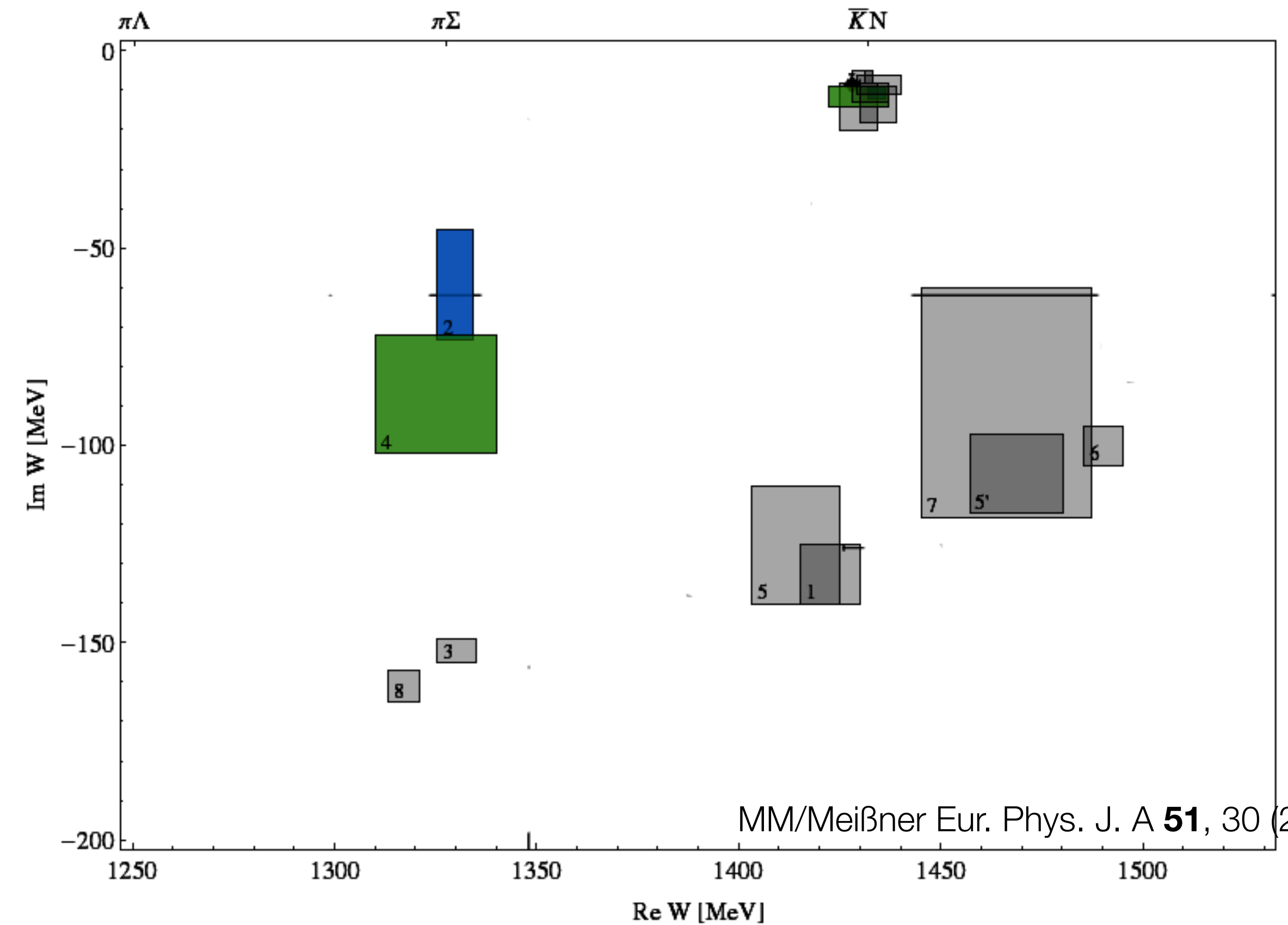
[2] Lu/Geng/Döring/MM (2022)

PHOTON INDUCED REACTIONS



High precision $\gamma p \rightarrow K^+ \pi \Sigma$ data from CLAS@JLAB^[1]

- data driven two-meson photo-production mechanism^[2]
- reduced systematic uncertainty (various model solutions)



[1] Moryia et al (CLAS coll) 2012, upcoming new data from GlueX

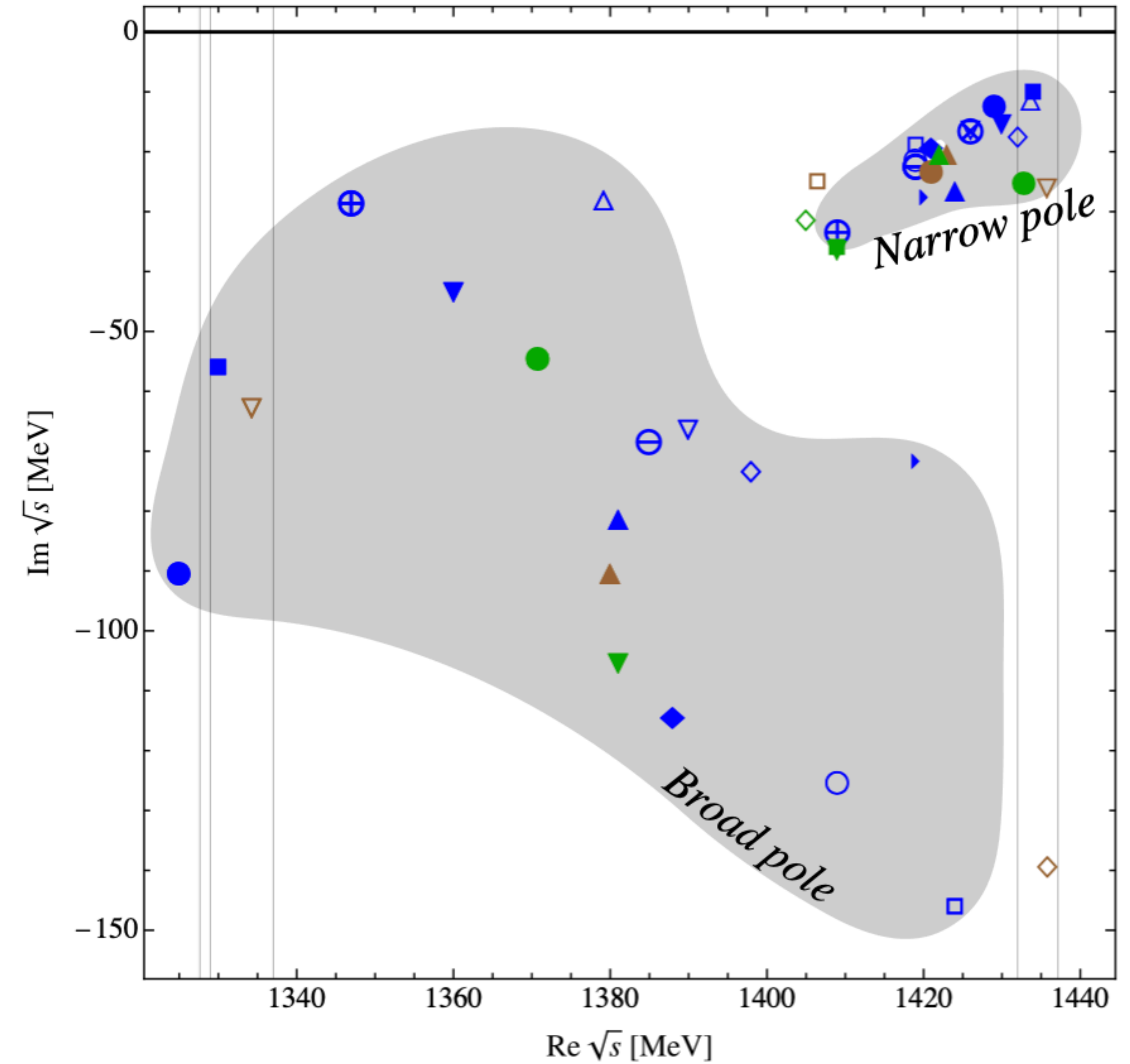
[2] Roca/Oset Phys. Rev. C **87**, 055201 (2013); MM/Meißner Eur. Phys. J. A **51**, 30 (2015)

SIDDHARTA 1 & 2

Review: MM Eur.Phys.J.ST 230 (2021)

Kaonic hydrogen^[1]

- crucial constraint on $a_{K-p}(a_0, a_1)$



[1] Bazzi et al. SIDDHARTA collaboration (2009)

[2] **TALK: SGARAMELLA[Thursday]**

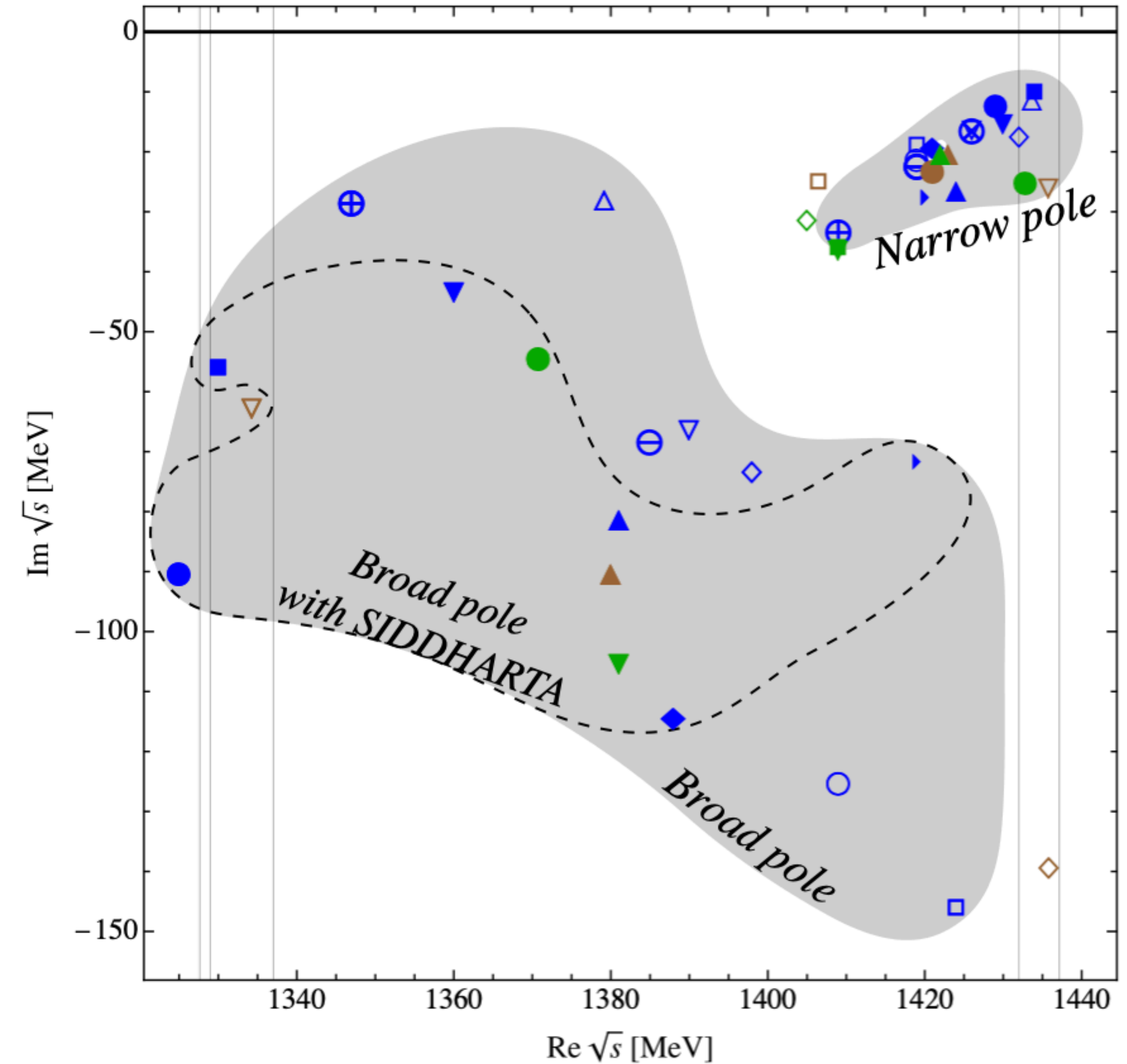
[3] Shevchenko Phys.Rev.C 85 (2012) 034001; MM/Epelbaum/Baru/Rusetsky *Phys.Rev.D* 91 (2015) 5; Gal Int.J.Mod.Phys.A 22 (2007) 226-233;

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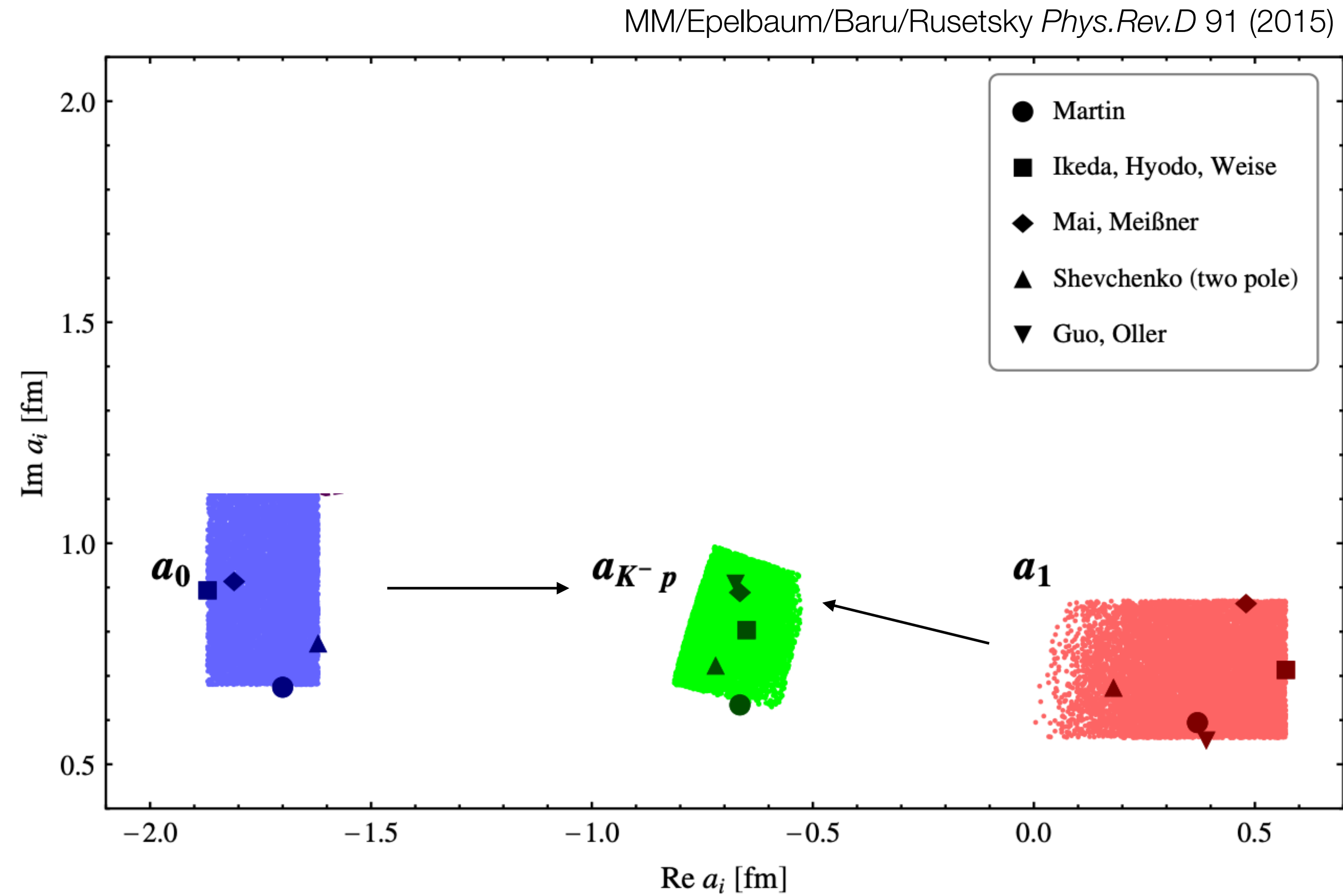
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SIDDHARTA 1 & 2

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[1] Bazzi et al. SIDDHARTA collaboration (2009)

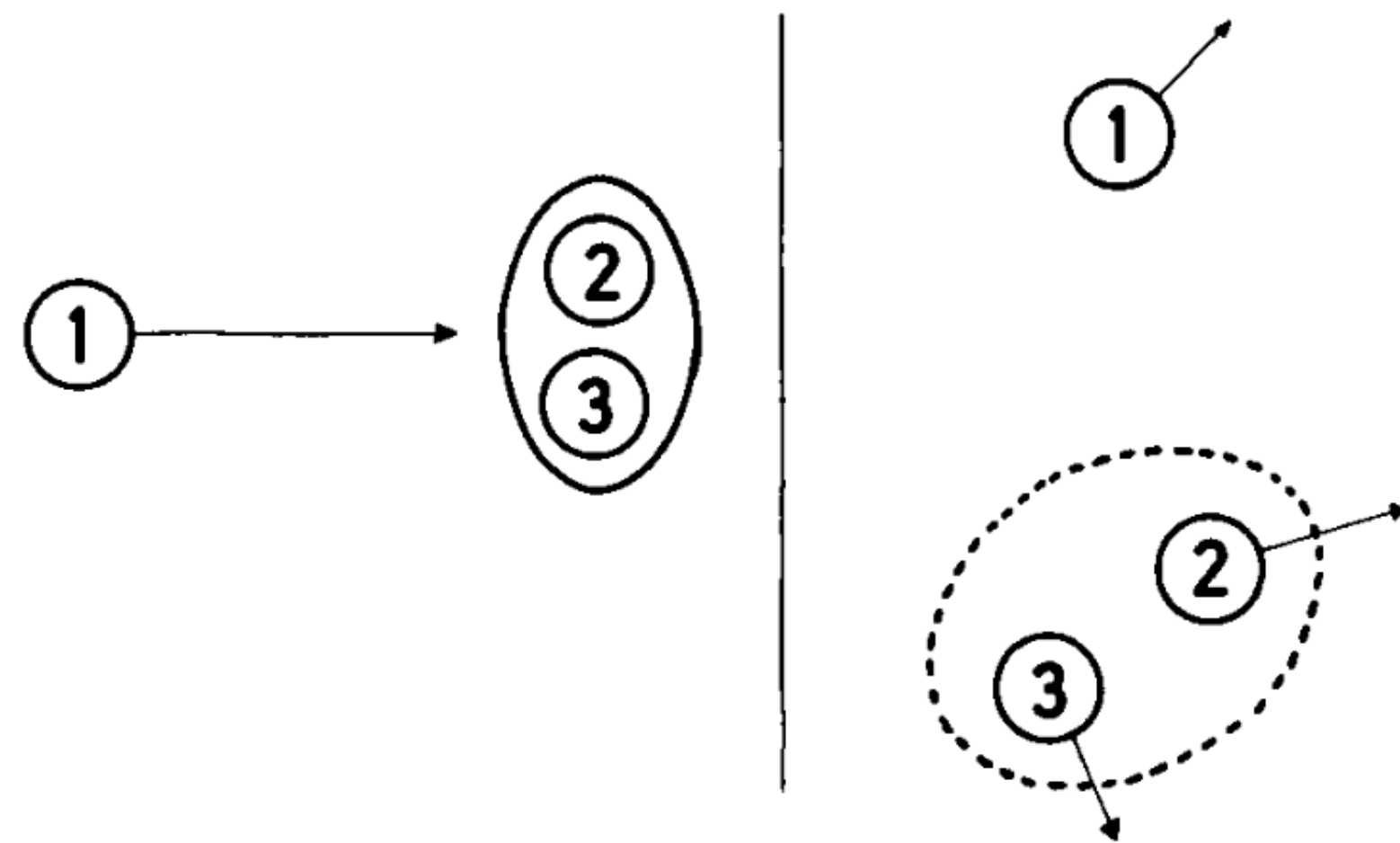
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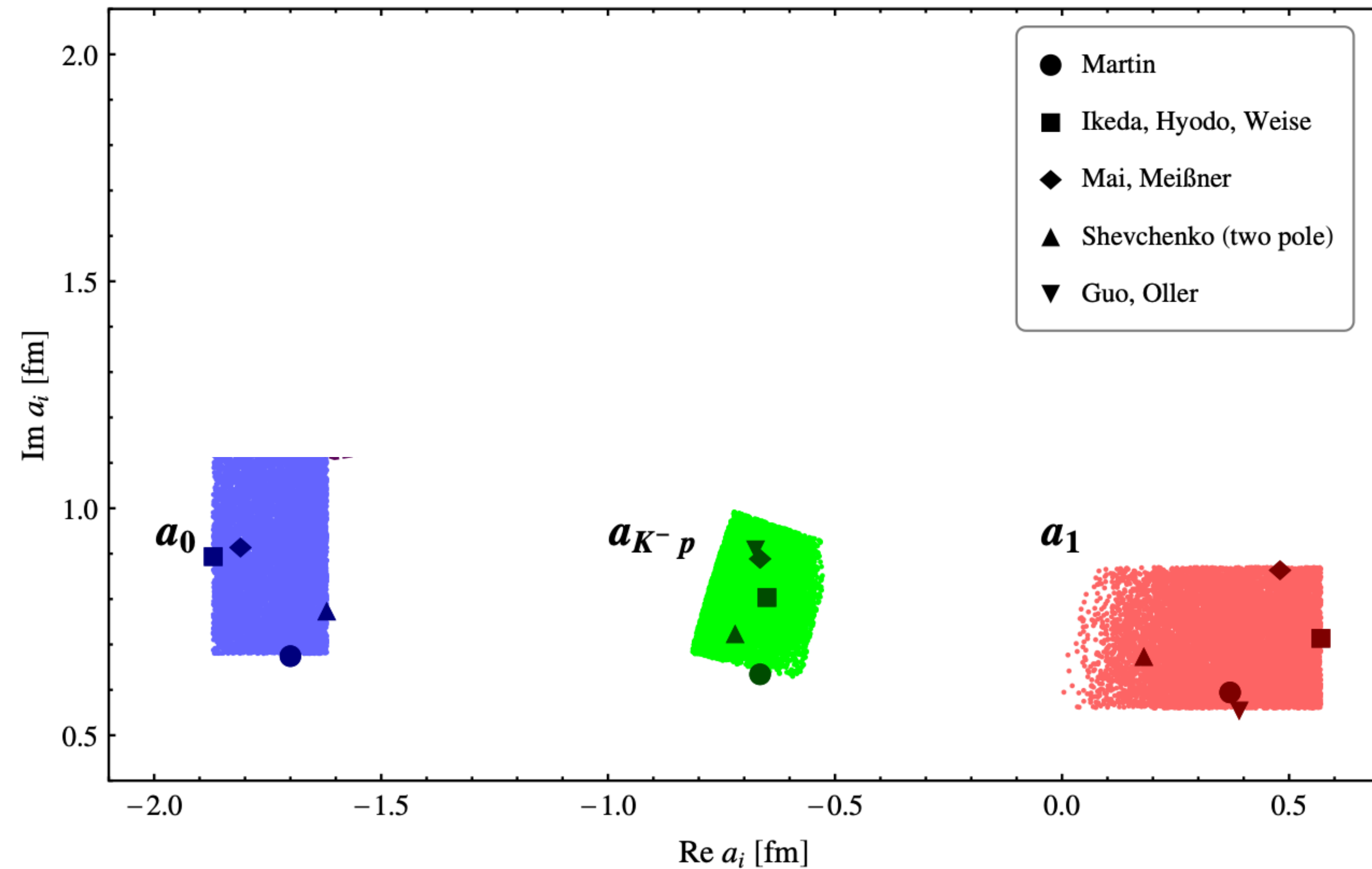
SIDDHARTA 1 & 2

Kaonic deuterium^[2]

- another datum needed to constrain $\{a_{K-p}, A_{\bar{K}d}\} \longleftrightarrow \{a_0, a_1\}$
- three-body scattering intricate^[3]



MM/Epelbaum/Baru/Rusetsky *Phys.Rev.D* 91 (2015)



[1] Bazzi et al. SIDDHARTA collaboration (2009)

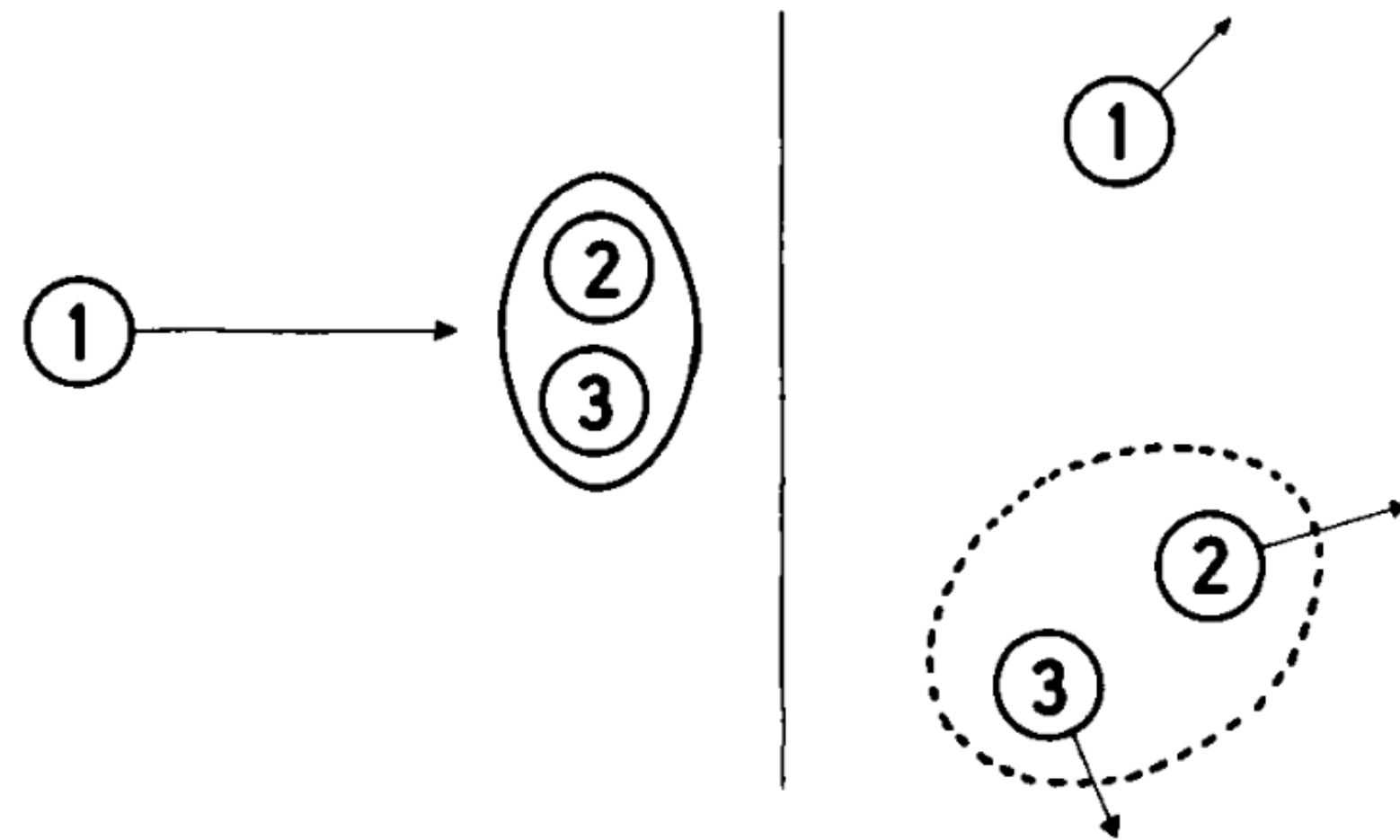
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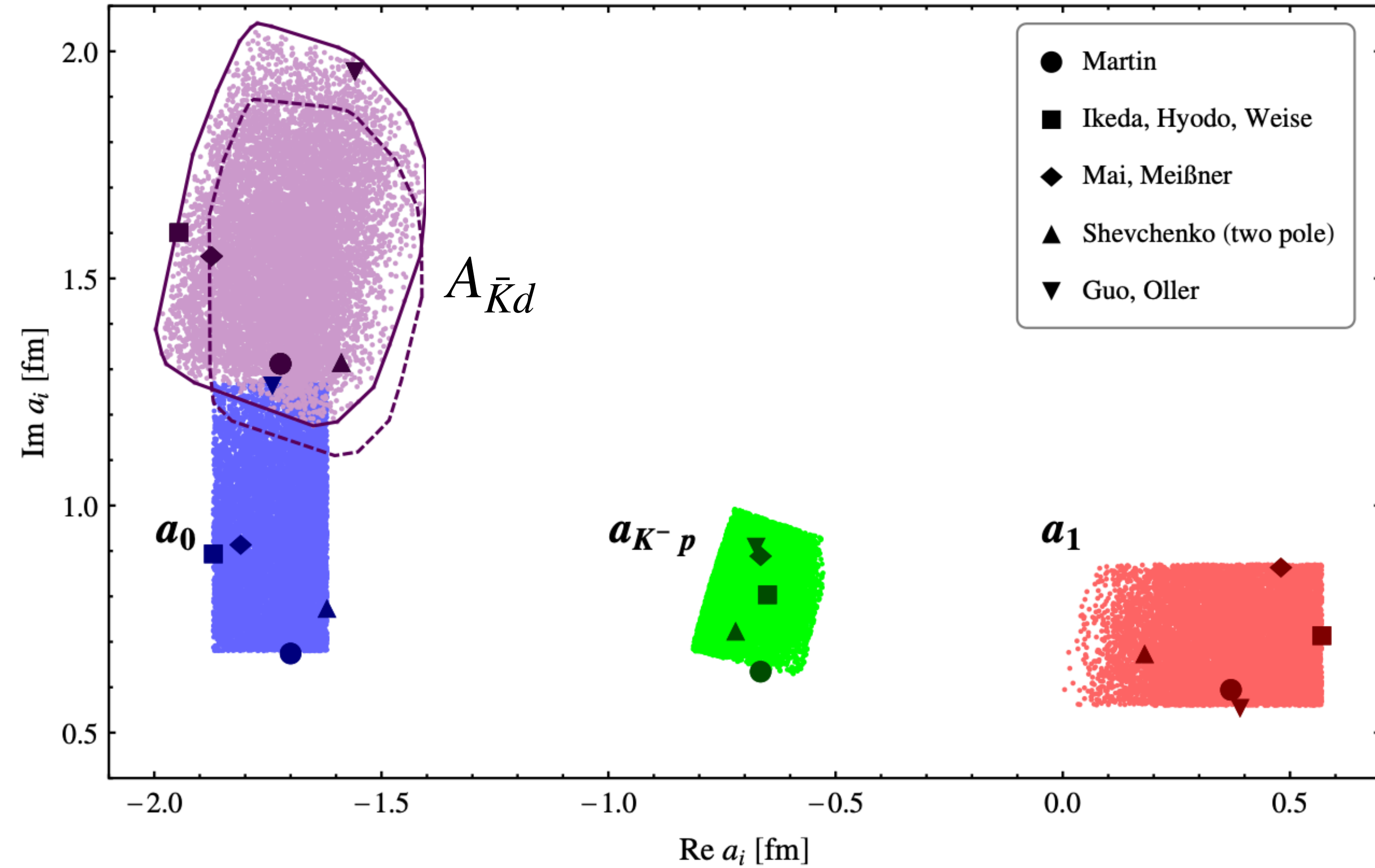
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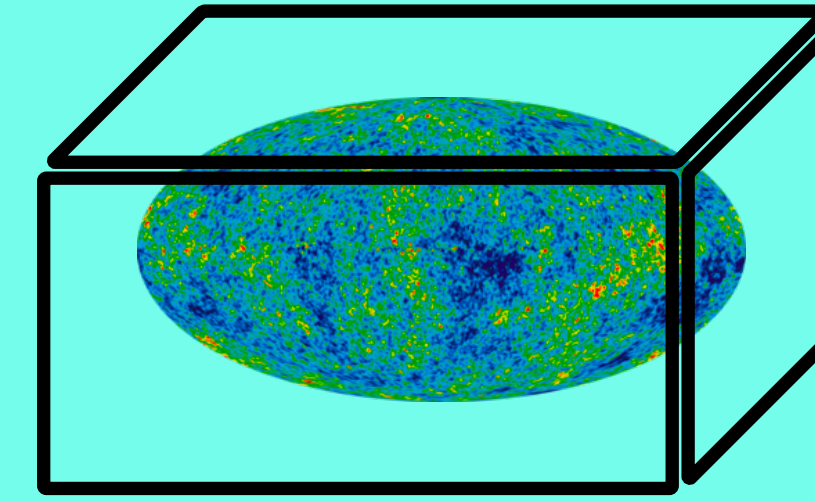
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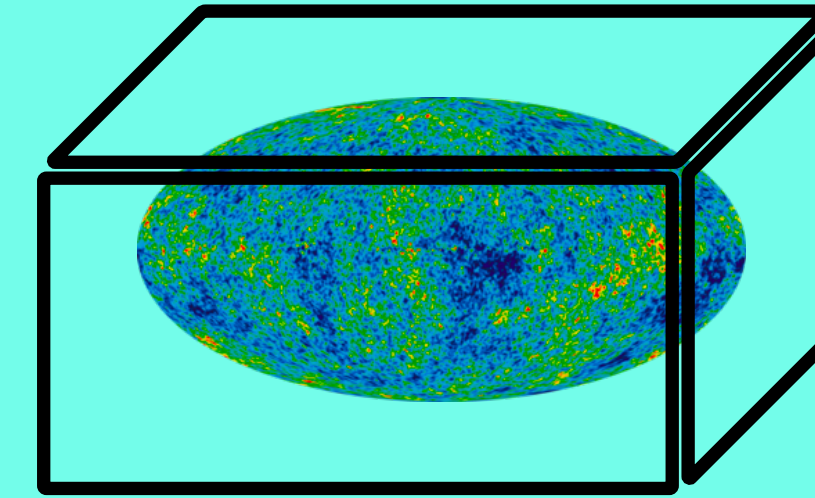
LATTICE QCD

Heavy Universe in a box

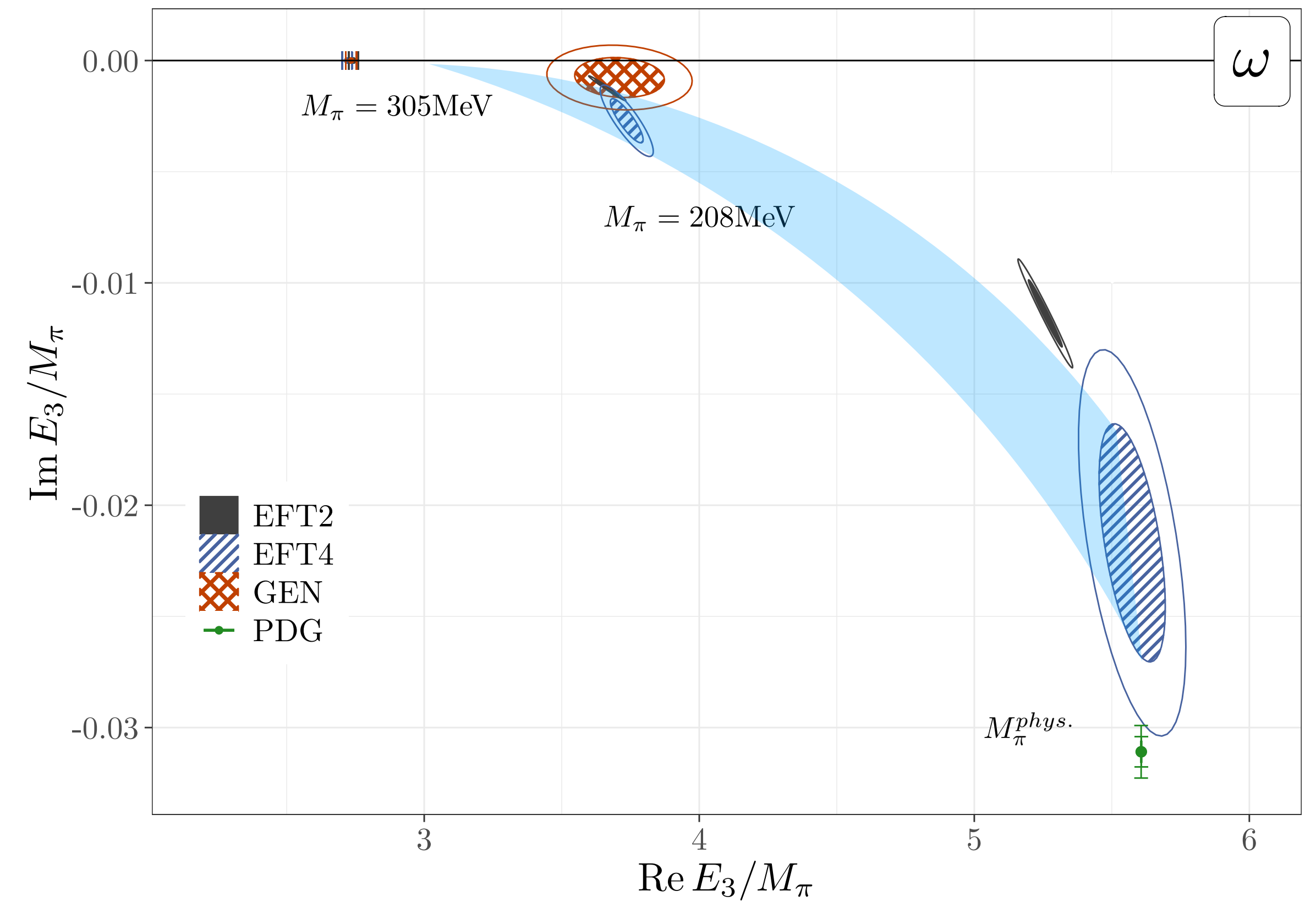
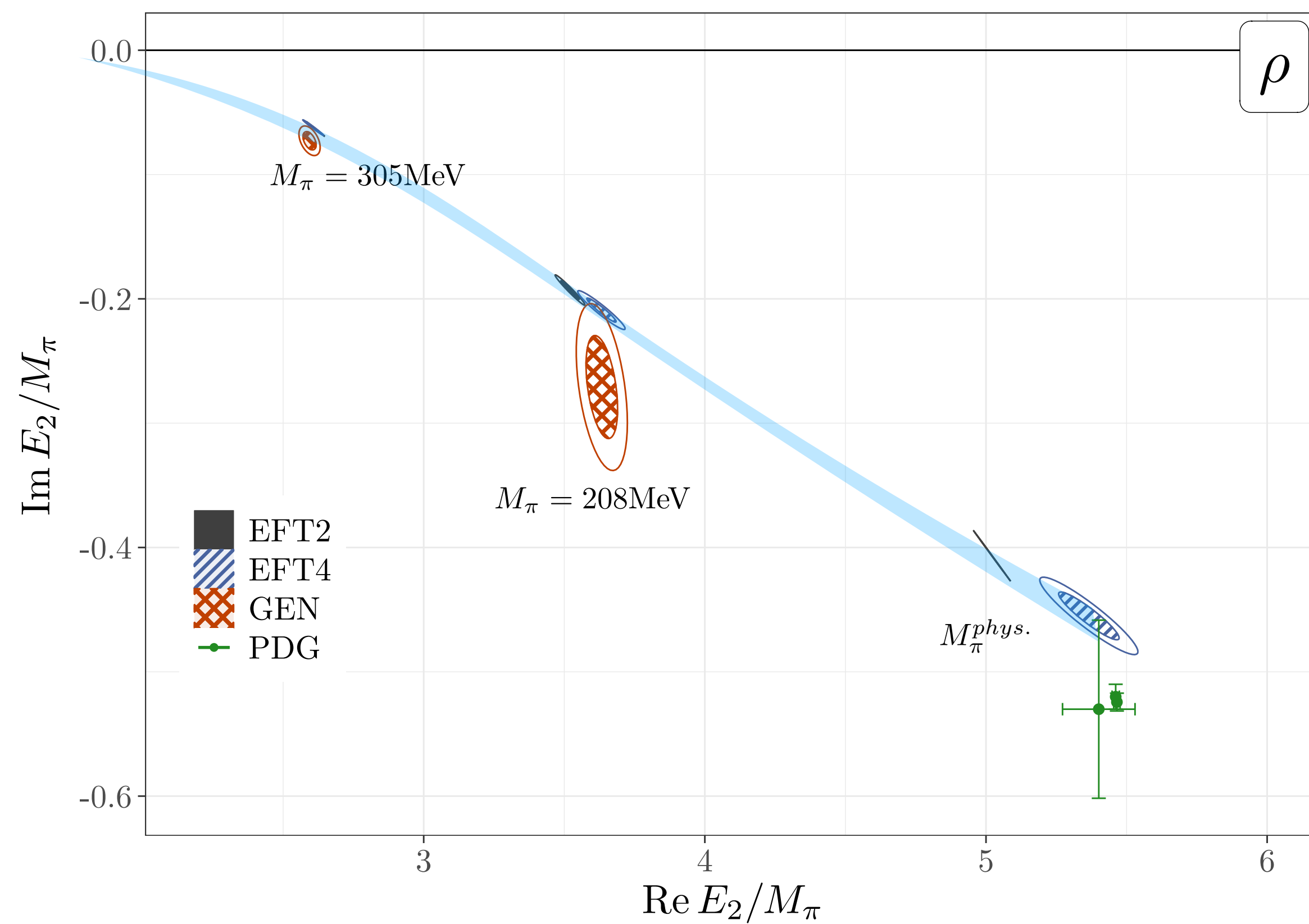


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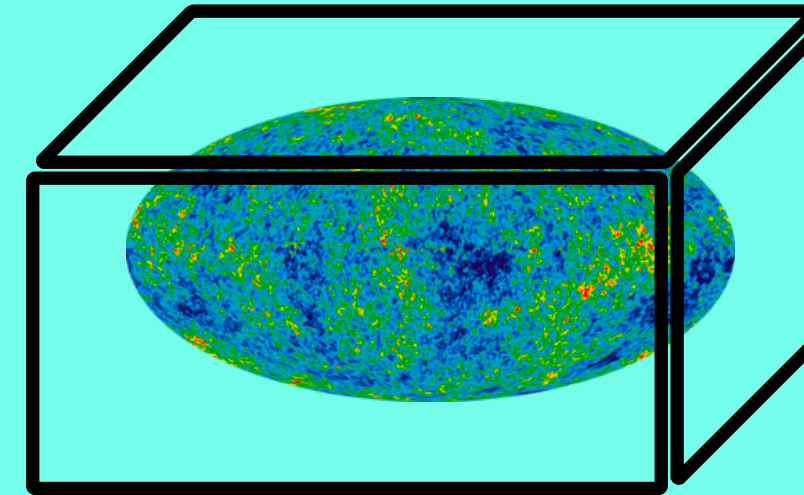
current frontier: 2- & 3-body resonances



ArXive: 2407.16659

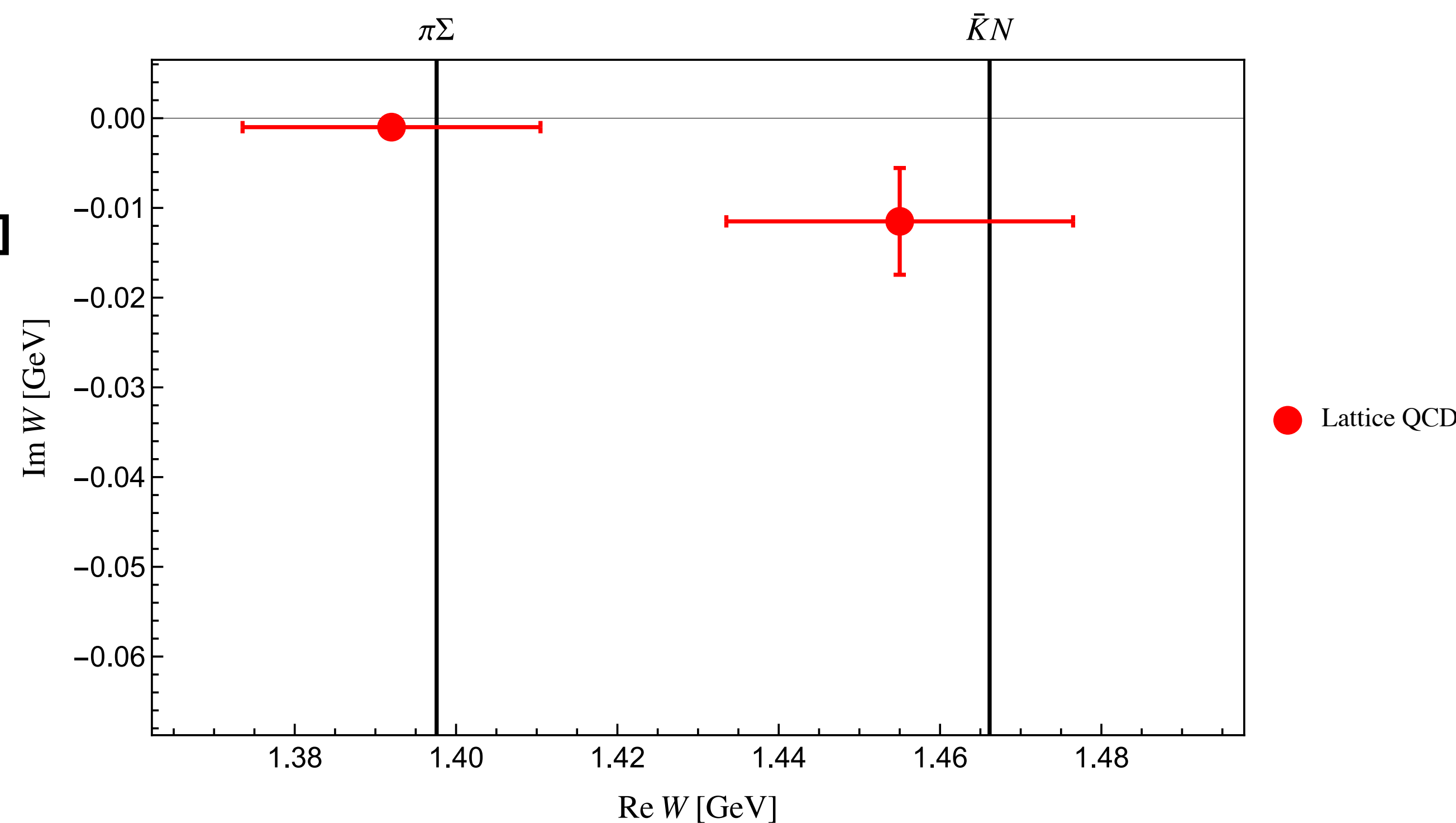
LATTICE QCD

Heavy Universe in a box



Available Lattice spectrum – BaSc setup^[1]

- $M_\pi \approx 200 \text{ MeV}$ $M_K \approx 487 \text{ MeV}$
- two poles! (K-matrix)



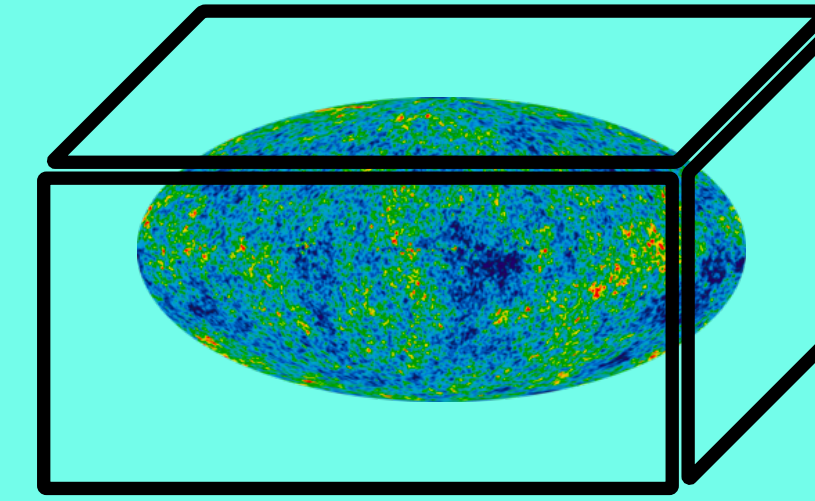
[1] [BaSc] Bulava et al. Phys.Rev.Lett. 132 (2024) 5; 2307.13471

[2] Guo/Kamyia/MM/Meißner Phys.Lett.B 846 (2023)

[3] Pittler/MM in preparation

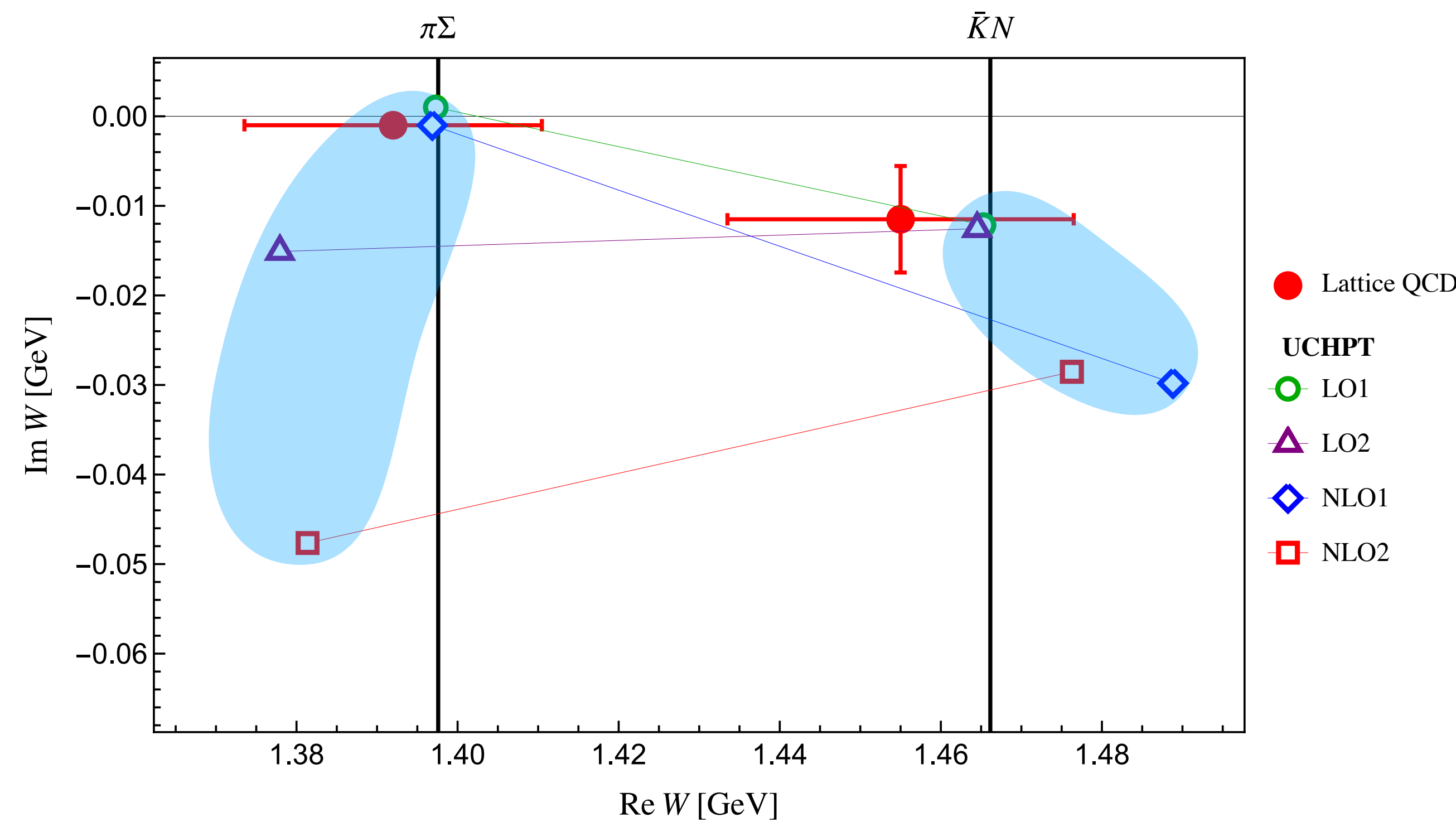
LATTICE QCD

Heavy Universe in a box



Unified (LQCD+UCHPT+Exp) analysis^[2,3]

- two poles
- positions: mostly ok^[2], but not always^[3]...



Guo/Kamyia/MM/Meißner Phys.Lett.B 846 (2023)

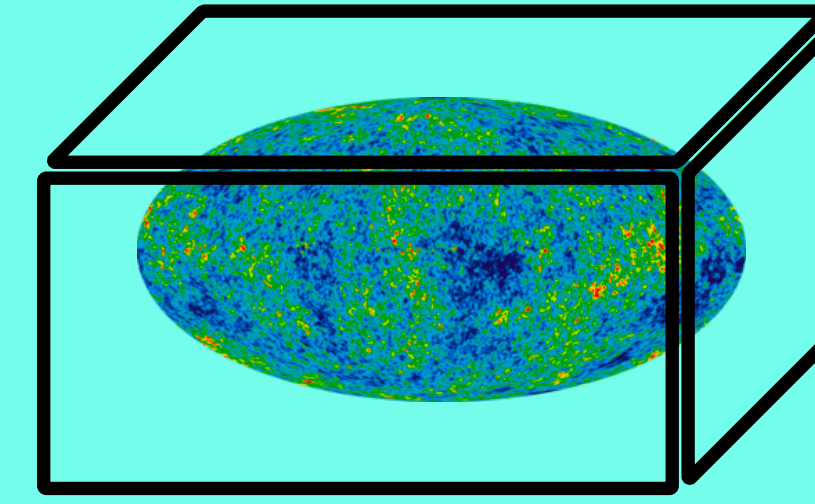
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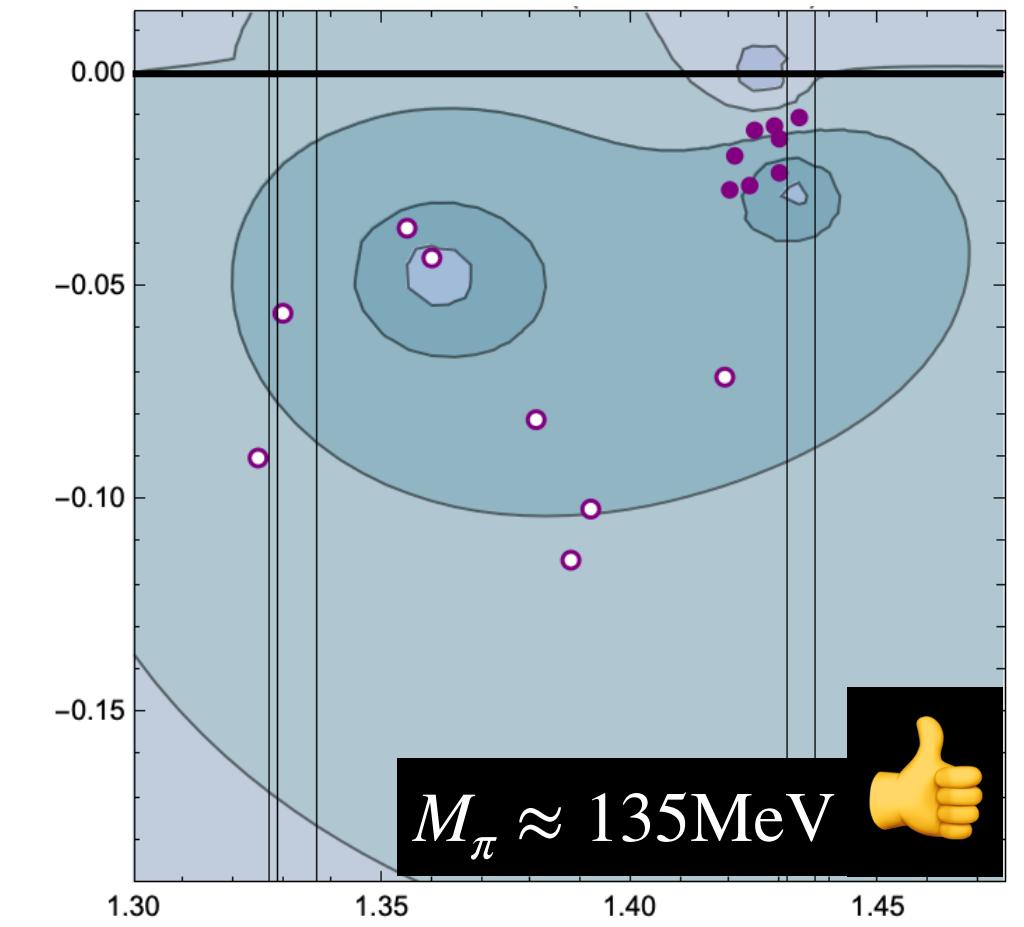
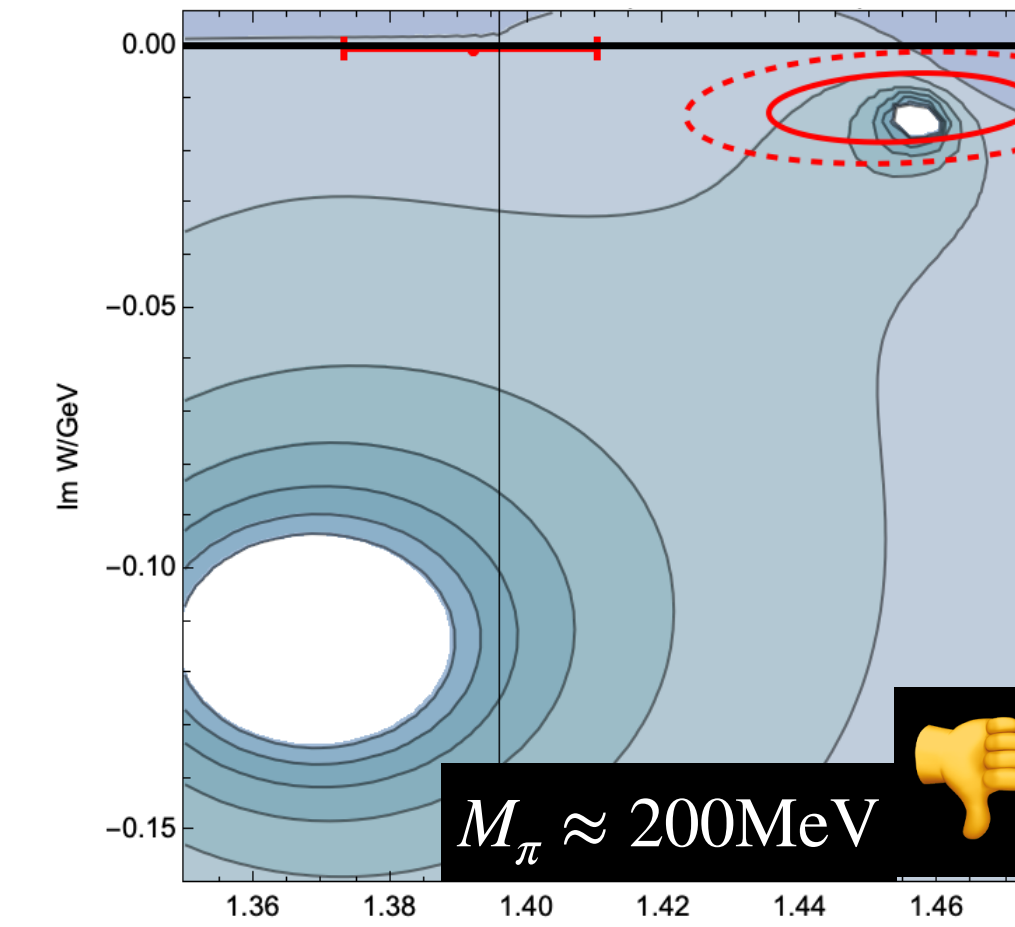
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Heavy Universe in a box

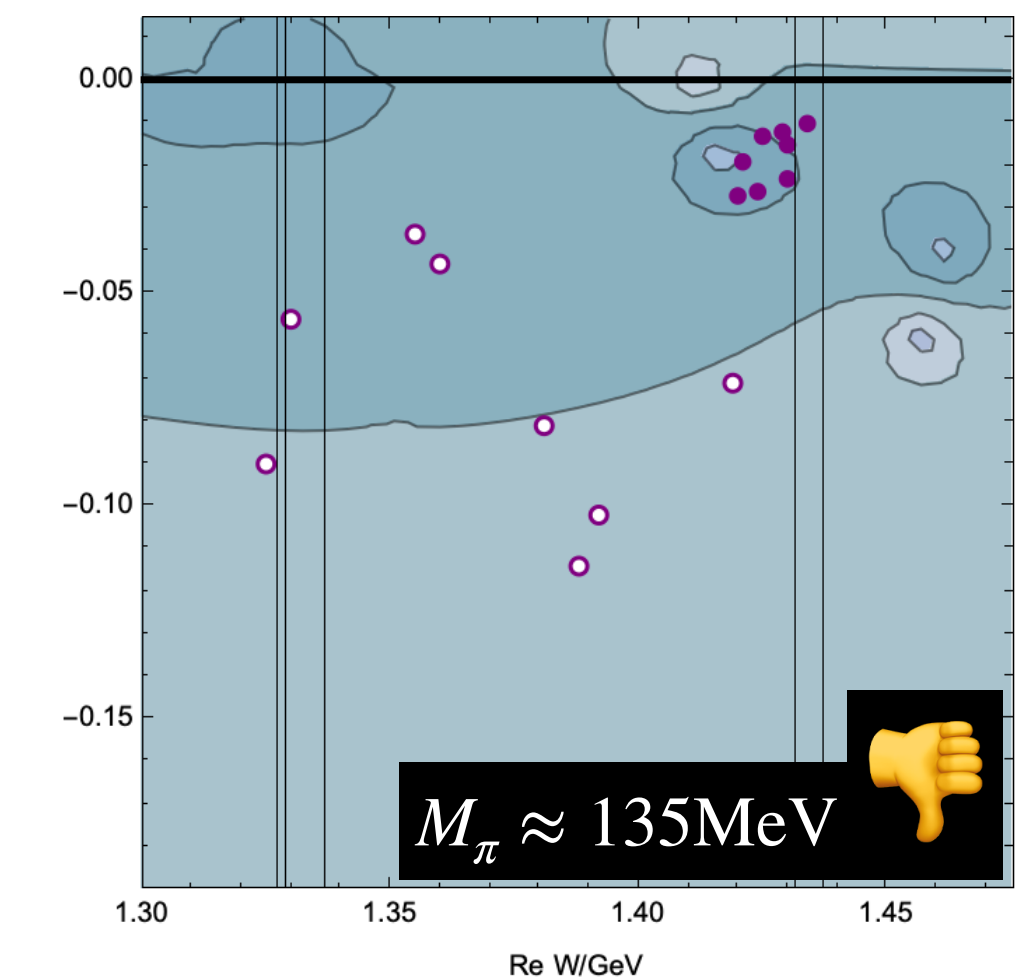
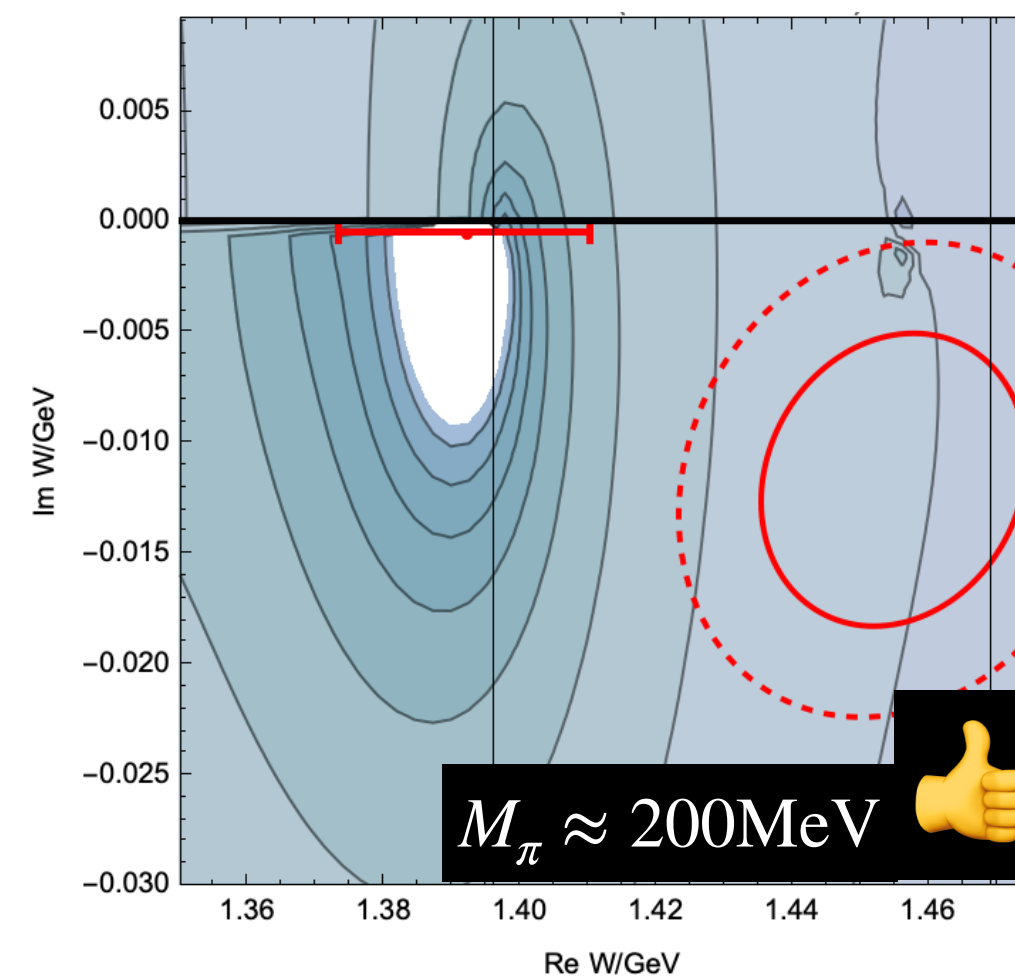


Unified (LQCD+UCHPT+Exp) analysis^[2,3]

- two poles
- positions: mostly ok^[2], but not always^[3]...



FIT A



FIT B

• LQCD/Kmatrix

• UCHPT/1405 • UCHPT/1380

[1] [BaSc] Bulava et al. Phys.Rev.Lett. 132 (2024) 5; 2307.13471

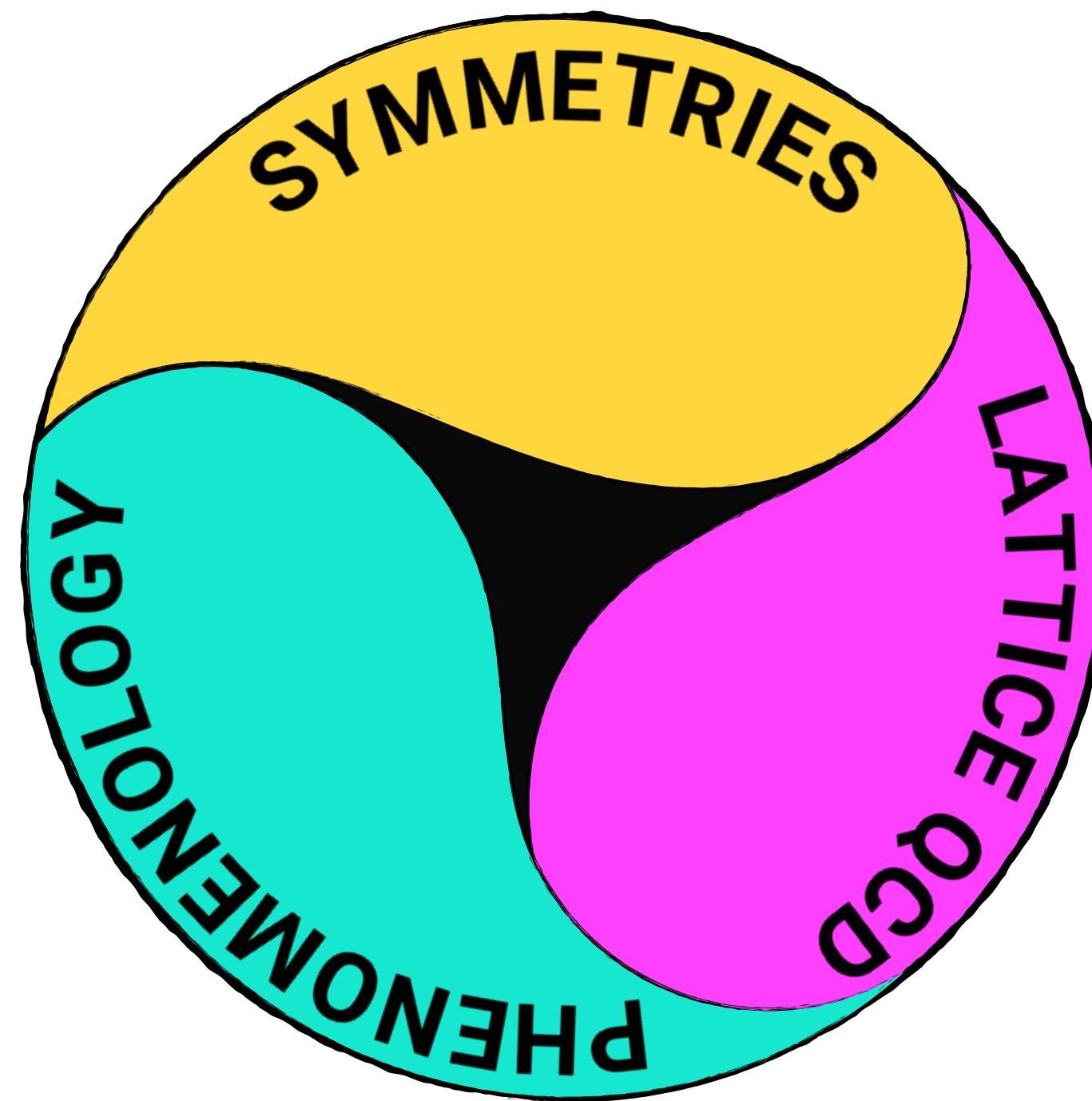
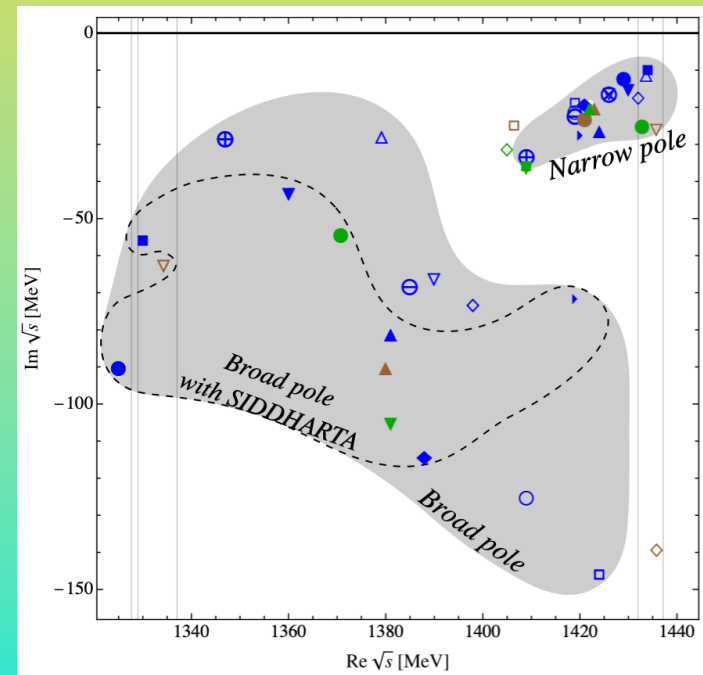
[2] Guo/Kamyia/MM/Meißner Phys.Lett.B 846 (2023)

[3] Pittler/MM in preparation

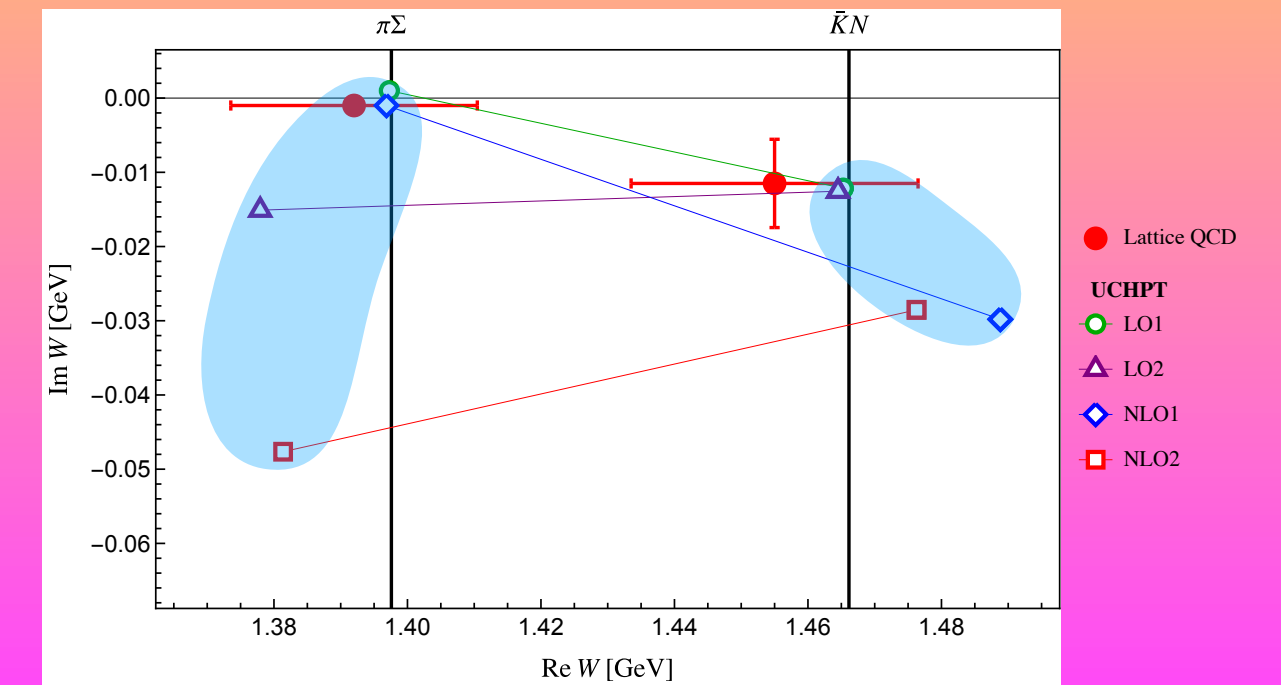
SUMMARY/OUTLOOK

“Kaon-nucleon interaction probes the limits of our understanding of QCD”

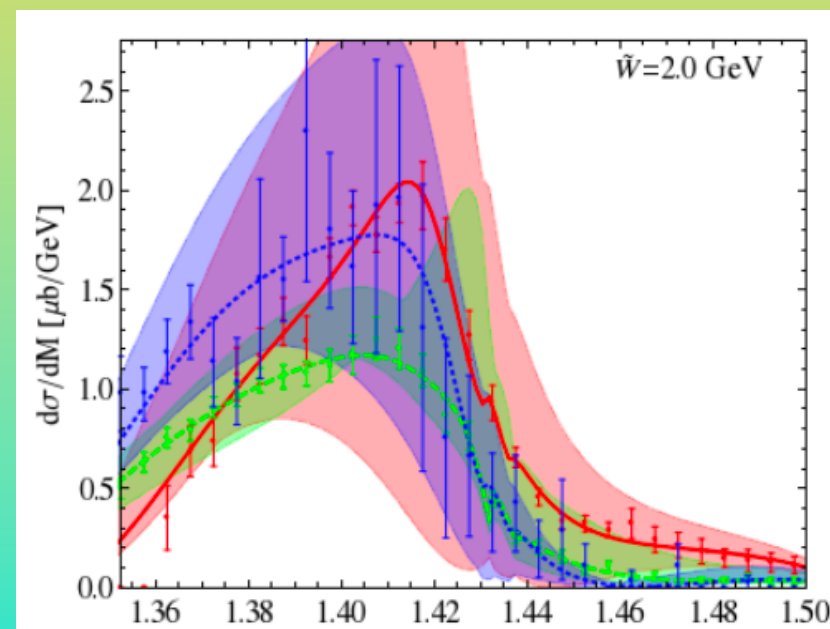
- S-Matrix & QCD symmetries
- Two-pole picture



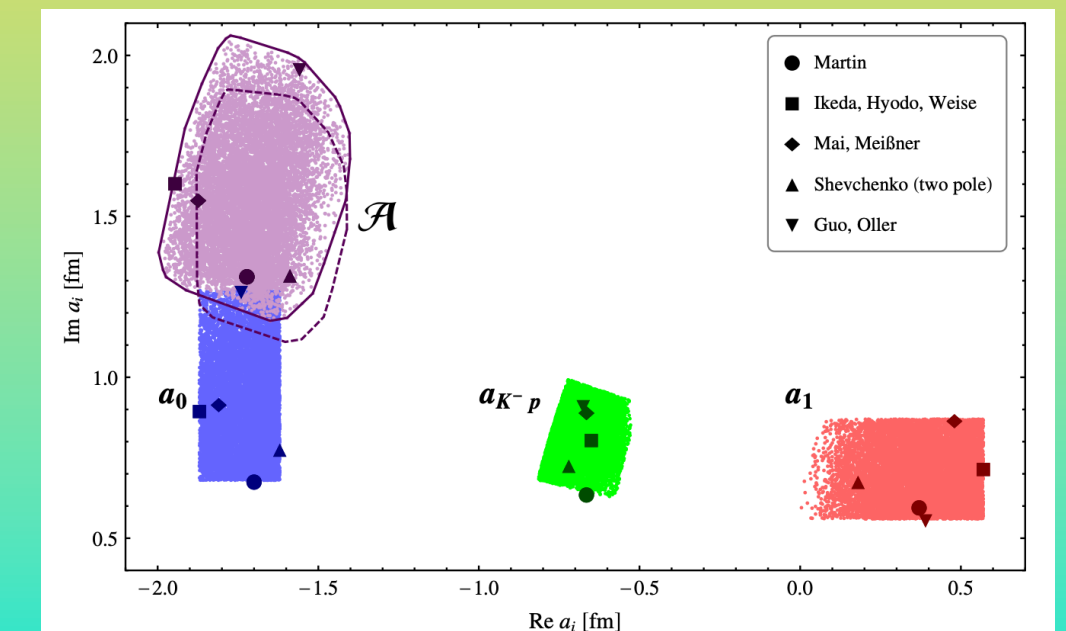
- Two-pole picture persists
- Chiral extrapolations under way



- photo-production data
- new narrow constraints

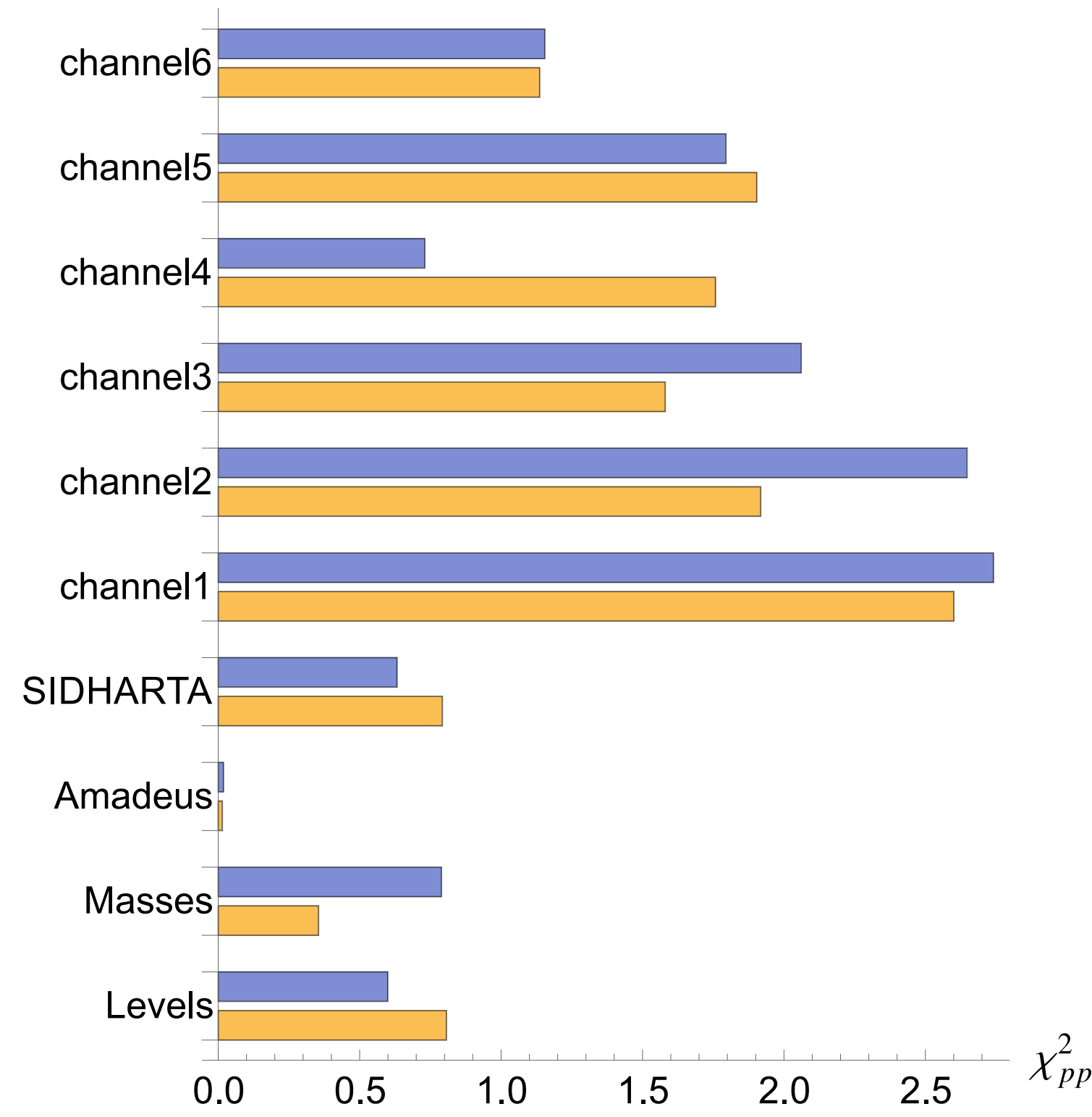


- Kaonic hydrogen
- Kaonic deuterium >> NEXT TALK



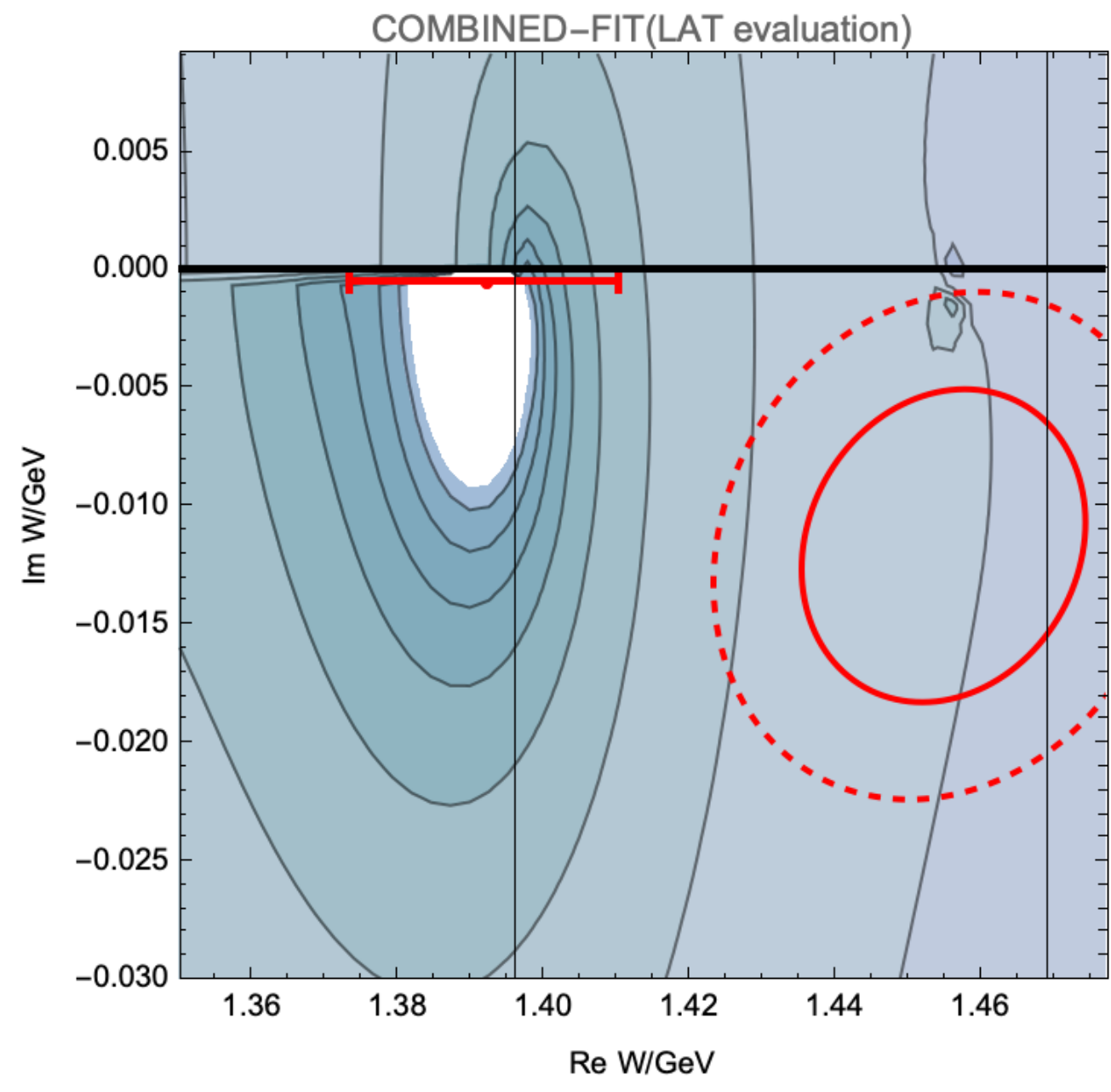
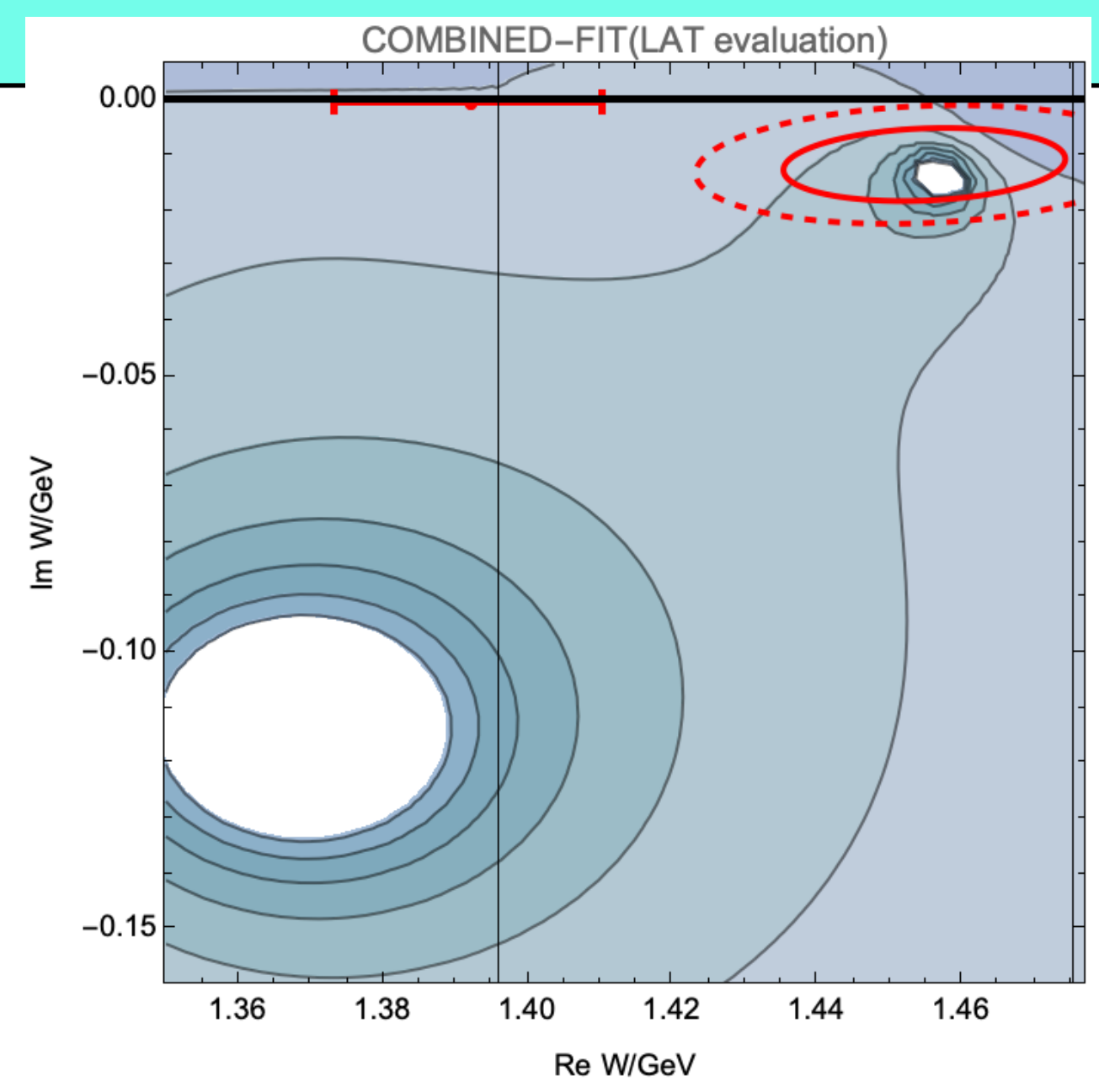
$M_\pi \approx 200$ MeV

$M_\pi \approx 135$ MeV

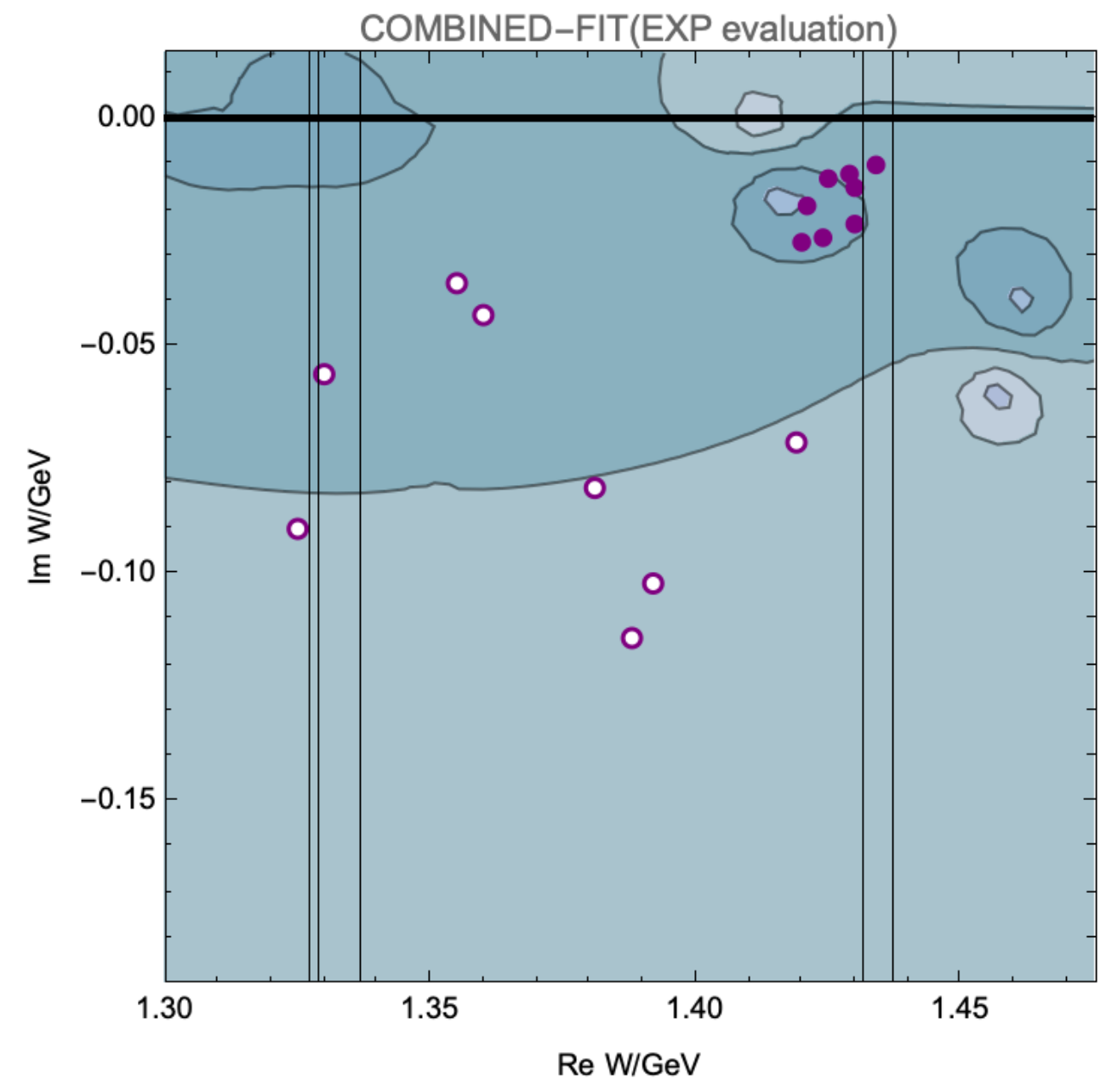
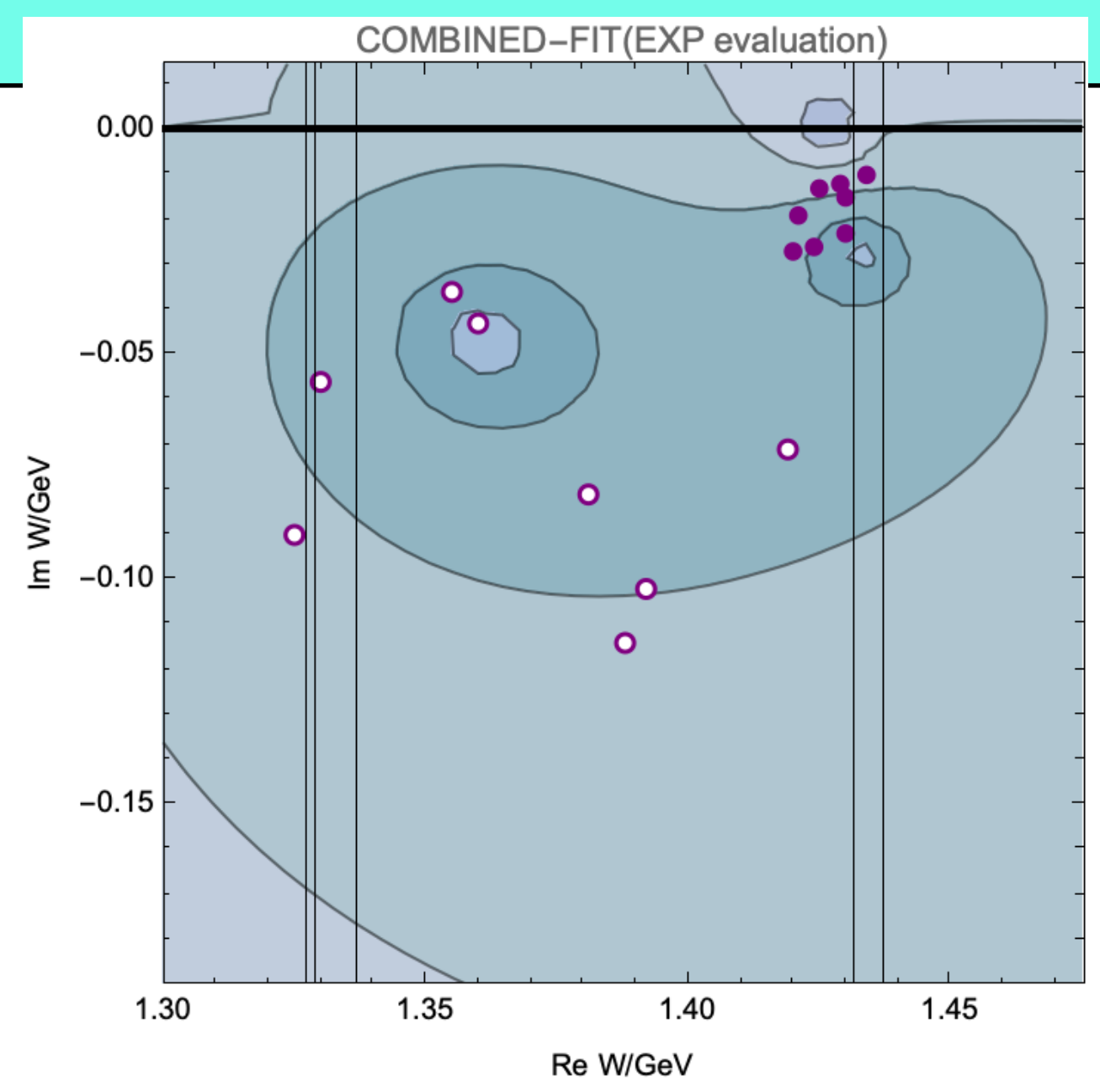


FIT A

FIT B



• LQCD/Kmatrix



• UCHPT/1405 • UCHPT/1380

PRELIMINARY
Pittler/MM in preparation

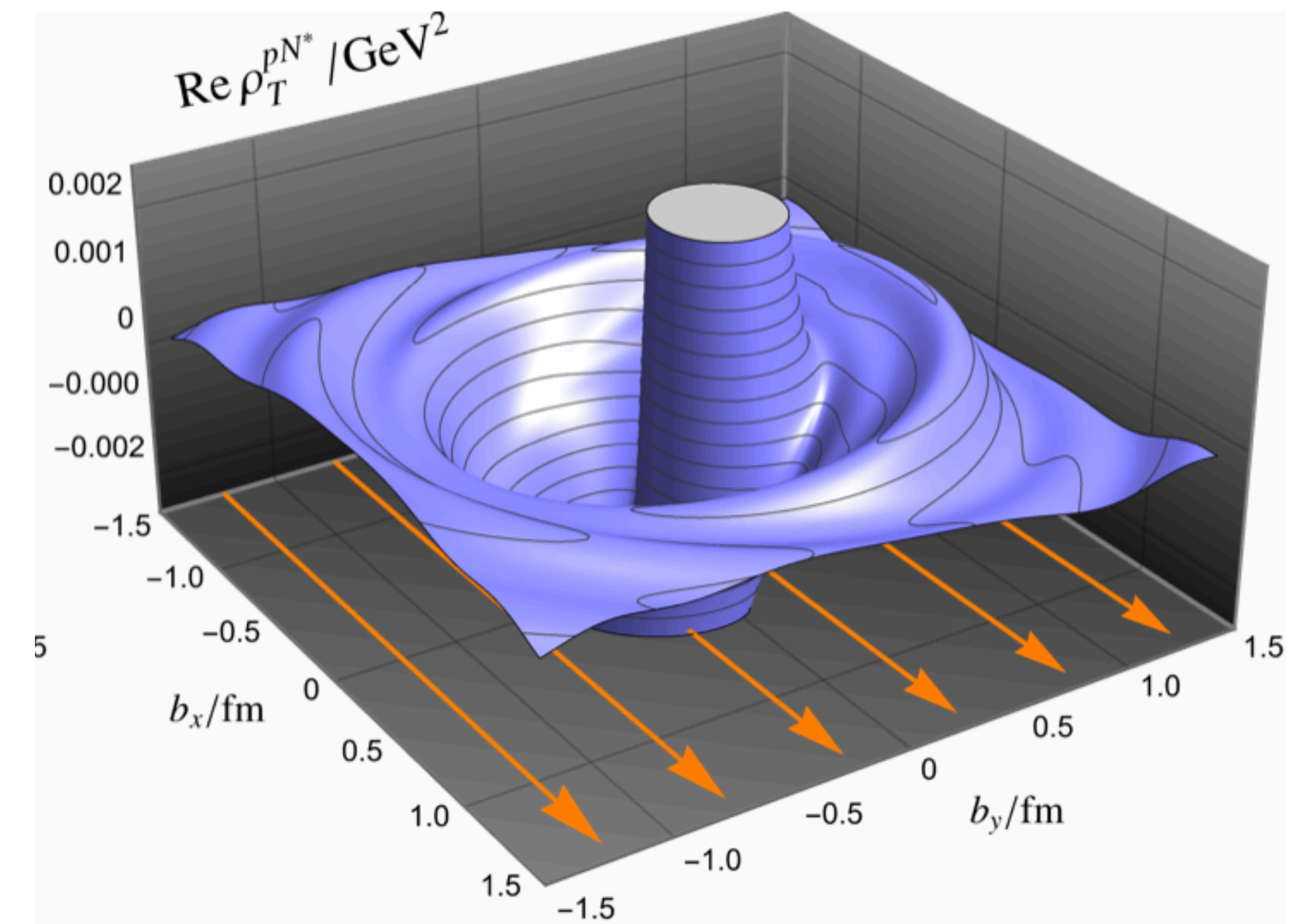
PHOTON INDUCED REACTIONS

Upcoming data from CLAS@JLAB

- New data upcoming in $-3 < S < +3$ Hyperons...^[1]

Virtual photons?

- Hadron structure probe^[2]
- Charge distribution in the excited states^[3]



LF CHARGE DISTRIBUTION OF ROPER N(1440)
[JBW] Wang et al. in print at PRL e-Print: [2404.17444](https://arxiv.org/abs/2404.17444)

[1] Garcia-Recio/Lutz/Nieves *Phys.Lett.B* 582 (2004) 49-54; ... **Vonk/MM in preparation**

[2] Aznauryan/Burkert, *Prog. Part. Nucl. Phys.* 67, 1 (2012); Ramalho/ Peña, *Prog. Part. Nucl. Phys.* 136, 104097 (2024) Tiator et al. *CPC(HEP & NP)*, 2009, 33(X)

LATTICE QCD

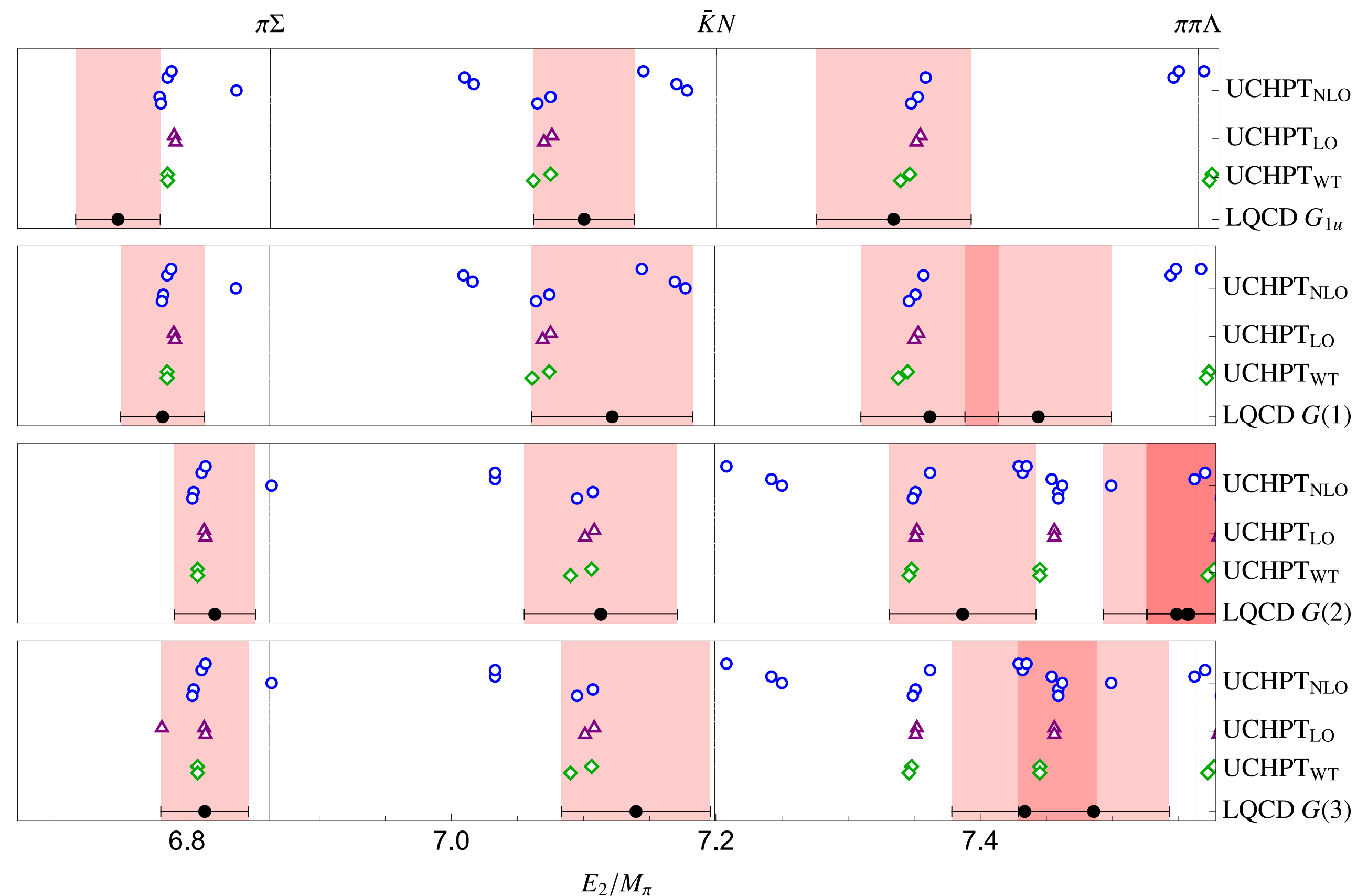
preliminary

Available Lattice spectrum — BaSc setup^[1]

$$M_\pi \approx 200 \text{ MeV} \quad M_K = \approx 487 \text{ MeV}$$

Unified analysis^[2] LQCD+UCHPT+Experiment

... mostly ok, but not always



[1] [BaSc] Bulava et al. Phys.Rev.Lett. 132 (2024) 5; 2307.13471

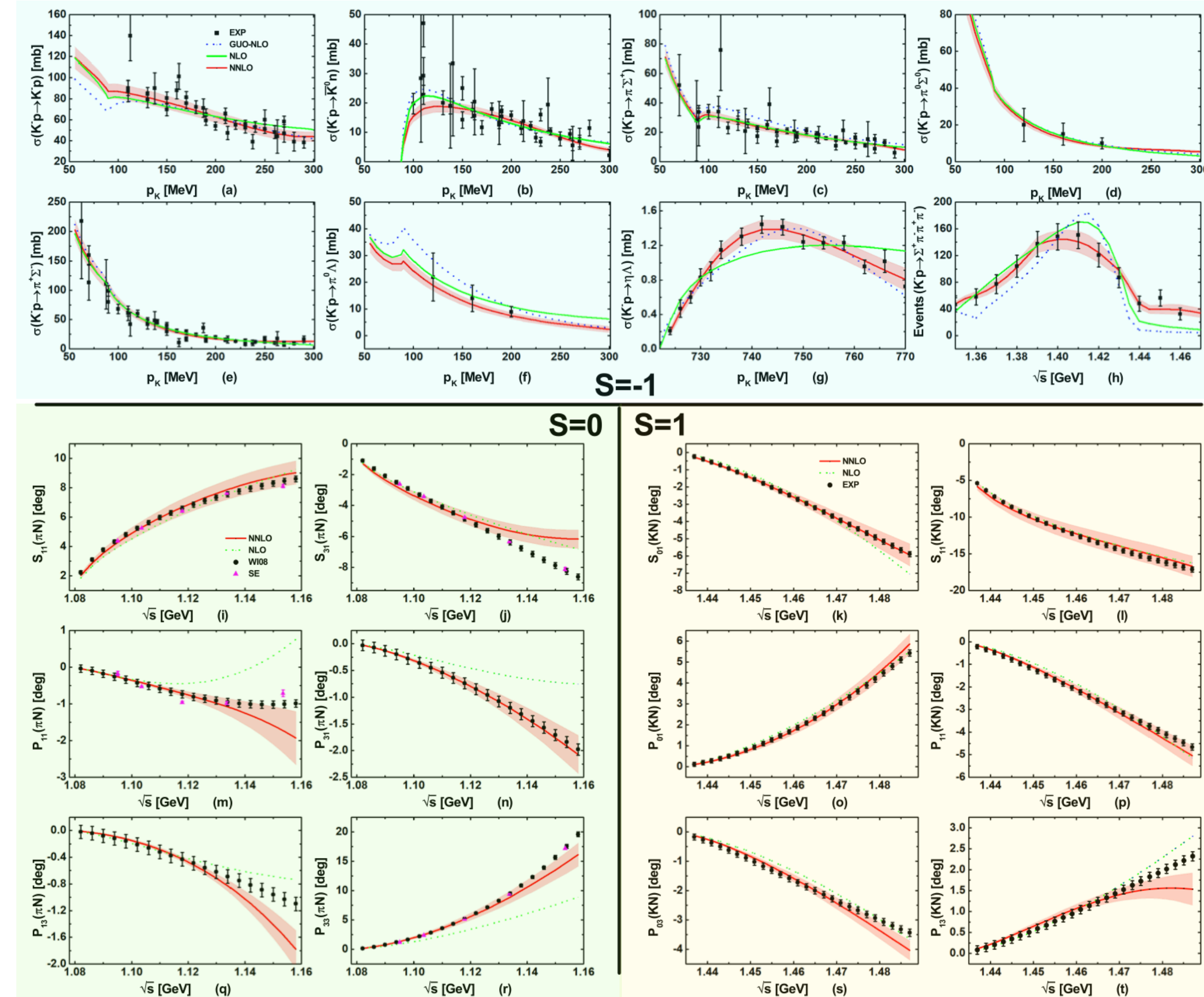
[2] Pittler/MM in preparation

MESON-BARYON SCATTERING

- Various implementations

- ➔ many scenarios with NLO kernel¹ tested

- ➔ first NNLO calculation² including $K_{bar}N/\pi N/KN$



1) Ikeda et al. (2012); Guo/Oller (2013); MM/Meißner (2013,14); Sadasivan et al. (2019)

2) Lu/Geng/Döring/MM (2022)

Lu/Geng/Döring/MM (2022)